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Spatio-temporal data classification through multidimensional sequential patterns: Application to crop mapping in complex landscape



Artificial Intelligence

Yoann Pitarch^a, Dino Ienco^{c,d,*}, Elodie Vintrou^{b,d}, Agnès Bégué^{b,d}, Anne Laurent^e, Pascal Poncelet^e, Michel Sala^e, Maguelonne Teisseire^{c,d}

^a IRIT, Toulouse, France

^b CIRAD, France

^c Irstea, France

^d UMR TETIS - 500 rue Jean-François Breton, 34093 Montpellier, France

^e LIRMM - CNRS - UM2, France

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1. Introduction

This work was motivated by a real-world problem in which the final goal is to monitor areas that are not easy to access in order to perform food risk analysis. The northern fringe of sub-Saharan Africa (Sahel belt) is considered to be particularly vulnerable to climate variability and change, which is why food security remains a major issue in this region (Lobell et al., 2008). One of the preliminary stages necessary for analyzing climate variabilities on agriculture is a reliable estimation of the cultivated land at a national scale. To perform this task, we need to know whether data from several sources (e.g. field surveys, climate, satellite images) can provide a correct assessment of the distribution of cultivated land at a national scale. Although data from satellite images are very useful for monitoring land surface, the large quantity of spatiospectro-temporal measurements stored by the instruments limits the usefulness as sources of information. In recent years, research on spatio-temporal databases has consequently increased alongside research on mining such data (Bogorny and Shekhar, 2010).

In our analysis, the main problem is to combine heterogeneous sources of information (temporal and static information) to exploit

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ABSTRACT

The main use of satellite imagery concerns the process of the spectral and spatial dimensions of the data. However, to extract useful information, the temporal dimension also has to be accounted for which increases the complexity of the problem. For this reason, there is a need for suitable data mining techniques for this source of data. In this work, we developed a data mining methodology to extract multidimensional sequential patterns to characterize temporal behaviors. We then used the extracted multidimensional sequences to build a classifier, and show how the patterns help to distinguish between the classes. We evaluated our technique using a real-world dataset containing information about land use in Mali (West Africa) to automatically recognize if an area is cultivated or not.

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the full set of dimensions without losing information. To this end, we first need to combine multidimensional temporal and static data. Second, we need a model from which the analyst can easily obtain a clear explanation, since, many previous models are black box models that do not provide a useful explanation for the classification (Qin and Obradovic, 2006).

We thus developed a data mining methodology to extract relevant multidimensional sequential patterns from both static descriptions and temporal behaviors.

In data mining literature the term multidimensional is used as a synonym for multi-attribute data that, instead, is commonly employed by researchers in statistics. In the rest of the paper we mainly use multidimensional as the proposed approach comes from the data mining field.

In our scenario, multidimensional (or multi-attribute) temporal measurements are obtained from moderate resolution remote sensing images. In the second step, we exploit the acquired know-ledge (in terms of sequential patterns) to build a classifier to distinguish between cultivated and non-cultivated areas. Classification techniques based on frequent patterns have been adopted in Zaiane et al. (2002) and Chien and Chen (2010). Nevertheless, since these approaches are based on association rules, the temporal aspect is not taken into account within the classification

^{*} Corresponding author.

rules. One of our originality is to propose a sequential rules-based approach. We applied our model to a real-world dataset from Mali, a representative country of the African Sahel Belt, in which monitoring crop production is a major issue.

In particular, the focus of our analysis is devoted to manage and exploit the temporal dimension of the data while we did not deal with the spatial one. This choice is motivated by the kind of data we analyzed in which the temporal aspect plays the main role. In the case the most important dimension of the problem is the spatial one, we refer the interested reader to other techniques explicitly designed to cope with spatial correlations among the data (Jiang et al., 2013).

The main contributions of our work are the following:

- the management of static and dynamic dimensions of temporal data;
- an heuristic approach to filter out irrelevant static dimensions;
- a model where the rules of the classifier are available for detailed inspection by the analyst.

The reason why, for our study, we adopt multidimensional sequential patterns instead of standard machine learning approaches (such as decision trees, support vector machine, Witten and Frank, 2005) is the capacity of these techniques to capture temporal correlation among data. Standard machine learning approaches mainly work on static data and they are not able to intelligently manage this important dimension of analysis.

The proposed approach is an extension of a preliminary work focused on the pattern extraction (Pitarch et al., 2011).

The paper is organized as follows: Section 2 supplies problem and preliminaries definitions, in Section 3 we introduce a running example. We describe our approach in Section 4. Section 5 describes the satellite and ground dataset we used for our analysis. In Section 6 we present results of our experiments. In Section 7 we give a brief overview of the state of the art. Finally, in Section 8 we conclude.

2. Problem definition and preliminaries

In this section, we present the concepts and definitions concerning multidimensional sequential patterns that were inspired by the notations introduced in Plantevit et al. (2005). For each table defined in the set of dimensions *D*, we consider a partition of *D* into three sets: D_t for the temporal dimension, D_A for the analysis dimensions and D_R for the reference dimension. Each tuple $c = (d_1, ..., d_n)$, with *n* being the number of dimensions, can thus be denoted as c = (r, a, t) with *r* being the restriction on D_R , *a* the restriction on D_A and *t* the restriction on D_t . We first provide an example to illustrate subsequent definitions.

Example 1. Let $D = \{A_{Id}, A_1, A_2, A_3, A_T\}$ be a 5-set of dimensions such that $D_t = \{A_T\}$, $D_R = \{A_{Id}\}$ and $D_A = \{A_1, A_2, A_3\}$. Table 1 shows some tuples from *D*. Following the aforementioned notations, the

Table 1An example of table, *T*.

A _{Id}	A_T	A_1	A ₂	<i>A</i> ₃
1	1	<i>a</i> ₁₁	a ₂₂	a ₃₂
1	2	a ₁₂	a ₂₂	a ₃₁
1	3	a ₁₁	a ₂₁	a ₃₁
2	1	a ₁₂	a ₂₁	a ₃₂
2	2	<i>a</i> ₁₁	a ₂₂	a ₃₁
3	1	a ₁₁	a ₂₂	a ₃₁

first tuple $c_1 = (1, 1, a_{11}, a_{22}, a_{31})$ can be rewritten into $c_1 = (r_1, a_1, t_1)$ with $r_1 = (1)$, $a_1 = (a_{11}, a_{22}, a_{31})$ and $t_1 = (1)$.

Definition 1 (*Multidimensional item*). A multidimensional item e defined on $D_A = \{D_1, ..., D_m\}$ is a tuple $e = (d_1, ..., d_m)$ such that $\forall k \in [1, m], d_k \in Dom(D_k)$.

Definition 2 (*Multidimensional sequence*). A multidimensional sequence *S* defined on $D_A = \{D_1, ..., D_m\}$ is an ordered non-empty list of multidimensional items $S = \langle e_1, ..., e_l \rangle$ where $\forall j \in [1, l], e_j$ is a multidimensional item defined on D_A .

Example 2. Assuming $D_A = \{A_1, A_2, A_3\}$, two possible multidimensional items are $e_1 = (a_{11}, a_{22}, a_{32})$ and $e_2 = (a_{12}, a_{22}, a_{32})$, and $S_1 = \langle e_1, e_2 \rangle$ is a multidimensional sequence.

Remark 1. In the original framework of sequential patterns (Agrawal and Srikant, 1995), a sequence is defined as an ordered non-empty list of itemsets where an itemset is a non-empty set of items. However, given the scope of this paper, we only consider sequences of items since at each date, one and only one item can occur for each identifier.

An identifier is said to support a sequence if a set of tuples containing the items satisfying the temporal constraints can be found. Given a table *T*, the set of all tuples in *T* with the same restriction *r* over D_R is said to be a *block*. Each block *B* is identified by *r*. Given a total order on the temporal dimension, each block is therefore associated with a multidimensional sequence. and we denote as B_{T,D_R} the set of all blocks that can be built up from table *T*. The set D_R identifies the blocks of the database to be considered when computing supports. The support of a sequence is the proportion of blocks embedding it.

Definition 3 (*Tuple definition*). An identifier $r \in Dom(D_R)$ supports a sequence $S = \langle e_1, ..., e_l \rangle$ if $\forall j \in 1...l, \exists d_j \in Dom(D_t), \exists t = (r, e_j, d_j) \in T$ where $d_1 < d_2 < \cdots < d_l$.

Definition 4 (*Sequence support*). Let D_R be the reference dimensions and T a table partitioned into the set of blocks B_{T,D_R} . The support of a sequence s is defined by

$$support(s) = \frac{|\{B \in B_{T,D_R} | s \text{ is included in } B\}|}{|B_{T,D_R}|}$$

Definition 5 (*Frequent sequence*). Let $minSupp \in [0, 1]$ be a minimum user-defined support value. A sequence *S* is said to be frequent if $support(S) \ge minSupp$.

Example 3. Let us consider B_1 , the block associated with $T_{Id} = 1$. This block is composed of the first three tuples in *D*. Hence, the multidimensional sequence $S_{B_1} = \langle (a_{11}, a_{22}, a_{32})(a_{12}, a_{22}, a_{31}) (a_{11}, a_{21}, a_{31}) \rangle$ naturally reflects the temporal variations on the analysis dimension values of B_1 . Now, let us consider the sequences $S = \langle (a_{11}, a_{22}, a_{32})(a_{11}, a_{21}, a_{31}) \rangle$ and $S' = \langle (a_{11}, a_{22}, a_{32})(a_{11}, a_{21}, a_{31}) \rangle$ $(a_{11}, a_{22}, a_{32}) \rangle$. S_{B_1} supports *S* but not *S'*. The support of *S* is 0.5 since it is only supported by S_{B_1} . Assuming *minSupp*=0.3, *S* will be considered as a frequent multidimensional sequence.

Considering the aforementioned definitions, an item can only be retrieved if there is a frequent tuple of values from domains of D_A containing it. For instance, it could be that neither (a_{11}, a_{22}, a_{32}) nor (a_{11}, a_{22}, a_{31}) is frequent whereas the value a_{11} and even a_{22} are frequent. Thus, Plantevit et al. (2005) introduces the *joker* value *. In this case, we consider $(a_{11}, a_{22}, *)$ which is said to be *jokerized*. A *jokerized* item contains at least one specified analysis dimension. It contains a * only if no specific value from the domain can be set. A *jokerized* sequence is a sequence containing at least one *jokerized* item.

Definition 6 (*Jokerized Item*). Let $e = (d_1, ..., d_m)$ be a multidimensional item. We denote by $e_{[d_i/\delta]}$ the replacement in e of d_i by δ . e is said to be a *jokerized* multidimensional item if

1. $\forall i \in [1, m], d_i \in Dom(D_i) \cup \{*\},\$

2. $\exists i \in [1, m]$ such that $d_i \neq *$,

3. and $\forall d_i = *, \nexists \delta \in Dom(D_i)$ such that $e_{[d_i/\delta]}$ is frequent.

Example 4. Let us assume minSupp = 1. Under this constraint, neither $I_1 = (a_{11}, a_{22}, a_{32})$ nor $I_2 = (a_{11}, a_{22}, a_{31})$ is frequent. Indeed, $support(I_1) = \frac{1}{3}$ and $support(I_2) = \frac{2}{3}$. However, if we now consider the jokerized item $I_3 = (a_{11}, a_{22}, *)$, then such item is frequent with support equals 1.

3. Motivating example

Despite our proposed framework is generic enough to deal with any kind of static and dynamic data, we illustrate our approach through the crop mapping perspective. We thus consider the following scenario that will be used throughout the paper as a running example. Let us consider a relational table T in which NDVI values per field are stored. We assume that *T* is defined over six dimensions (or attributes) as shown in Table 2. The dimension D_t is the date of statements and we consider two dates, denoted as 1 and 2. The *I* dimension is associated with the field identifier and we consider 4 different fields denoted as F1, F2, F3 and F4. The dimension C is the crop type and we consider two discretized values, denoted as FP (food-producing) and NFP (non-food-producing). The dimension S represents the soil type whose values can be GS (gravelly soils), SL (sandy loam) and CL (clay loam). The dimension DV is the distance from the field concerned to the nearest village and we consider two discretized values, denoted as near and far. The dimension NDVI stands for the NDVI value associated with each field at each timestamp and we consider 4 abstract values n_1 , n_2 , n_3 and n_4 for this example. We consider five sets of dimensions as follows: (i) the dimension D_t representing the date, (ii) the dimension I representing the identifier, (iii) the dimensions S and DV, that we call static dimensions since they do not change over time or descriptors (values of these dimensions associated with a given field do not change over time), (iv) the dimension NDVI, that we call dynamic dimension or indicators (values of these dimensions associated with a given field do evolve over time) and (v) the dimension C that we call class. For instance, the first tuple of *T* (Table 2) means that field 1 is a food-producing crop composed of soil CL, near a village and that, at date 1, the *NDVI* value was n_1 . Observing the static attribute values of each class in more detail, some comments should be made. First, food-producing crops are always located near the village whereas soil composition changes. Similarly, non-foodproducing crops are always cultivated on GS whereas the distance to the nearest village changes. A first interpretation of these comments is that the dimension DV appears to be decisive in

Table 2 Table T.

D (Date)	I (Id)	C (Crop)	S (Soil)	DV (Distance to village)	NDVI (NDVI value)
1	F1	FP	CL	Near	<i>n</i> ₁
1	F2	FP	SL	Near	n_1
1	F3	NFP	GS	Far	n ₂
1	F4	NFP	GS	Near	n ₃
2	F1	FP	CL	Near	n_2
2	F2	FP	SL	Near	n_2
2	F3	NFP	GS	Far	n_4
2	F4	NFP	GS	Near	n ₃

identifying food-producing crops whereas the dimension S appears to be decisive in identifying non-food-producing crops. Consequently, it is relevant to only consider decisive dimensions of each crop when mining representative rules. Once static dimensions have been filtered, the dynamic dimension (NDVI) is considered in order to mine sequential patterns that characterize crops. Let us suppose that we are looking for sequences that are verified by all the crops in a given class. Under this condition, the pattern $\langle (near, n_1)(near, n_2) \rangle$ (meaning that fields located near a village and where the *NDVI* statement are n_1 at a certain date and n_2 after) characterizes the food-producing crops and the pattern $\langle (GS, n_3) \rangle$ characterizes the non-food-producing crops. It should be noted that the representative rules of each class can be composed of values of different dimensions. In the rest of this paper, we describe the method used to determine the decisive attributes of each class and how table T is subdivided and mined to obtain representative rules for each class.

4. Method

4.1. Overview

In this study, our aim was to discover and use representative rules in order to characterize crop classes. First we propose a fourstep method to discover representative rules for each class, then we combine these rules to build a classifier to distinguish between crop classes. It should be noted that the crop class depends on the user-defined interest level of the crop hierarchy shown in Fig. 3. For instance, assuming that the user would like to discover representative rules for classes in the second level of the hierarchy, the set of classes will be {*food-producing,non food-producing, other*}. The four steps to discover representative rules are illustrated in Fig. 1 and are detailed here:

- 1. *The raw database pretreatment:* During this step, two actions are performed. First, since the raw database stores crops at the lowest level of the hierarchy, these attribute values must be rewritten to match the user-defined interest level. Second, sequential pattern mining aims to discover frequent relations in a database but is not suitable for mining numerical attributes (*e.g.*, distance to village, NDVI value) due to the huge definition domain of such attributes. Consequently, numerical attributes are discretized to improve the sequential pattern mining step.
- 2. *The building of projected databases:* Since we would like to obtain representative rules for each class, the pretreated database is projected on the different class values.
- 3. *The decisive attribute computation:* During this step, a search is performed on each projected database in order to find and delete non-decisive static attributes. Intuitively, a static attribute is said to be non-decisive if none of its value allows the class to be characterized. More precisely, we guarantee that if there is no value of a static attribute in at least *minSupp*% of the projected database, the representative rules associated with this class will never contain specific values of this static attribute. Consequently, it is a waste of time to consider it in the rest of the process and this attribute is discarded from the projected database.
- 4. The sequential pattern mining: Once the projected databases have been cleaned, the algorithm M^2SP (Plantevit et al., 2005) is applied on each database. We obtain a set of frequent patterns for each class.

Once the representative rules for each class have been extracted, we combine them to build a classifier.

These steps are detailed in the following subsections.

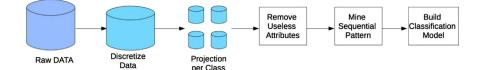


Fig. 1. Overall schema of the proposed methodology.

4.2. Database pretreatment and projections

The first treatment is rewriting the database to match the values of the crop attributes to the user-defined interest level. This is motivated by two reasons. First, mining representative rules for precise crop values are not consistent. Consequently, crop attribute values must be rewritten, at least to the level of granularity above. Second, since the hierarchy is composed of two workable levels of granularity, it is interesting to allow the user to choose which level to explore. To this end, a user-defined parameter, *Level*, is introduced to specify which level of granularity to mine. As a result, rules representing different generalized classes can be compared. Table 2 gives an example of database rewriting in which crop attribute values have already been generalized to the second level of granularity (*i.e.*, *Dom*(*Crop*) = {*FP*, *NFP*}).

The second pretreatment is the discretization of numerical attributes. This is motivated by the use of the sequential pattern technique to mine representative rules. Indeed, sequential pattern algorithms aim to discover frequent relations among the fields belonging to the same class. When dealing with numerical attributes, two values can be considered as different items even if they are very close. For instance, let us consider that the distance to the nearest village is 200 m for field 1 and 205 m for field 2. Without discretization, these two distances would have been considered as different items by the M^2SP algorithm even if they are semantically close. In our application, numerous attributes are numerical, so discretization is required. Numerous discretization techniques can be found in the literature (Catlett, 1991). Section 6 details the technique used for each numerical attribute.

Once the database has been pretreated, projection on each crop attribute value is performed. This is motivated by the fact that we would like to discover representative rules for each class. An intuitive way to achieve this goal is to subdivide the pretreated table into smaller ones associated with each class. Tables 3 and 4 show the result for our running example.

4.3. Dimensionality reduction

Once the projected databases have been built, a search is performed on the static attributes of each database to identify unnecessary static attributes. Intuitively, if the values of a static attribute change a lot, the attribute is not really characteristic of this class, and can be deleted from the projected class. The main advantage of such a strategy is to reduce the search space during the sequential pattern mining step. Indeed, it is empirically shown in Plantevit et al. (2005) that the number of dimensions exponentially influences both memory consumption and extraction time. Whereas traditional applications often deal with only a few analysis dimensions, this point can be very problematic in our context since the number of both static and dynamic dimensions can be high. For instance, the experimental results presented in Section 6 concern up to 12 dimensions. Traditional multidimensional sequential pattern approaches cannot efficiently deal with such a number of analysis dimensions. Moreover, aside from performance considerations, it is important to note that the higher the number of dimensions, the higher the number of extracted patterns. Since the extracted patterns will be exploited by experts,

Table	23		
T _{FD} , t	he FP	projected	table.

D (Date)	I (Id)	S (Soil)	D (Distance to village)	NDVI (NDVI indices)
1	F1	CL	Near	<i>n</i> ₁
1	F2	SL	Near	n_1
2	F1	CL	Near	<i>n</i> ₂
2	F2	SL	Near	<i>n</i> ₂

Table	e 4				
T _{NFP} ,	the	NFP	projected	table.	

D	I	S	D	NDVI
(Date)	(Id)	(Soil)	(Distance to village)	(NDVI indices)
1	F3	GS	Far	n ₂
1	F4	GS	Near	n ₃
2	F3	GS	Far	n ₄
2	F4	GS	Near	n ₃

reducing the dimensionality without loss of expressivity is very useful to improve the results of the analytical step.

To perform such a dimensionality reduction, we proceed as follows. Let *minSupp* be the user-defined parameter used during the sequential pattern mining step, let T_i be a projected database and $D_i \in T_i$ be one of the static dimensions in T_i . It can be easily proved that if there is no value of D_i appearing at least *minSupp* × $|T_i|$ tuples in T_i (where $|T_i|$ is the size of T_i), no sequential pattern can be extracted from T_i where a value of D_i appears. If so, the dimension D_i is considered as unnecessary and is thus deleted from *T_i*. A direct corollary of this property is that if an attribute is retained, there will be at least one sequential pattern containing a value of D_i . To illustrate this affirmation, let us consider, T_{FP} , the projected database presented in Table 3 and *minSupp*=1. The two static attributes are D and S. Regarding the D attribute, all the tuples share the same value (near). This attribute is considered as useful for the next step and is thus retained. Let us now consider the S attribute. Here, no value satisfies the minSupp condition. As a consequence, S is deleted from this table. To check the consequence of such a strategy, let us consider, SP_{FP} , the set of the multidimensional sequential patterns extracted from T_{FP} where $minSupp = 1, D_t = D, D_R = I \text{ and } D_A = \{C, S, NDVI\}$ (*i.e.*, all the static and dynamic attributes are considered). Under these conditions, $SP_{FP} = \{\langle (*, near, n_1) \rangle, \langle (*, near, n_1)(*, near, n_2) \rangle \}$. It rapidly becomes obvious that *D* occurs in SP_{FP} but not *S*.

It is interesting to observe that the set of useful attributes of each class can differ. As a consequence, independent of the values of these attributes, the attributes themselves can be representative of one class. For instance, when applying the dimensionality reduction technique to T_{NFP} described above (see Table 4), *S*, not *D*, is retained.

4.4. Mining representative rules

Once unnecessary attributes have been deleted, the M^2SP algorithm is applied on each projected and cleaned database T_i such that *minSupp* is the same as defined during the previous step,

 $D_t = D$, $D_R = I$ and D_A is composed of the static attributes and dynamic attributes retained. We denote SP_{T_i} the set of sequential patterns extracted from T_i . For instance considering T_{FP} and minSupp = 1, $\langle (near, n_1)(near, n_2) \rangle$ is a frequent sequence meaning that NDVI values equal n_1 and then n_2 is a frequent behavior for fields under food-producing crops located near a village.

4.5. The classification model

In this step we combine multidimensional sequential patterns to obtain a global classification model. We name our method MSPC (Multidimensional Sequential Pattern Classifier). The general procedure is presented in algorithm 1. The algorithm MSPC takes as input the training data *D*_{train} over which it learns the model, the test data D_{test} that represents the set of new objects to classify, the parameter k that specifies the number of rules per object to use to classify it and the support threshold supp_t used to extract the sequential patterns per class. The $supp_t$ is the same for all the classes. The MSPC (Algorithm 1) starts retrieving the set of classes C using the function *classes* over the training data D_{tr} . As a second step it projects the whole training dataset over only the sequences belonging to a class c, this operation is done by the function classProjection. Then the algorithm extracts the set of rules to use in the classification process. To do this, it calls the procedure extractRules. This procedure mines the frequent multidimensional sequential patterns per class.

In Algorithm 3 the pseudo-code of this approach is supplied. It builds the set *L* of rules used for the classification. A rule is a triple (s, w, c) where *s* is a multidimensional sequential pattern and *w* stands for the weight of the rule for the class *c*. The concept of rules is different by the concept of sequential pattern, in particular a sequential pattern could appear in more than one class while a rule is specific for each class. The weight *w* differentiates the sequential patterns and it could be seen as the strength of the specific sequential pattern *s* for the class *c*. Given a class *c* and a sequential pattern *s* we compute the weight *w* as follows:

```
w = \frac{getSupp(s, D_c)}{getSupp(s, D)}
```

The function *getSupp* returns the support (the number of sequences that support a sequential pattern) in the specified dataset. *w* has a value greater than 1 if the support in D_c (sequences in class *c*) is greater than the support in the whole dataset (sequences in the training set D_{train}). In this case we can assume that the presence of the pattern in class *c* is significant w.r.t. the whole dataset. When the weight is equal to 1, the support statistic in both the class *c* and the dataset is the same. If the value is less than 1, we can assume that the presence of the pattern in the class is less significant. In this paper we use the notation . to access each element of the rule. The *MSPC* algorithm uses the set of rules *L* to classify each test instance. To do this it employs the *classifyInstance* function (Algorithm 2).

It takes as input the instance to classify x, the set of rules L, the number of rules to use k and the set of classes C. First it extracts the order set of rules L_x from L that are supported by x (x supports the sequence s associated with the rule in L). The set is ordered in the decreasing order w.r.t. the weight w. From L_x the algorithm retains only the first k rules, we call this ordered set L_x^k . The final classification for the object x is given by the following formula:

$$\arg\max_{c \in C} \sum_{l \in L_x^{c,k}} l.w \cdot I\{l.c = = c\}$$

where *l.w* and *l.c* are respectively the weight and the class of the rule *l*, $I\{l.c = c\}$ is the indicator function and it is equal to 1 if the argument is true otherwise it returns 0. Practically, we choose, as final label, the class that maximizes the sum of the weight in the set of top-K supported rules. This process is performed for all

the objects in D_{test} and the final classification is returned by the algorithm. The classification is used to compute any evaluation measure to test the performance of the classifier.

Algorithm 1. MSPC(D_{train} , D_{test} , k, $supp_t$).

1: (C = classes	(D_{train})
------	-------------	---------------

- 2: $L = extractRules(D_{train}, supp_t, C)$
- 3: predictedValue $= \emptyset$
- 4: **for all** $x \in D_{test}$ **do**
- 5: predictedValue[x] = classifyInstance(x, L, k, C)
- 6: end for
- 7: **return** predictedValue

Algorithm 2. classifyInstance(x, L, k, C).

- 1: findClass=Ø
- 2: $L_x = \{l | l \in L \land x \text{ supports } l.s\}$
- 3: $L_x^k = \text{extractTopK}(L_x, k)$
- 4: findClass = arg max_{c \in C} $\sum_{l \in L_{v}^{c,k}} l.w \cdot l\{l.c = -c\}$
- 5: **return** findClass

Algorithm 3. extractRules(*D*, *supp*_t, *C*).

1:	L=Ø
2:	for all $c \in C$ do
3:	$D_c = \text{classProjection}(D, c)$
4:	$S = extractFreqPattern(D_c, supp_t)$
5:	for all $s \in S$ do
6:	$W = \frac{getSupp(s,D_c)}{getSupp(s,D)}$
7:	$\mathbf{L} = L \cup (s, w, c)$
8:	end for
9:	end for
10:	return L

4.6. Complexity analysis

We now provide an analysis of the time complexity of the proposed methodology. It is noteworthy that the first two steps, *i.e.* data pretreatment, projections and dimensionality reduction, can be merged and achieved in linear time on the size of the table T. Indeed, one scan of T is necessary to dispatch each tuple in its appropriated projected table, discretize numerical values and count each value. Once this scan has been performed, one has to discard static dimensions in which no item is frequent. The multidimensional sequential pattern mining is the most time consuming step of our framework. From a theoretical point of view, enumerating frequent sequences is NP-hard (Yang, 2006). However, M2SP performs well on relatively large databases in practice. Indeed, experiment results reported in Plantevit et al. (2005) show that mining multidimensional sequential patterns can be achieved in reasonable time, e.g., it takes around 20 min to mine patterns in a database of 25 K tuples considering 15 dimensions and *minSupp*=0.5. Finally, the time to perform the classification step is logarithmic on the number of extracted rules, denoted by *n*. Here again, this number is theoretically exponential on the number of dimensions and the definition domain size of each dimension. However, it is well-known that minSupp constraint can drastically help in reducing the number of mined patterns, *i.e.*, the higher the *minSupp*, the lower the number of patterns. Since we aim at considering only the k most important rules according to their weight, the *n* rules can be sorted in logarithmic time. Extracting the *k* first rules and finding the predicted class are then straightforward.

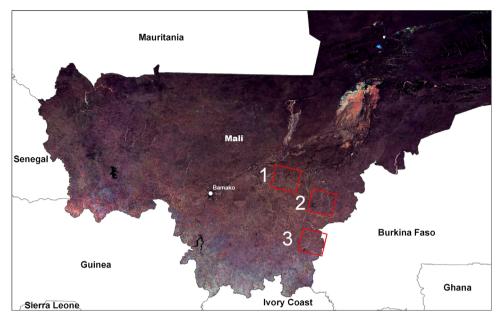


Fig. 2. The three study sites in Mali (a color composite MODIS image) – 1: Cinzana, 2: Koutiala; 3: Sikasso. (For interpretation of the references to color in this figure caption, the reader is referred to the web version of this article.)

Main characteristics of the three study sites.

Eco-climatic zone name	Mean annual rainfall (mm)	Main crops	Natural vegetation type
Cinzana (Sudano-Sahelian)	600	Millet, sorghum	High proportion of bare soils and sparse vegetation
Koutiala (Sudano-Sahelian)	750	Cotton, millet, sorghum	Large areas of semi-open and closed natural vegetation
Sikasso (Sudanian)	1000	Maize, cotton, fruit crops	Dense natural vegetation

5. Data description

In this project, we used data acquired over 3 sites in southern Mali (Fig. 2). Mali is representative of the Sahel Belt, a region where mapping cultivated areas is still a challenge. First, Sahel is a transition zone between the hyper-arid Sahara in the north and the more humid savannas and woodlands in the south, with specific weather conditions resulting in high regional variability in terms of rainfed agricultural systems (and calendars); second, West African land-scapes are complex, with small-scale farming, numerous trees in the fields, and synchronized phenology for crops and natural vegetation due to the rainfall regime (Vintrou et al., 2012).

5.1. Field data

Field surveys were conducted in Mali during the 2009 and 2010 cropping seasons (from May to November) in order to characterize Sudano-Sahelian rural landscapes. Three sites (Cinzana, Koutiala, Sikasso) were selected to sample the main agro-climatic regions of central and southern Mali (Table 5). A total of 744 GPS waypoints were registered and farmers were interviewed. Each waypoint was transformed into a polygon and a land use was attributed to the center of each polygon.

5.2. External data

Seven static descriptors were also used to characterize the survey points:

• soil type,

- name of the eco-region,
- distance to the nearest village,
- distance to the nearest river,
- rainfall,
- ethnic group,
- name of the village,

5.3. Image data

MODIS (or Moderate Resolution Imaging Spectroradiometer) (Justice et al., 1998) is a key instrument aboard the TERRA and AQUA satellites. The NASA Land Process Distributed Active Archive Center (LP DAAC) is the repository for all MODIS data. Among the MODIS products, we selected the "Vegetation Indices 16-Day L3 Global 250 m SIN Grid" temporal syntheses (MOD13Q1). In fact, the quality of MODIS images is affected by atmospheric contamination (clouds and aerosols). MODIS images are therefore composited over 8 or 16 days using cloud-screening algorithms and these temporal syntheses were especially useful in our study because of the high probability of cloud cover during the monsoon season in West Africa.

In our study, a set of 12 MODIS 16-day composite normalized difference vegetation index (NDVI) images (MOD13Q1/V005 product) at a resolution of 231.6 m were acquired in 2007 (we selected the best quality composite image out of the two acquire each month) from the NASA LP DAAC. The year 2007 was chosen to overlap with more recent higher resolution data. We assume that the observed classes of land use (Fig. 3) remained globally unchanged from 2007 to 2009 (the field surveys were conducted in 2009).

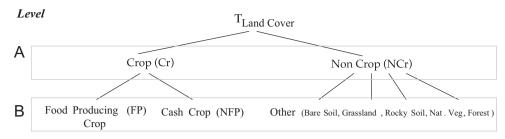


Fig. 3. Crop hierarchy: the hierarchical organization of the classes to predict. Level A contains only two classes: Crop, Non-Crop while level B refines the previous set of classes adding a specialization (food producing crop, cash crop) of the Crop class. The class labels for the data are manually collected by the experts involved in the project during field missions in MALI region.

We underline that the proposed data mining framework is not specific to MODIS images but it can be straightforwardly applied on high resolution time series. In our scenario, due to project constraints, the only available images are MODIS ones. From a practical point, considering only low resolution images is not limitation because (i) low resolution images are cheaper or freely available, (ii) they allow us to consider longer and denser time series as they are produced with higher frequency, (iii) if the results on low resolution images are satisfactory, probably with high resolution images the performance will improve. These considerations summarize the pragmatic implications to considering as source of information MODIS time series

5.4. Remotely sensed indices used

Information content in a digital image is expressed by the intensity of each pixel (*i.e.*, reflectance or spectral index) and by the spatial arrangement of pixels (texture) in the image.

• The Normalized Difference Vegetation Index, or NDVI, is one of the most successful indices to simply and rapidly identify vegetated areas (Rouse, 1974) and their "condition", providing a crude estimate of vegetation health. Based on the spectral contrast that exists between soil and green vegetation in the RED and NIR spectral bands (intensity), commun bands used in the Earth Observation Systems, NDVI is used as a proxy of plant biomass and fractional vegetation cover:

$$NDVI = \frac{NIR - RED}{NIR + RED}$$

where RED and NIR stand for the spectral reflectance measurements acquired in the red and near-infrared regions, respectively. In general, NDVI values range from -1.0 to 1.0, with negative values indicating clouds and water, positive values near zero indicating bare soil, and higher positive values of NDVI ranging from sparse vegetation (0.1-0.5) to dense green vegetation (0.6 and above). Furthermore, different land covers exhibit distinctive seasonal patterns of variation in NDVI. Crops generally have a distinct growing season and period of peak greenness, which allows them to be distinguished from other types of land cover.

Texture analysis is also an important contributor to scene information extraction. The majority of image classification procedures, particularly those in operational use, rely on spectral intensity characteristics alone and thus ignore the spatial information contained in the image. Textural algorithms, however, attempt to measure image texture by quantifying the distinctive spatial and spectral relationships between neighboring pixels. Numerous texture algorithms have been developed in response to the need to extract information based on the spatial arrangement of data in digital images. Statistical approaches, such as those developed by Haralick et al. (1973),

make use of gray-level probability density functions, which are generally computed as the conditional joint probability of pairs of pixel gray levels in a local area of the image. In this study, we used four Haralick textural indices (Haralick, 1979) calculated on the MODIS time-series: variance, homogeneity, contrast and dissimilarity. The Haralick textural features describe the spatial distribution of gray values and the frequency of one gray tone appearing with another gray tone in a specified distance and at a specified angle. The generation of these indices is based on different orientations of pairs of pixels, with a specific angle (horizontal, diagonal, vertical, co-diagonal) and distance, called patterns. We determined empirically a pattern size of 15 pixels for MODIS, which is the smallest patch repeated in different directions and at different distances.

6. Experiment study

In this section, we describe the experiments performed to evaluate the feasibility and efficiency of our approach. Throughout the experiments, we answer the following questions that are inherent to efficiency issues: Does the dimensionality reduction technique allow unnecessary static attributes to be deleted without losing information? Does the mining process allow discriminating patterns to be discovered in each class ? Does the texture data allow better extraction of discriminating patterns than only considering NDVI values? Does the extracted pattern enable a good classifier to be built? Is the classification process affected by the support threshold? Which dimensions allow the best classification? The experiments were performed on a Intel(R) Xeon(R) CPU E5450 @ 3.00 GHz with 2 GB of main memory, running Ubuntu 9.04. The methods were written in Java 1.6. We first describe the protocol and then present and discuss our results. In order to evaluate the performance of our method we use the F-Measure. Finally, we discuss about the genericity of the proposed framework.

6.1. Protocol

The method was evaluated on the dataset described in Section 5. This dataset contains 744 distinct fields, and a MODIS time-series of length 12 was associated with each field. The seven static dimensions and the five dynamic dimensions (NDVI, variance, homogeneity, contrast and dissimilarity) were the same as described in Section 5. As mentioned in Section 4, a discretization step is necessary to efficiently mine frequent patterns. The following discretization methods were used:

- Equi-Width technique (the generated intervals have the same width) was used for distance to village, and for distance to river attributes.
- Equi-Depth technique (the generated intervals are the same size) was used for the other numerical attributes.

The motivation behind these choices are the following. First, these two techniques are very well known and extensively used in data mining approaches where numerical attributes need to be converted into categorical attributes, *i.e.*, intervals. Then, we experimentally verified that this setting offers the best experimental results. Interested readers could refer to a recent survey on discretization techniques in Kotsiantis and Kanellopoulos (2006).

Two sets of classes were used in this experiment. The first set of classes, denoted as *B*, aims to discover patterns enabling the distinction between food-producing crops (FP), non-food-producing crops (NFP) and non-crops (OTHER). The second set of classes, denoted as *A*, aims to discover patterns enabling the distinction of more general classes, *i.e.*, crops (*Cr*) and non-crops (*NCr*).

To evaluate the impact of texture data on the extraction of discriminating patterns, we consider a first configuration, denoted as *Default*, in which all the dynamic attributes were used. Conversely, the configuration denoted as *NDVI* was only composed of NDVI values as dynamic attributes.

Three experimental results are presented and discussed in this section:

- 1. The first experiment was performed to evaluate the number of retained static attributes according to two *minSupp* values offering representative results.
- 2. The second experiment was performed to evaluate the number of discriminating patterns. Here, *discriminating* means that a pattern appears in one class but not in the others.
- 3. The third experiment was performed to observe the discriminating dimension values according to the two configurations described above.

6.2. Results and discussion on patterns

Table 6 shows the retained attributes according to the two sets of classes and two *minSupp* values. First, it can be seen that the *minSupp* threshold value had obvious clear impact on this attribute selection. Indeed, when minSupp=0.5, more than half of the attributes were deleted. It is also interesting to note that the retained attributes per class and set of classes were roughly the same.

Table 7 shows the proportion of discriminating patterns per class with minSupp = 0.5 and the NDVI configuration. Indeed, even if a pattern was extracted from one class, this is not enough to consider it as discriminating (*i.e.*, since the same pattern can

Table 6

Retained static attributes under default configuration (up: minSupp=0.5/down: minSupp=0.3).

Level Class		Static attributes						
	Distance to village	Site name	Ethnic group	Rainfall	Soil type	Distance to river	Village	
В	FP	×		×	×			
	NFP	×		×				
	OTHER	×		×				
А	Cr	×		×				
	NCr	×		×				
Level	Class	Static attributes						
		Distance to village	Site name	Ethnic group	Rainfall	Soil type	Distance to river	Village
В	FP	×	×	×	×	×		
	NFP	×	×	×	×	×		
	OTHER	×	×	×	×	×		
А	Cr	×	×	×	×	×		
	NCr	×	×	×	×	×		

appear in different classes). Thus, queries were formulated to search for patterns that appear in one class and not in any others. Two conclusions can be drawn from this figure. First, considering the set of classes *B*, most of the extracted patterns are discriminating (even if the *FP* class obtained the worst score). Second, finding discriminating patterns on the set of class *A* is apparently more difficult.

Table 7

Proportion of discriminating patterns per class with minSupp = 0.5 and the NDVI configuration.

Level	Class	#disc. patterns	#patterns	Proportion (%)
В	FP	6	9	66.67
	NFP	12	12	100
	OTHER	13	16	81.25
А	Cr	3	10	30
	NCr	4	11	36.36

Table 8

Some discriminating dimension values per class with minSupp = 0.3 (top: default config./bottom: NDVI config.).

Level	Class	Attribute	Value
В	FP	Modis homogeneity 1 km Modis variance 1 km	0.48-0.52 3.27-4.34
	NFP OTHER	Modis dissimilarity 1 km Distance village Modis contrast 1 km Modis dissimilarity 1 km NONF	1.36–1.51 3150–6205 5.35–6.54 1.51–1.66
	UTHER	INUINE	
А	Cr	Modis dissimilarity 1 km Modis variance 1 km	1.21–1.36 3.27–4.34
	NCr	Modis variance 1 km	3.27-4.34 10.28-14.15
Level	Class	Attribute	Value
В	FP NFP	NONE Rainfall	800
	OTHER	Distance village NONE	3149.3-6205.6
А	Cr NCr	NONE Distance village 3149.3–6205	

Table 8 shows some representative values of discriminating attributes according to the two configurations and the two sets of classes. An attribute value is said to be discriminating if it does not appear in a pattern in any other classes. The aim of this experiment is to observe the impact of texture dynamic values on the extracted patterns. Some conclusions can be drawn. First of all, class *OTHER* does not contain any discriminating values independent of the configuration. Second, a very interesting and promising result is that the default configuration contains many more discriminating values than the NDVI configuration. Moreover, these discriminating values concern the texture attributes. This result reinforces our hypothesis that texture attributes are very useful in automatic landscape recognition.

To conclude the first part of our experiment, we empirically showed that (1) the dimensionality reduction method allows the search space to be reduced by deleting unnecessary attributes; (2) most of the extracted patterns are discriminating; (3) it appears to be more difficult to distinguish between *Cr* and *NCr* classes than *FP*, *NFP* and *OTHER* classes with our approach and (4) most of the discriminating attribute values concern the texture attributes. In the second part of the experiment we used the previously extracted patterns to build the *MSPC* classifier. We saw that the patterns are able to discriminate between the classes of the problem. For this reason we hypothesize that combining them will enable us to obtain very interesting results from the classification point of view, especially with respect to the problem of distinguishing between *Cr* and *NCr* classes.

6.3. Results and discussion on classification

In this section we evaluate the capacity of *MSPC* to discriminate between *Cr* and *NCr* classes, but in fact, it could be applied at any level of the hierarchy in Fig. 3. We evaluated the classification results using *Precision* and *Recall* for the *Cr* label. Finally, we combined these two measures using the *F-Measure*. The *Precision* is defined as the number of areas correctly assigned to the class (*Cr* divided by the total number of areas assigned to this class (correctly or not). The *Recall* is the number of areas with true label equals *Cr*. Finally the *F-Measure* is defined as

$$F-Measure = 2 \times \frac{Precision \times Recall}{Precision + Recall}$$

Since sequential pattern mining uses discrete data, we used the Equi-Width discretization method to discretize the time-series values. For our approach we varied the support threshold from 0.3 to 0.6 and the values of k ranges over the set $\{5,10,15\}$. The choice of minimum support threshold values and step size is motivated by the following arguments. First, it is crucial to extract at least one frequent pattern per class. Otherwise, it would lead to the construction of a classifier containing unrepresented class. Thus, we experimentally verified that with a support threshold above 0.6, some classes were not represented. Conversely, setting up the minimum support threshold to a very low value does not really make sense in our approach since we only consider the *k* extracted patterns having the highest score. Second, we experimentally verified that this step size allows us to show the most representative results. The choice of k values and step size is motivated by the following arguments. First, considering a very low value for k contradicts the vote-based classification system philosophy. Conversely, setting up the k value to a high value will introduce the selection of noisy patterns, *i.e.*, patterns with low supports, in the process and will decrease the performances. Second, similar to the minimum support step size motivation, we experimentally verified that this step size allows us to show the most representative results. We also adopted a 10 Fold Cross Validation strategy to test the generalization ability of our approach.

In our comparison, we used the MOD12Q1 V005 as base-line competitor. This product, based on an ensemble classification approach, is widely used in the remote sensing field. The base algorithm is a decision tree (Quinlan, 1996) and ensemble classifications are estimated using boosting (Freund et al., 1998). The results of this approach are listed in Table 9. Table 10 shows the classification of the Mali dataset using our method. It can be seen that higher F-Measure values were obtained with an increase in the support threshold. This probably happened because, with a low support threshold we also obtain noisy patterns that could influence the whole process. In particular, these noisy patterns could be anomalous patterns that represent particular behavior associated with a particular geographical area, but not are related to the problem of discriminating between Crop and Non-Crop areas. Compared with the baseline method presented in Table 9, our results were good. In fact with a support equal to 0.5 or 0.6, the classifier gave very good results (a F-Measure greater than 0.70) compared with the baseline approach.

6.3.1. Evaluation of different projections over dynamic dimensions

In this subsection, our aim is to identify the most important source of information to distinguish Crop and Non-Crop areas. When we consider dynamic information we have two different groups of information, the first is supplied by the NDVI, and the second is supplied by the four texture indices. For our analysis, from the original dataset, we obtain two different projections that we denote as D_{NDVI} and $D_{TEXTURE}$. D_{NDVI} is the projection of the original dataset over the static dimensions plus the NDVI timeseries while the *D*_{TEXTURE} is the projection of the original dataset over the static dimensions plus the four texture time-series. Table 11 shows the F-Measure resulting from the classification process using the different projections over dynamic dimensions. In this comparison, the best results were obtained with the full set of information (0.72 with support equal 0.6 and k equal 5). From this analysis, we can conclude that the most useful information to discriminate between the classes of the problem is supplied by the texture dimensions. This information always produced interesting results and was not affected by changing support values. The worst results were obtained when the classifier used only the NDVI information. From this analysis we can conclude that the texture information plays a very important role in discriminating between

Table 9

Classification results using the MOD12Q1 V005 base-line product.

Precision	Recall	F-measure
0.63945	0.6578	0.6485

Table	10	

Classification results using all dynamic time-series information.

Support	k	Precision	Recall	F-measure
0.3	5	0.6453	0.4843	0.5533
0.3	10	0.6202	0.4288	0.5070
0.3	15	0.6321	0.4518	0.5270
0.4	5	0.6046	0.5485	0.5751
0.4	10	0.5969	0.5469	0.5708
0.4	15	0.6388	0.4012	0.4928
0.5	5	0.6008	0.8059	0.6884
0.5	10	0.6092	0.7672	0.6792
0.5	15	0.6178	0.7300	0.6693
0.6	5	0.6004	0.9155	0.7252
0.6	10	0.6002	0.8676	0.7095
0.6	15	0.6007	0.8871	0.7163

 Table 11
 Classification (F-measure) results using different projections over dynamic dimensions.

Support	k	D _{TEXTURE}	D _{NDVI}	D _{DEFAULT}
0.3	5	0.6930	0.3337	0.5533
0.3	10	0.6699	0.3095	0.5070
0.3	15	0.6685	0.3147	0.5270
0.4	5	0.6750	0.4687	0.5751
0.4	10	0.6847	0.5714	0.5708
0.4	15	0.6565	0.6097	0.4928
0.5	5	0.6635	0.6206	0.6884
0.5	10	0.5689	0.6531	0.6796
0.5	15	0.3059	0.6275	0.6693
0.6	5	0.7211	0.6440	0.7252
0.6	10	0.7152	0.6490	0.7095
0.6	15	0.7103	0.6466	0.7163

Table 12

Classification (F-measure) results using different projections over dynamic dimensions.

Support	k	Equi-Depth	Equi-textureWidth
0.3	5	0.5459	0.5533
0.3	10	0.6005	0.5070
0.3	15	0.6609	0.5270
0.4	5	0.6663	0.5751
0.4	10	0.6257	0.5708
0.4	15	0.6262	0.4928
0.5	5	0.4242	0.6884
0.5	10	0.4623	0.680
0.5	15	0.4456	0.6693
0.6	5	0.1252	0.7252
0.6	10	0.2435	0.7095
0.6	15	0.2347	0.7163

Crop and Non-Crop areas, while the NDVI dimension mostly affects the quality and the stability of the results.

6.3.2. Impact of different discretization over dynamic dimension

In this section we evaluate to what extent the discretization technique used to manage the dimensions of the time-series affects the final results. Table 12 shows part of the results of the experiment.

We observed that the classifier learned with the Equi-Depth discretization was very sensitive to changes in the support threshold. In fact, for low support threshold it gave good quality results, but its performance decreased with an increase in the support threshold. Examining the data in more detail, we observed that the classification using Equi-Depth discretization always obtained good results with respect to the Precision measure but the Recall drastically decreased and as a result, the *F*-Measure also decreased. This means that the Equi-Depth discretization influences the whole process by increasing the number of false negatives. This increase in the number of false negatives means that the rules will assign nCr label to Cr areas. In the same context we observed that while the performance of the classification decreased with the full set of dimensions, if we used the Equi-Depth discretization combined only with the texture information the results we obtained were of good quality and were very similar to those obtained using Equi-Width discretization. This means that Equi-Depth discretization mainly affects the discriminating ability of the NDVI dimension and consequently reduces overall performance.

6.3.3. Low support patterns

We have seen that support influences the performance of the classification step. The aim of this set of experiments was to evaluate the classification performance using a lower support threshold. Usually using a low threshold avoid noisy patterns that are shared between all the classes. Instead, in our study we obtained worst results by decreasing the threshold. When the support value we used was too low we observed that the algorithm used infrequent patterns that could resemble local anomalies or patterns that describe only a particular geographical zone but are not able to describe the overall difference between *Cr* and *nCr* areas. Another interesting observation, from the point of view of our analysis, is that when we used a low support threshold, the classifier learned using only the NDVI projection gave similar or slightly better results to the classifier learned using the full set of dynamic dimensions.

6.3.4. Example of rules

Table 13 lists some examples of rules that we extracted from *MSPC*. To make the analysis easier we only show the dimensions used and avoid showing the dimensions with no specific value with the * operator. For the same reason, we multiply the value of NDVI by 10⁴ because this helps interpret the bins obtained by the discretization step.

It can be seen that, using our approach, we were able to take both static and dynamic dimensions into account as shown in rules 1 and 2.

In rule 1, the algorithm uses the combination of a static information (*distance_village*) with a change in the value of NDVI to predict *Cr* areas. In this rule, the weight or the score was greater than 1.

In rule 2, a pattern, composed of three multidimensional items, appeared that gave a high score for the *NCr*. In this rule, static information is always combined with dynamic information. In this particular case, we observed that the NDVI was stable in the first and the second multidimensional item, whereas it increased in the third position of this sequence. This phenomenon is closely correlated with the *ethnic group* and is a good indicator to predict *NCr* areas.

In rules 3 and 4, the same rule is used to predict both classes but with a different score. In these rules, the two multidimensional items involved in the sequence are always the same. This is still an useful information because it underlines the fact that constant behaviors are also useful to discriminate the two classes.

We also supply the entire set of rules (per class) to remote sensing experts in order to have a qualitative interpretation of them. After some manual inspection, the experts highlighted that the rules employed in the classification model are coherent with the temporal profile of each class. The interpretability of the rule set, supplied by our model, is a bonus of our proposal.

6.4. Genericity of MSPC

In this section, we discuss about the genericity of the framework that has been proposed in this paper. Multidimensional and heterogeneous data are rarely considered as input of classification techniques. Indeed, most of the pattern-based classification techniques focus on the sequential behavior and omit to take contextual and external knowledge into account. Though, recently, a new trend in the data mining field tries to incorporate expert knowledge in the process to improve the result quality (Cao, 2010; Rauch and Simunek, 2011; Tatti and Mampaey, 2010). Our approach clearly comes within this scope and we experimentally show that adding as much as available non-sequential information would lead to increase the classification performances. Moreover,

Table 13 Example of rules.

Number	Sequential pattern	Weight	Class	
1	< (distance_village = -inf-3149.3,modis_ndvi = 2182.6-2927.0) (distance_village = -inf-3149.3,modis_ndvi = 2927.0-3671.5) >	1.074524	Cr	
2	<pre>< (modis_ndvi=2182.6-2927.0,ethnic_group=senoufo_nanerige) (modis_ndvi=2182.6-2927.0,ethnic_group=senoufo_nanerige)</pre>	1.0115681	NCr	
3	(modis_ndvi=2927.0-3671.5,ethnic_group=senoufo_nanerige) > <(modis_variance=-inf-7.585,modis_contrast=-inf-6.245) (modis_variance=-inf-7.585,modis_contrast=-inf-6.245) >	1.03212	Cr	

thanks to the dimensionality reduction mechanism, we guarantee that no matter the number of additional dimensions we consider, the framework will select the most appropriated ones in order to preserve the scalability.

7. Related work

In the literature several sequential pattern mining approaches are proposed to deal with spatio-temporal data. In Cao et al. (2005) a method to mine frequent sequential patterns from spatiotemporal data is presented. Given a set of objects that move together, this strategy extracts frequent routes followed by the objects. The mined pattern is constrained to be consecutive w.r.t. the temporal dimension.

A more recent approach that extracts sequential patterns from spatio-temporal events is introduced in Huang et al. (2008). The authors proposed to use an indexing structure in order to mine the sequential behavior of events in the data. The final patterns are sequences of events that occur in the same neighborhood area. This kind of approach is useful if the objects to follow slightly change their position while they are equivalent to standard sequential patterns when the followed objects do not move.

In Julea et al. (2006, 2008, 2011) and Petitjean et al. (2010) sequential pattern mining methods are employed to extract useful knowledge from Time Series of Satellite Images (TSSI). The interest in these methods used to detect change using satellite images is due to the fact that they are (i) multi-temporal, (ii) robust to noise, (iii) able to handle large volumes of data, and (iv) capable of capturing local changes without the need for prior clustering.

Sequential pattern mining is used to analyze changes in land cover over a 10-month period in a rural area in eastern Romania in Julea et al. (2008). Pattern extraction is used to group SPOT pixels that share the same spectral change over time. The TSSI data is thus processed at the pixel level, by taking the values of the pixels on each of the SPOT bands. A method is proposed to visualize the extracted patterns on a single image.

A similar approach is proposed in Petitjean et al. (2010) but the pixel values are computed from four SPOT bands instead of only one band. The TSSI period covered is also much longer: a 20-year time image series is mined to study urban growth in South West France. A visualization technique is proposed to locate areas undergoing change. Results show that mining all pixels of the images leads to the generation of a huge number of no change patterns. Additional strategies are then required to filter out all non-informative patterns.

To tackle this type of problem, the classification part of our approach was inspired by the LeGo framework (Fürnkranz and Knobbe, 2010) in which a global model is built starting from local pattern. An evaluation of different kinds of discriminating sequential patterns is presented in Deng and Zaïane (2010). In this work the authors propose an occurrence based approach to filter out the non-discriminating sequences. This work deals only with mono-

dimensional sequential patterns that are used as a feature for standard classification algorithms.

A method to classify multivariate time-series is introduced in Weng and Shen (2008). The method is based on a set of metafeatures that are used to represent the data. The meta-feature is recurrent substructure contained in the data and they need to be defined by the user because they are dependent on the specific application domain. In this way each time-series is represented as a bag of meta-features. The meta-features are used to partition the space. Using this representation any classification algorithm that works over the attribute-value format could be applied. The main disadvantage of this approach is that each meta-feature needs to be defined by the expert and in their examples they consider only dynamic information. In particular they do not provide any example in which they manage both static and dynamic information. The effort is focused to construct meta-features for temporal domain. Generally, meta-features that take into account both information could be designed but (a) they will be very time expensive and complex to obtain, (b) our approach supplies automatically this kind of meta-features as multidimensional sequential pattern.

A new method for the classification of multi-variate time-series is proposed in Batal et al. (2009). The approach is based on abstraction patterns. The abstraction patterns are relations introduced by the user to describe the data. In this way, a time-series is defined as a sequence of related states using these temporal relationships. The relationships are specified between the different dimensions of a multivariate time-series. Each time-series is represented in this format and an itemset mining algorithm (A priori) is used to extract frequent patterns. Then the patterns are filtered using a Chi-Square test. The final set of patterns are used as boolean features to represent the original dataset and standard classification algorithms (like SVM and Naive Bayes) are employed to perform classification. Also in this work the problem is the specification of relationships among the data. The method is developed to use only the dynamic information while in our scenario we need to analyze static information to exploit the whole set of information.

A different point of view is presented in Kadous and Sammut (2005). In this work the authors present a method based on two dimensional singular value decomposition. Always in this case the decomposition method is used to extract a new representation of the data in a different feature space. First each multivariate timeseries is represented in the new feature space then a K-nearest neighbors approach (with K=1) is employed to perform the classification. This method avoids the definition of any type of background relationships among the data while it is able to take into consideration only the dynamic aspect of the data. In particular the integration of some static information in the framework is more harder than the approaches based on the definition of background relationships or meta-features and no proposition to do this is supplied.

Concerning Satellite Image classification, some works proposed to use decision trees model in order to perform land cover prediction (Friedl and Brodley, 1997). A recent approach in this direction (Jiang et al., 2013) introduces a new technique to create spatial decision trees. This kind of model can be efficiently used in land cover classification for remote sensing images. The novelty in the proposed method lies in the use of focal test (at node level) in order to capture spatial autocorrelation. Focal tests allow us to model neighborhood pixel relations while previous works only focus on local data characteristics without considering autocorrelation. All these kinds of approaches are well suited to analyze only one image while they cannot be applied to TSSI data where the temporal dimension plays a fundamental role in the whole analysis.

To the best of our knowledge, sequential pattern mining of remote sensing images has only been applied at the pixel level using high resolution images without taking into account external data or texture information in the mining process. In this paper, we have shown that sequential pattern mining can help us characterize cultivated areas in moderate resolution MODIS remote sensing images combining both dynamic and static data.

8. Conclusion

The objective of this study was to propose an original method to extract sets of relevant sequential patterns from heterogeneous data in order to build an accurate classifier. We developed a data mining method that first extracted multidimensional sequential patterns and then used the extracted information to build a classifier to label the data. This approach has been applied on MODIS time-series combined with field data coming from the Mali dataset to perform the classification of cultivated land. The experiment conducted on this dataset reinforced our intuition about the importance of texture attributes to improve automatic landscape recognition.

In the proposed work we perform some close world assumptions, first of all the observed classes of land use remained globally unchanged from 2007 to 2009. As future work we want to consider the situation in which changes in land use happen during the time series. This scenario adds more complexity to the classification task and it needs to be addressed with new techniques or smart extension of the proposed one.

Other possible research directions to extend our method can manage imbalanced classes as proposed in García et al. (2012) or combine spatial classifiers (such as spatial decision trees Jiang et al., 2013) with multidimensional sequential patterns in order to obtain a spatio-temporal classification model for Time Series of Satellite Images.

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