

A Formal Approach to Designing Autonomous Systems:

from Intelligent Transport Systems to Autonomous Robots

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Motivation

Specifics critical complex systems

- intrinsically **highly distributed** systems
- ensure correct **behaviour**
- **real-time** properties: durations, timeouts, ...
- **real-space** aspects: safety distances, ...

Use of formal methods

- **describe** the problem
- **verify** that expected properties are satisfied
- **simulation** not sufficient
- formal methods are **mathematically sound**
- provide **automated tools**

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Outline

- 1 Running example: Intelligent Transport Systems
 - ITS example: safe insertion in a motorway
 - Modelling issues
- 2 Specification
 - Specification issues
 - Symmetric Nets
- 3 Modelling methodology
 - Structure and abstraction level
 - Dynamic actors
 - Plus time and space
- 4 ITS analysis
- 5 From ITS to autonomous robots

Intelligent Transport Systems

Characteristics

- highly critical: failures may lead to fatal accidents
- involve a significant number of partners
- cooperation between partners must be both efficient and secure

Partners involved

- road operators
- infrastructure
- vehicles with or without embedded equipment
- drivers

Intelligent Transport Systems

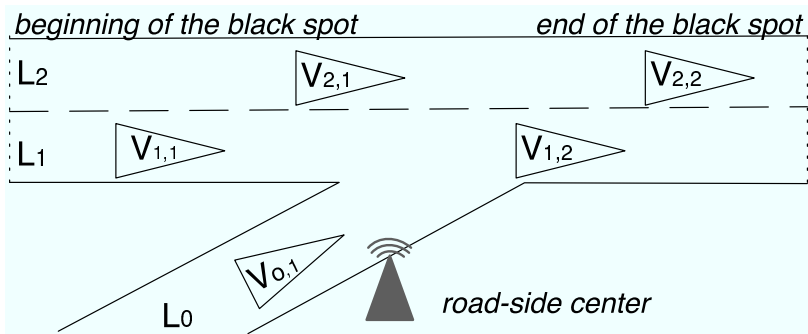
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ITS example: safe insertion in a motorway



Black-spot functioning

Requirements

- minimum distance between vehicles within a same lane
- vehicles in the entrance lane must eventually enter the motorway
- vehicles should not stop

A cyclic functioning

- 1 vehicles get their position
- 2 they send their position to the infrastructure
- 3 when the infrastructure has received all positions, it issues commands according to a predefined strategy

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Modelling issues

Requirements

- managing **dynamic actors**
- modelling **physical aspects**
- preserving a **fair progression** of the system: actors perform actions at a similar pace.

Development steps

- 1 first formal specification
- 2 qualitative analysis: is the global behaviour correct?
- 3 refinement including time or space features
- 4 quantitative analysis: do the envisioned strategies satisfy the physical constraints?

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Specification issues

UML

- + industrial standard
- + structured models
- semantics not formal enough
- analysis by simulation

Algebraic methods

- + formally defined
- tools require experienced users

Model-checking

- + structured models
- + large automated tools support
- + exhaustive and efficient analysis techniques
- cope with models complexity

Choosing the formalism

Requirements

- capture **relevant aspects** of the problem
- **simple** enough
- allow for **efficient verification** techniques
- **tool** support

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⇒ **Symmetric Nets**

Symmetric nets basic features

SN characteristics

- **high-level** features
- **simple data and functions**: enumerated types, intervals, tuples ; predecessor, successor, selector and *broadcast*

Class

P is 1..PR;

Val is 1..V;

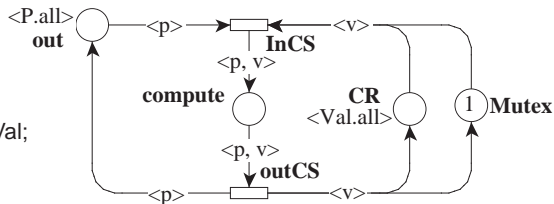
Domain

D is <P,Val>;

Var

p in P;

v, v2 in Val;

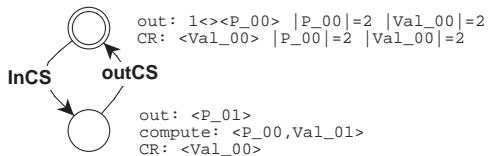


Dedicated analysis techniques

Symbolic reachability graph

- **nodes** represent a set of states with a similar structure
- based on **symmetries** computation

⇒ well-suited for ITS which enjoy intrinsic symmetries (e.g. same algorithm in all cars)

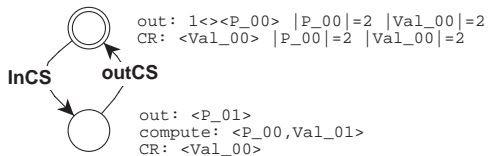


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Components and abstraction level

Why is structure necessary?

- **interaction** between components
- **communication mechanisms**: **asynchronous** (place fusion) or **synchronous** (transition fusion)

Advantages

- **reusability**: try out several models for a single component
- use of modular analysis techniques

Abstraction

- apply a **refinement** process
- add details step by step until the desired **abstraction level** is reached
- start with general behaviour and add the real-time and real-space aspects at a later stage

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Dynamic actors

How to handle dynamicity?

create new vehicles getting in and discard those getting out

not suitable

- numbers associated with vehicles \Rightarrow state space explosion (even if there is a maximal id)
- identities are not important as long as the vehicles can be distinguished

maximal number of vehicles in the system (due to physical reasons)

\Rightarrow reuse identity of exiting vehicles

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Adding real-time and real-space aspects

Complex functions

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- 2 use **timed** or **hybrid** formalisms

Fair execution of components

- use of a **timeline** as in timed Petri nets
- state space construction with **branching criteria** discarding unsuitable sequences

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More advanced analysis techniques

Analysis techniques **inadequate** for systems where types have many values (due to discretisation)

⇒ more elaborate techniques:

- **symbolic/symbolic** approaches combine:
 - symbolic reachability graphs
 - symbolic encoding of states
 - sharing features
 - hierarchical structuring
- **distributed model-checkers** running on clusters of machines

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Similarities between ITS and autonomous robots

- robots evolve in an **environment** which may have **unexpected behaviour**
- information obtained from sensors gives an **abstract vision** of the environment
- **real-time** and **real-space** features

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- robots ↔ vehicles
- interacting agents ↔ infrastructure

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