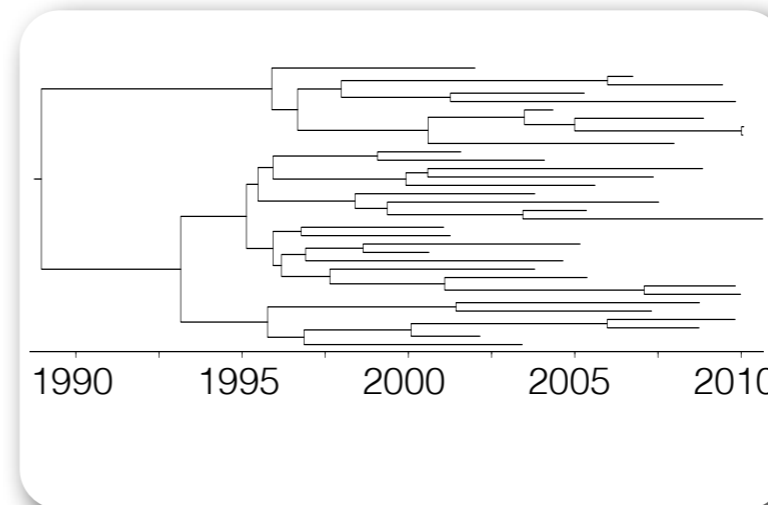
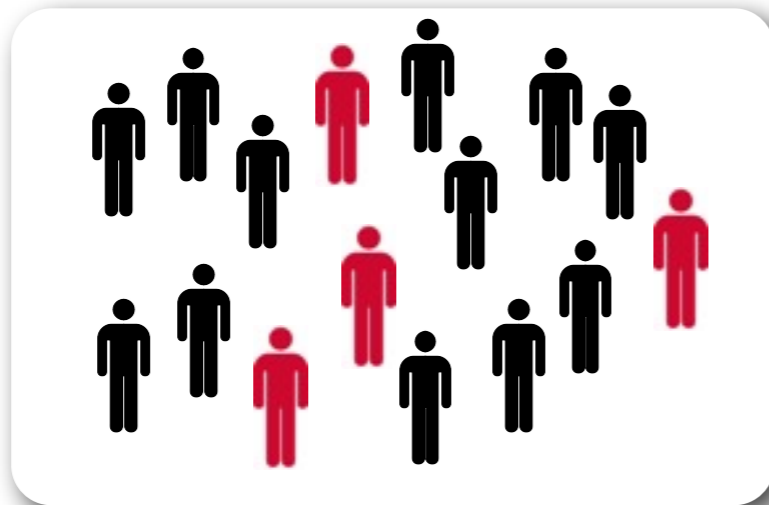


# Epidemiology meets phylogenetics

## Inferring epidemiological dynamics based on genetic sequence data

Gabriel Leventhal, Sebastian Bonhoeffer

Denise Kühnert, Alexei Drummond

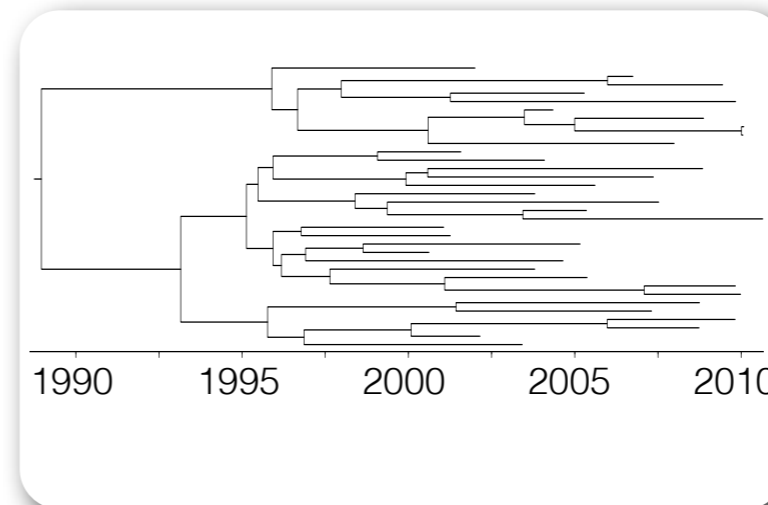
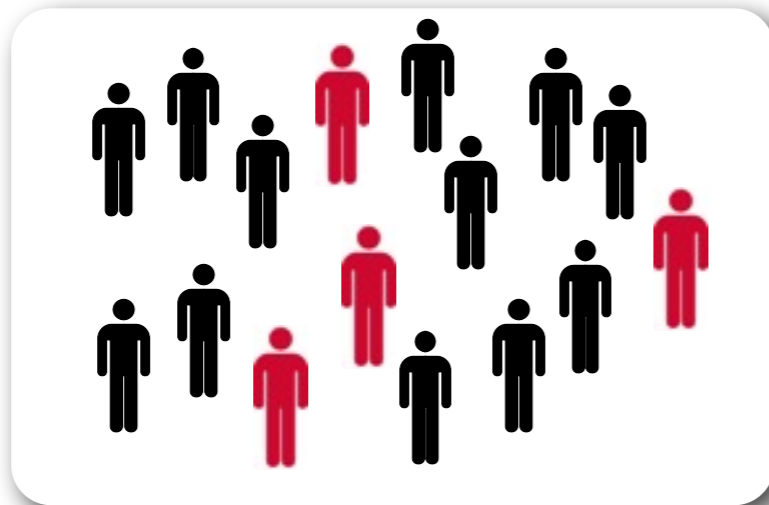


# Epidemiology meets phylogenetics

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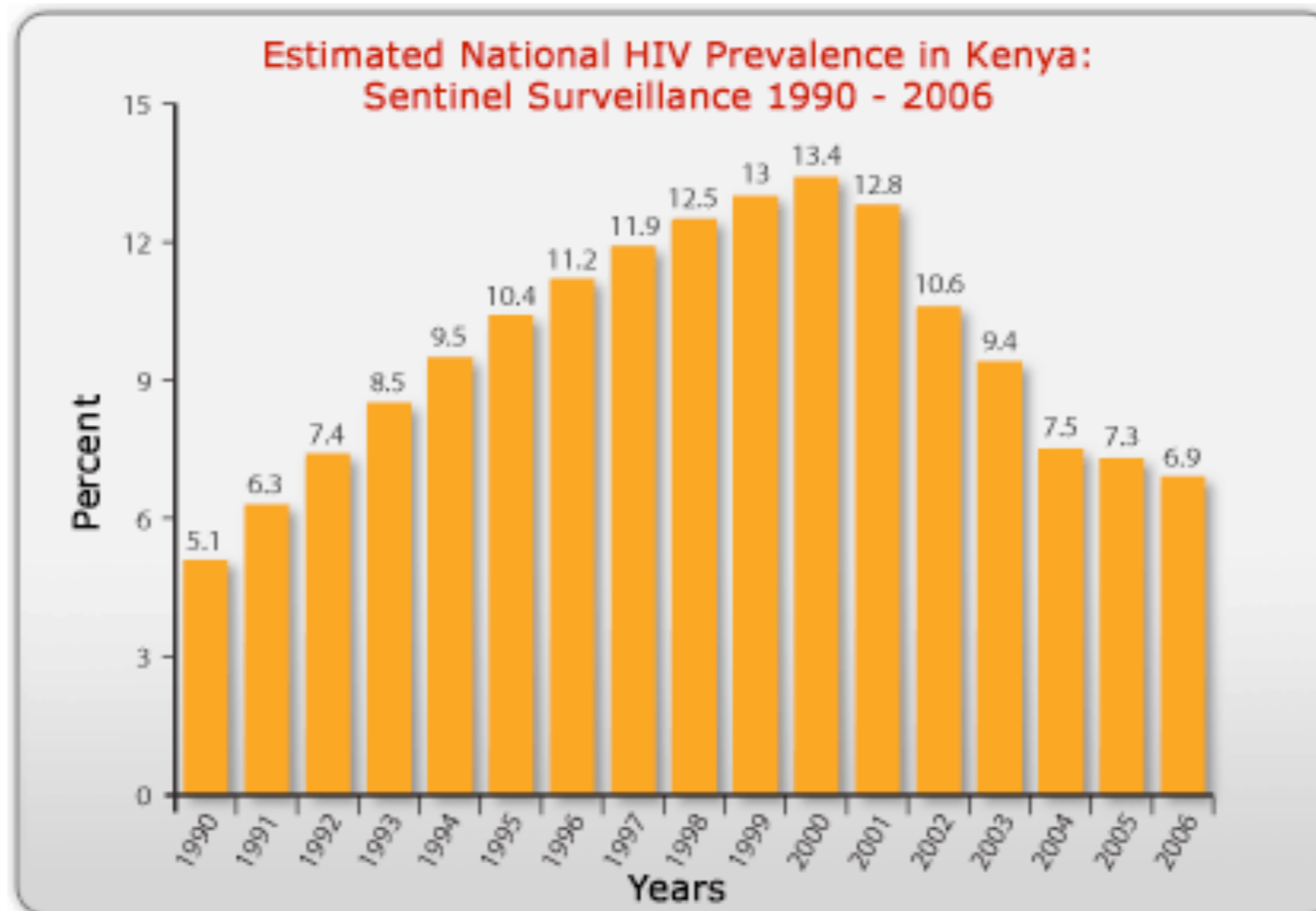
Gabriel Leventhal, Sebastian Bonhoeffer

Denise Kühnert, Alexei Drummond



# Epidemiology

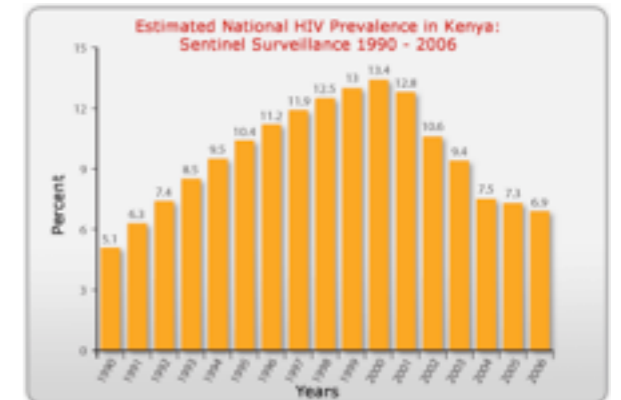
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# Epidemiology

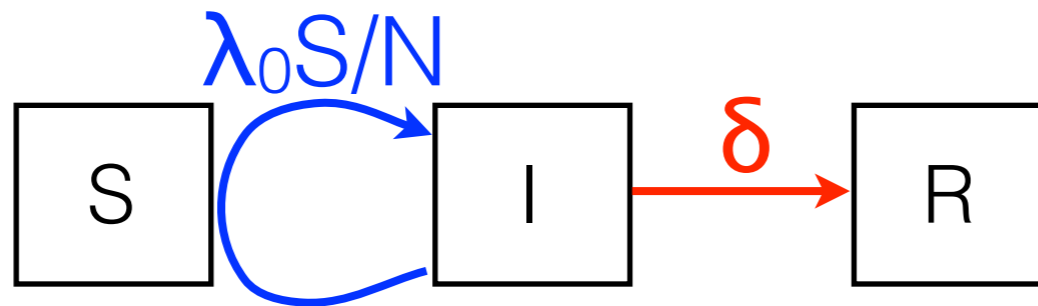
Data

# of infected individuals through time



Models

Population dynamics described by SIR models:

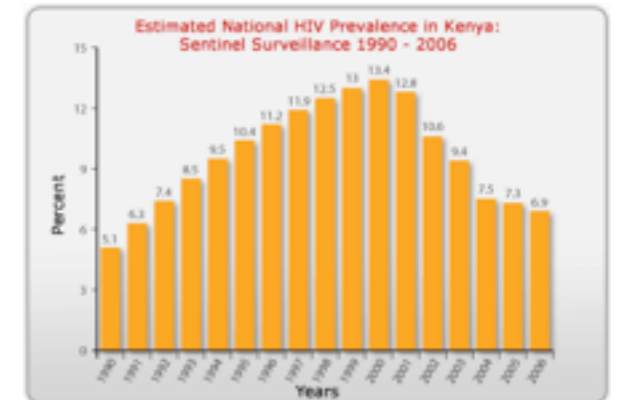


$$\begin{aligned}\frac{dS}{dt} &= -\lambda_0 IS/N \\ \frac{dI}{dt} &= \lambda_0 IS/N - \delta I \\ \frac{dR}{dt} &= \delta I\end{aligned}$$

# Epidemiology

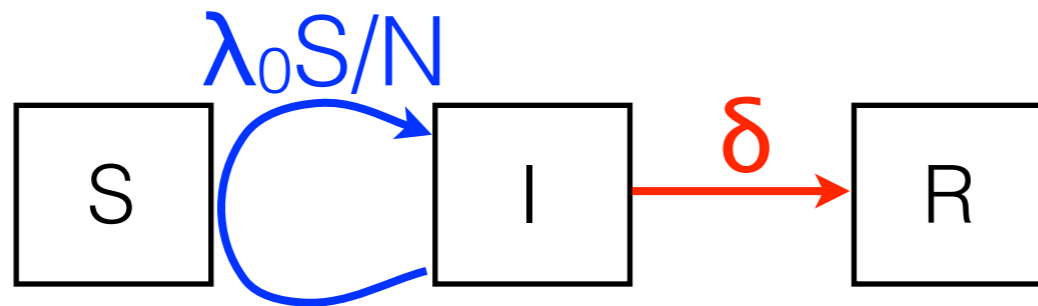
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# of infected individuals through time



Models

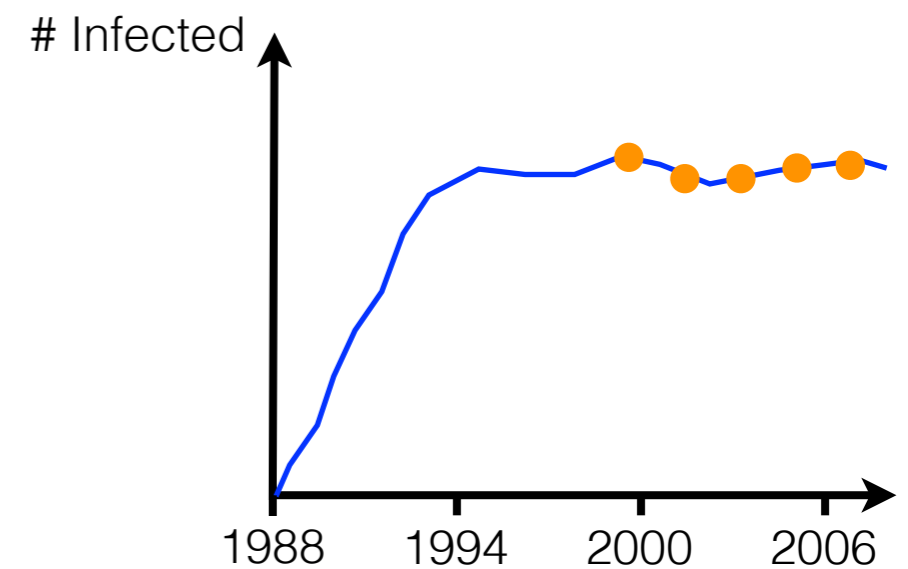
Population dynamics described by SIR models:



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Limitations

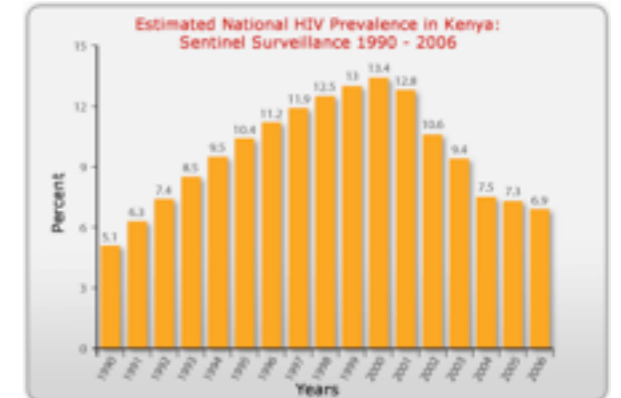
If sampling in early epidemic was missed:



# Epidemiology

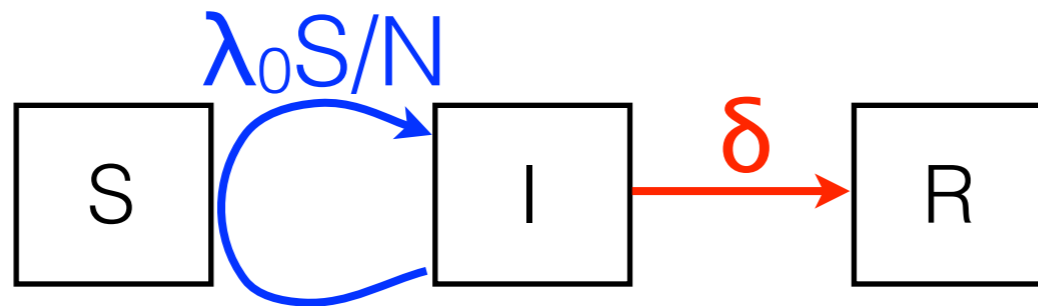
Data

# of infected individuals through time



Models

Population dynamics described by SIR models:

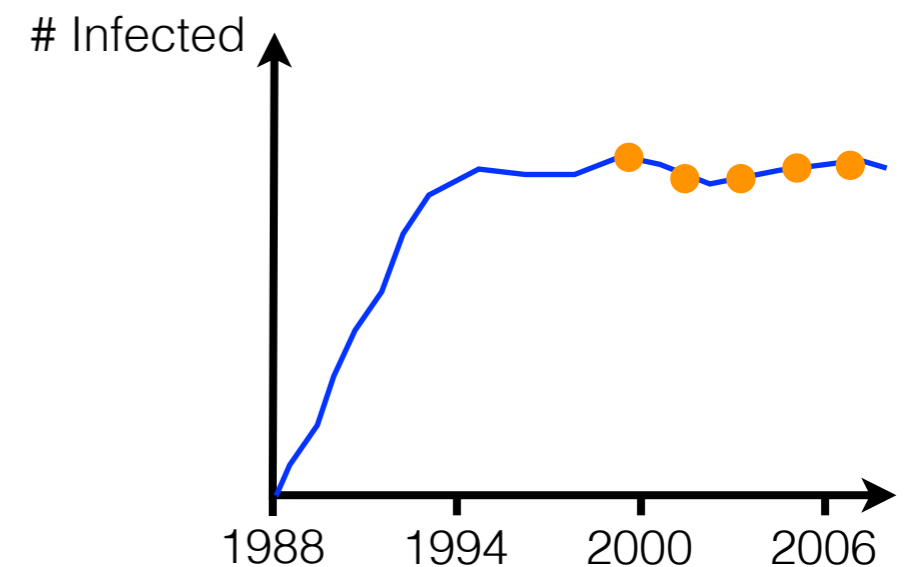


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If sampling in early epidemic was missed:

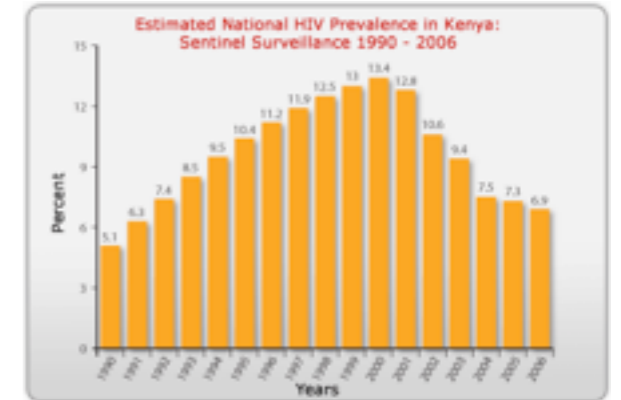
- ▶ **Time of epidemic outbreak?**
- ▶ **Basic reproductive number  $R_0$ ?**



# Epidemiology

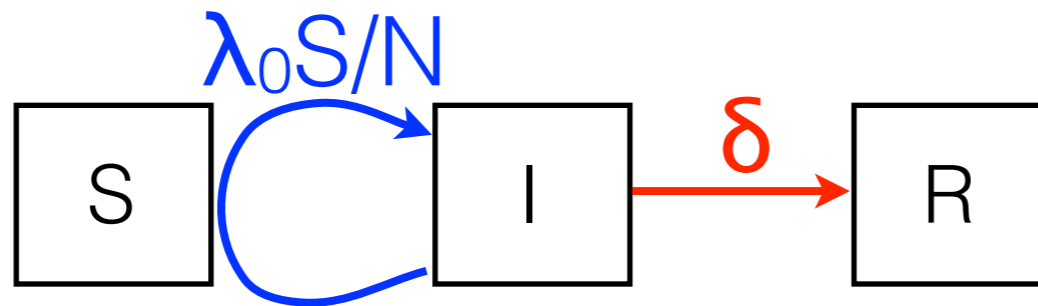
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# of infected individuals through time



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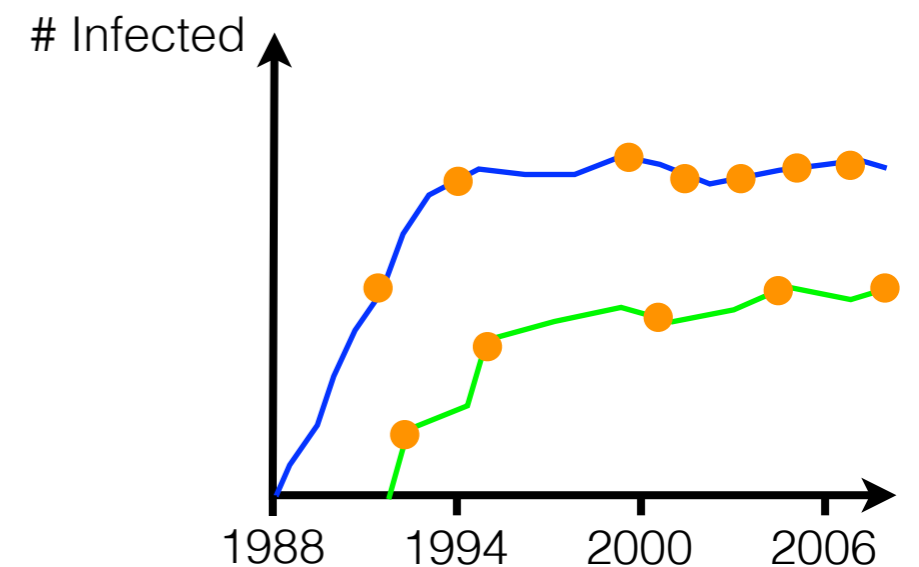
Limitations

If sampling in early epidemic was missed:

- ▶ **Time of epidemic outbreak?**
- ▶ **Basic reproductive number  $R_0$ ?**

Data does not tell who infected whom:

- ▶ **Population structure?**



# Genetic data entering epidemiology

---

Phylo-  
genetics

Inf1 ACACACCC  
Inf2 TCACACCT  
Inf3 AAAGACTT  
Inf4 ACAGACTT



# Genetic data entering epidemiology

---

Phylo-  
genetics

Input:

Pathogen genetic data from different hosts

Inf1 ACACACCC

Inf2 TCACACCT

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Inf4 ACAGACTT

# Genetic data entering epidemiology

---

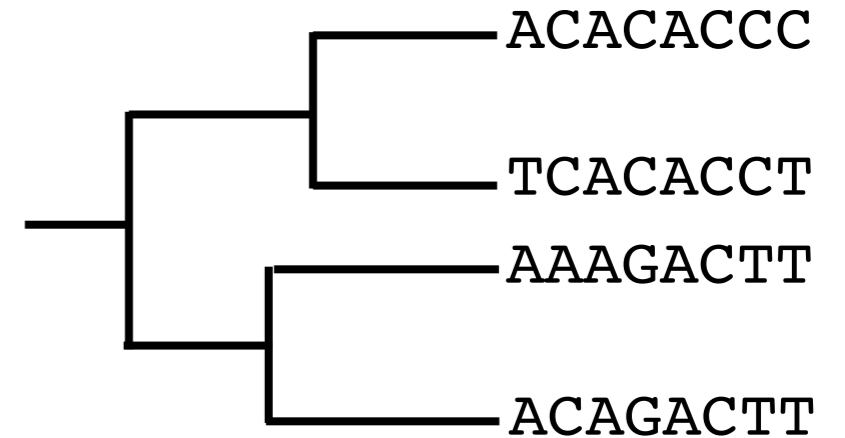
Phylo-  
genetics

Input:

Pathogen genetic data from different hosts

Output:

Transmission chain (who infected whom)



# Genetic data entering epidemiology

---

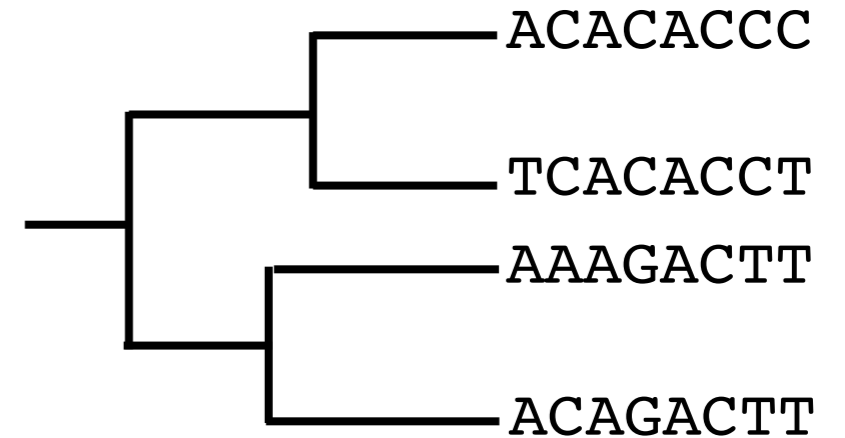
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Pathogen genetic data from different hosts

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Transmission chain (who infected whom)



## Example key result

Emergence of HIV

Epidemic identified in 1980s

# Genetic data entering epidemiology

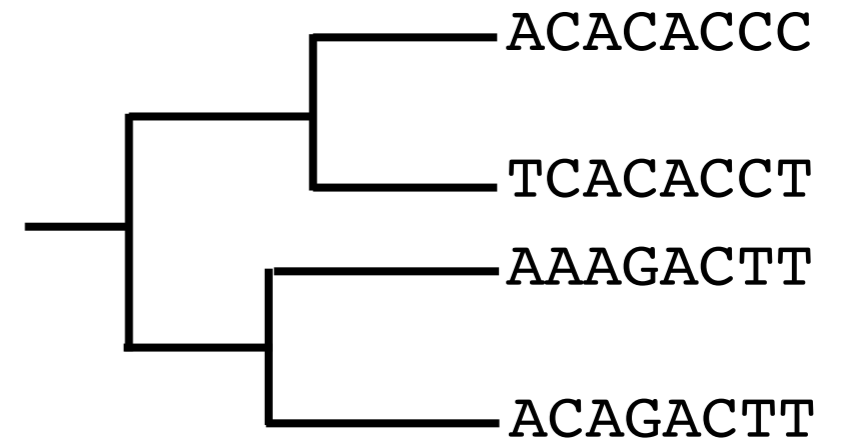
## Phylo- genetics

Input:

Pathogen genetic data from different hosts

Output:

Transmission chain (who infected whom)

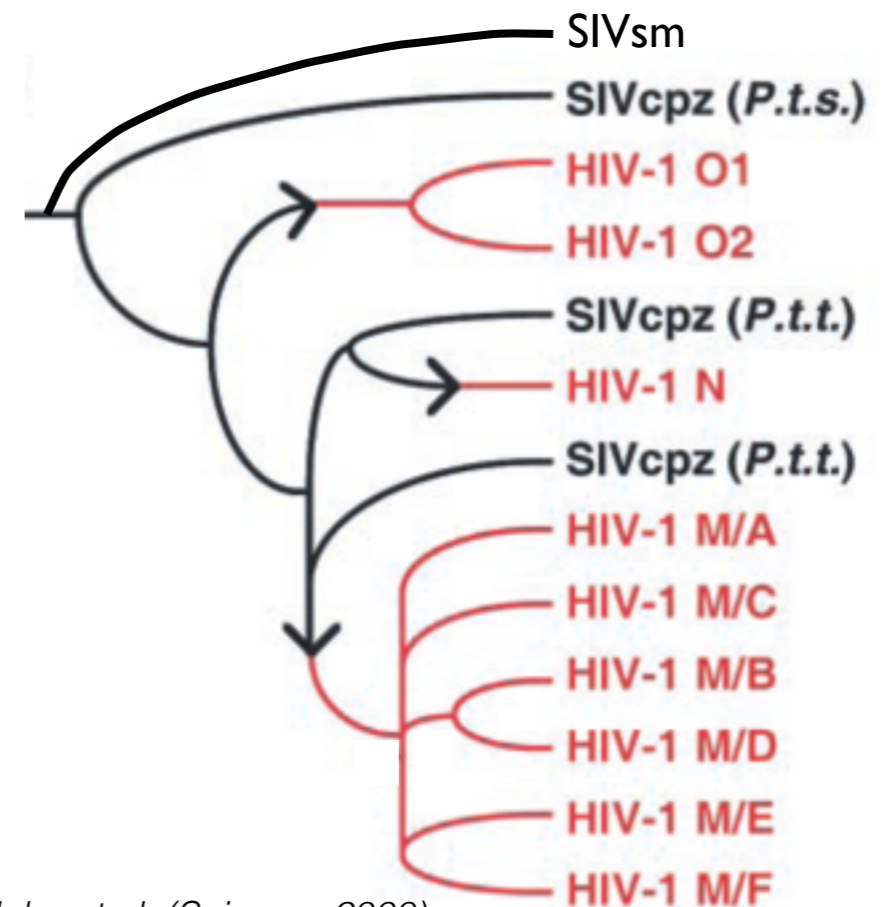


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Epidemic identified in 1980s

**Sequence data tells us about pre-1980**

Example  
key result



# Genetic data entering epidemiology

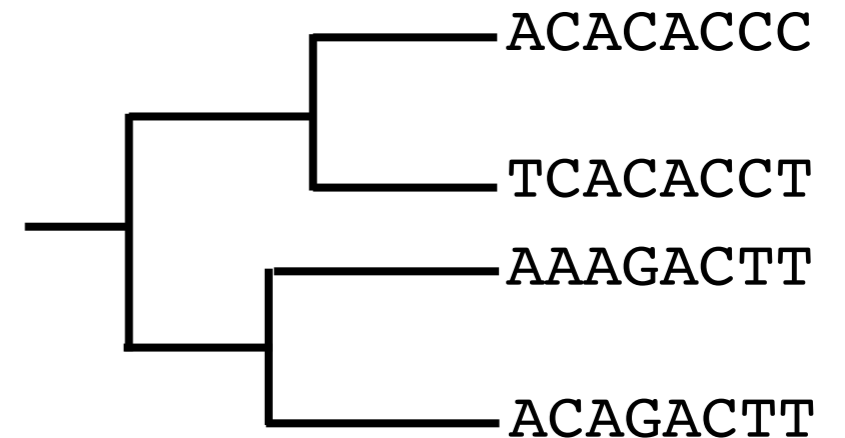
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Pathogen genetic data from different hosts

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Transmission chain (who infected whom)



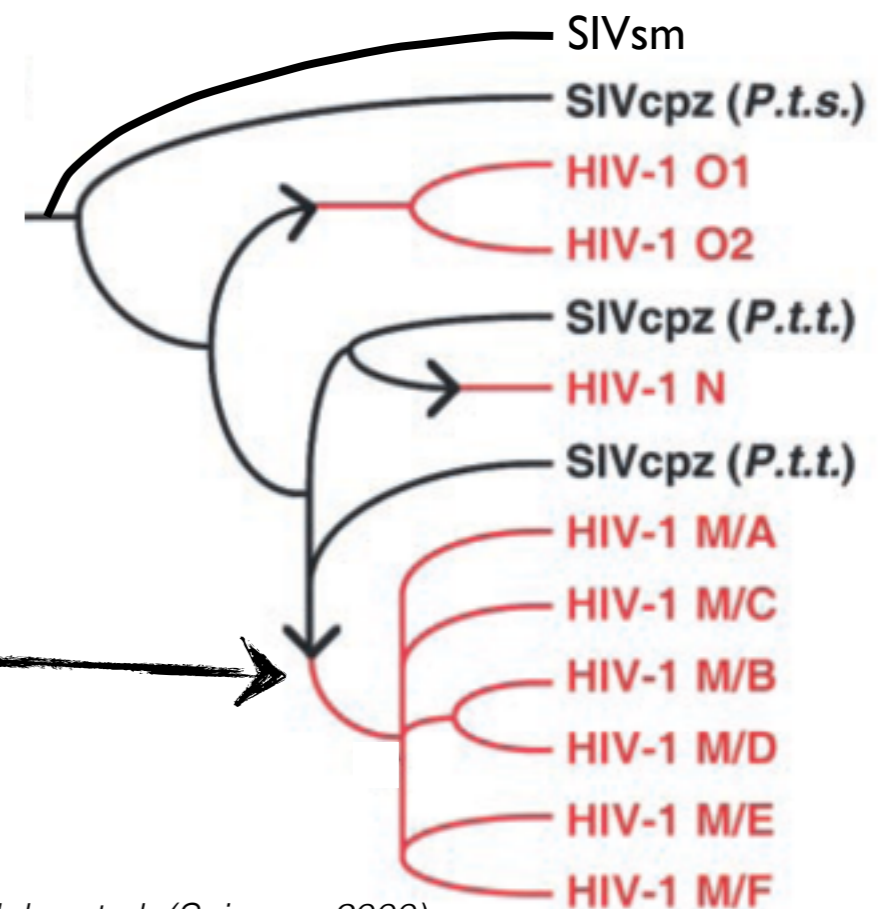
## Example key result

Emergence of HIV

Epidemic identified in 1980s

**Sequence data tells us about pre-1980**

- ▶ Zoonosis from chimps
- ▶ In Africa
- ▶ Early 20th century

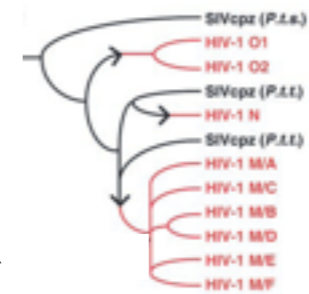


# Genetic data contains information about the epidemiological dynamics

Phylo-  
genetics

State of process

- ▶ Time and geographic location of outbreak



Emergence of a  
pathogen  
(here HIV)  
Hahn et al. (Science, 2000)

# Genetic data contains information about the epidemiological dynamics

## Phylo- genetics

State of process

- ▶ Time and geographic location of outbreak

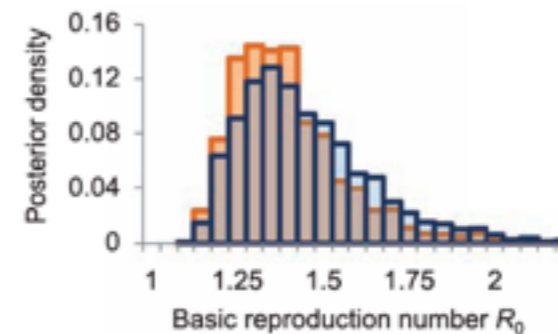


Emergence of a  
pathogen  
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Hahn et al. (Science, 2000)

## Phylo- dynamics

Dynamics of process

- ▶ Transmission process



Basic reproductive  
number of an  
emerging pathogen  
(here H1N1)  
Fraser et al. (Science, 2009)

# Genetic data contains information about the epidemiological dynamics

## Phylogenetics

State of process

- ▶ Time and geographic location of outbreak

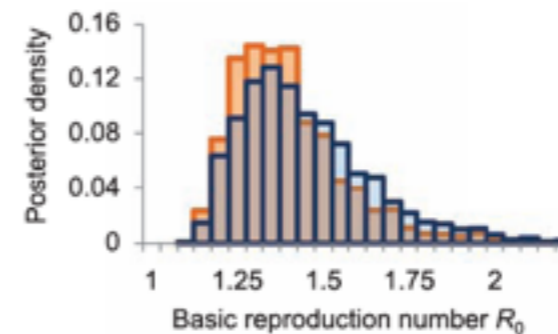


Emergence of a pathogen (here HIV)  
Hahn et al. (Science, 2000)

## Phylo-dynamics

Dynamics of process

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Basic reproductive number of an emerging pathogen (here H1N1)  
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## Epidemiological models

Ideally: assume epidemiological model in phylogenetics (birth-death model)

- ▶ Quantification of all model parameters!

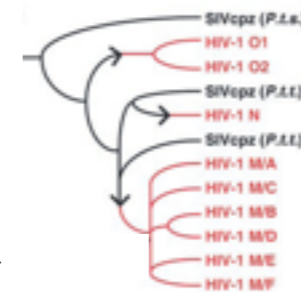


# Genetic data contains information about the epidemiological dynamics

## Phylogenetics

State of process

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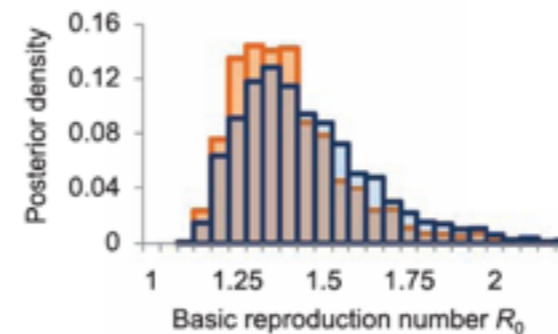


Emergence of a pathogen (here HIV)  
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## Phylo-dynamics

Dynamics of process

- ▶ Transmission process



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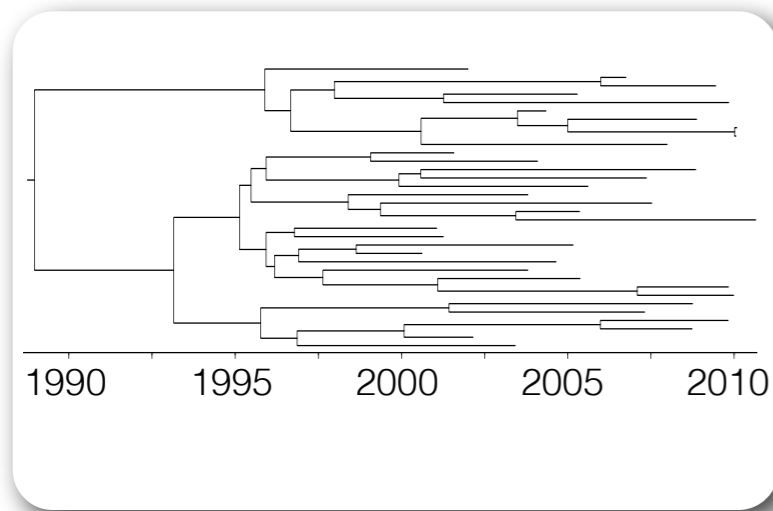
- ▶ Quantification of all model parameters!

Approximate: by population genetic model (coalescent)

- ▶ Only deterministic population size is parameterized!

# Merge epidemiology and phylogenetics

---

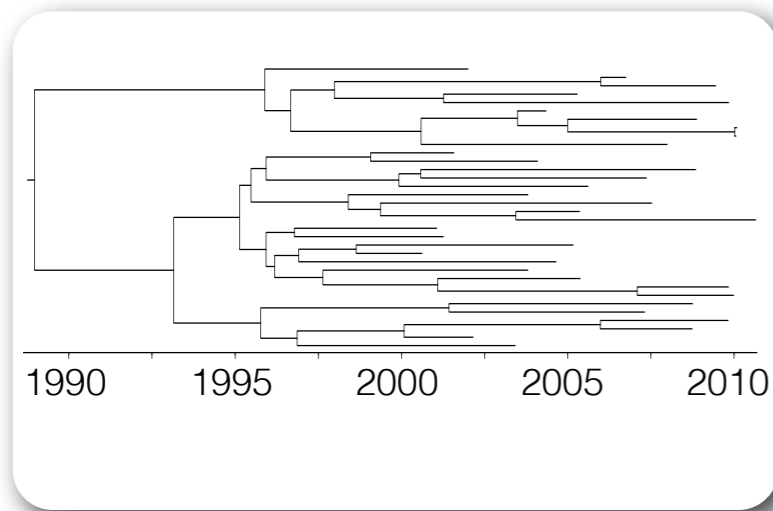


## **Methodology to:**

- 1) Reconstruct phylogenetic trees
- 2) Fit epidemiological models to phylogenetic trees

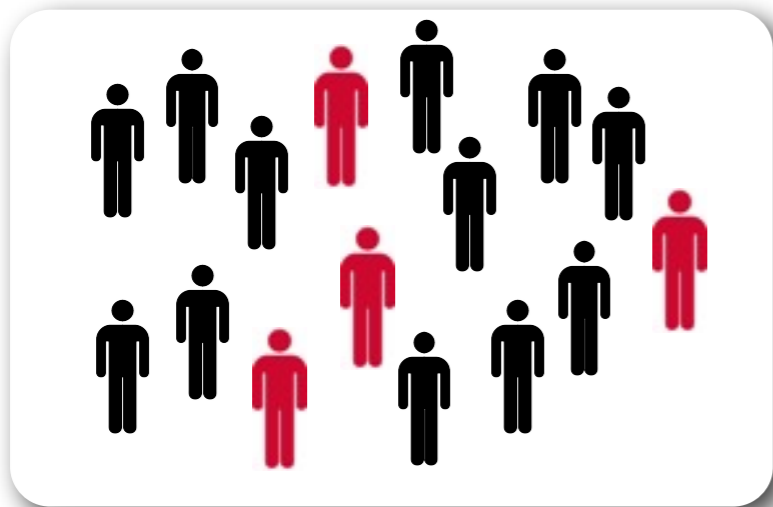
# Merge epidemiology and phylogenetics

---



## **Methodology to:**

- 1) Reconstruct phylogenetic trees
- 2) Fit epidemiological models to phylogenetic trees



**Quantification of spread of infectious diseases?**

**Factors governing transmission dynamics?**

(e.g. population structure, environment, vaccines)

# General modeling framework

---

Epidemiological model

Growth of tree

- ▶ parameters  $\eta$



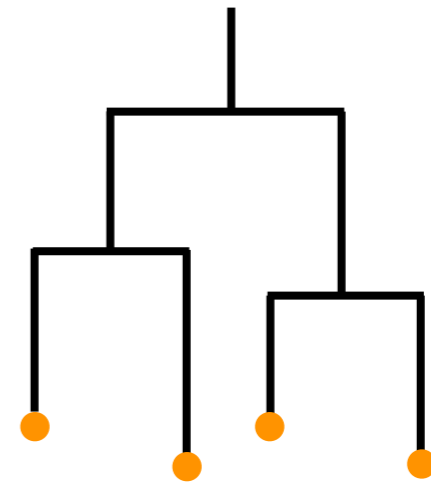
# General modeling framework

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# General modeling framework

---

Epidemiological model

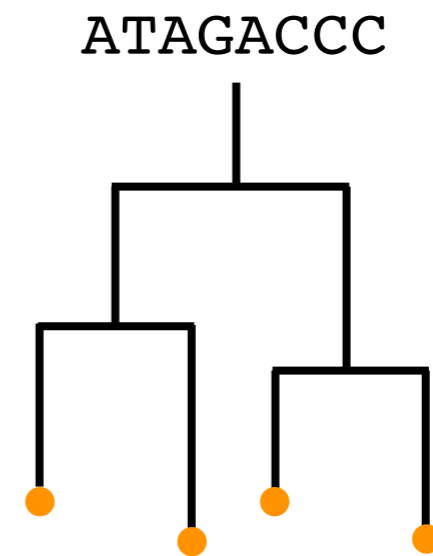
Growth of tree

- ▶ parameters  $\eta$

Evolutionary model

Evolution of sequences along tree

- ▶ parameters  $\theta$



# General modeling framework

---

Epidemiological model

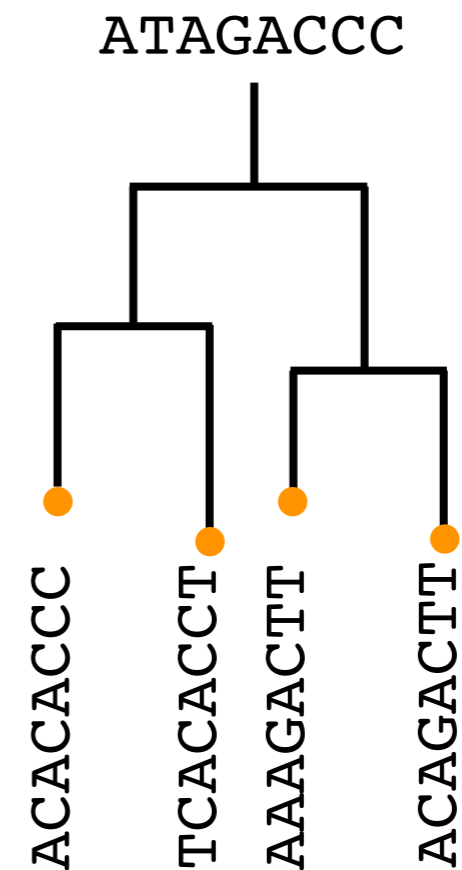
Growth of tree  
▶ parameters  $\eta$

Evolutionary model

Evolution of sequences along tree  
▶ parameters  $\theta$

Tree distribution

Defined through  $\eta$  and  $\theta$



# General modeling framework

---

Epidemiological model

Growth of tree  
▶ parameters  $\eta$

Evolutionary model

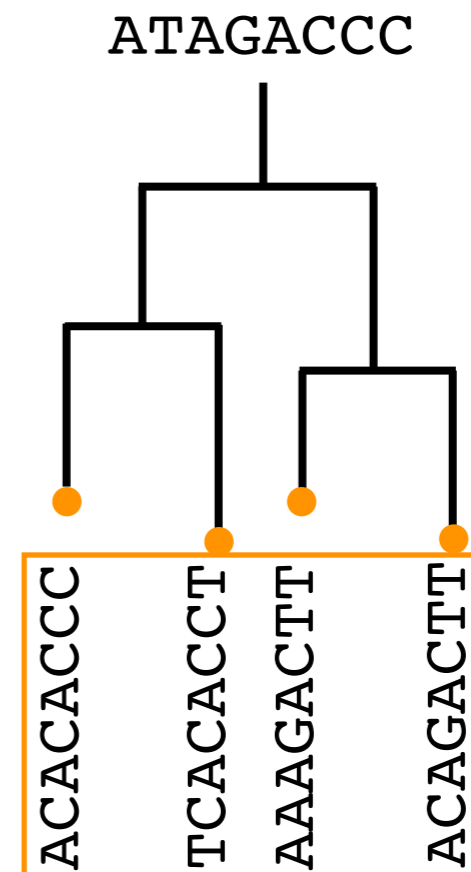
Evolution of sequences along tree  
▶ parameters  $\theta$

Tree distribution

Defined through  $\eta$  and  $\theta$

Data

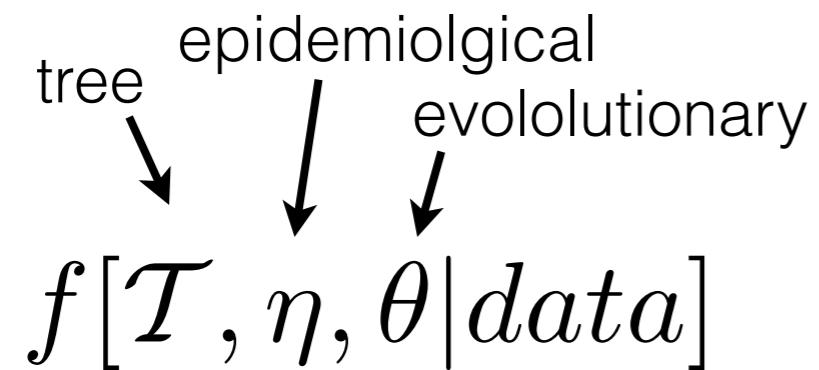
Sequence alignment





# Bayesian approach for estimating epidemiological parameters

---



# Bayesian approach for estimating epidemiological parameters

---

tree          epidemiolglcal  
                  ↓                    ↓  
  ↓  
  evololutionary

$$f[\mathcal{T}, \eta, \theta | data] = \frac{f[data | \mathcal{T}, \theta] f[\mathcal{T} | \eta] f[\eta, \theta]}{f[data]}$$

# Bayesian approach for estimating epidemiological parameters

---

tree      epidemiological  
          ↓      ↓  
          ↓      ↓  
          ↓      ↓  
          ↓      ↓  
          ↓      ↓

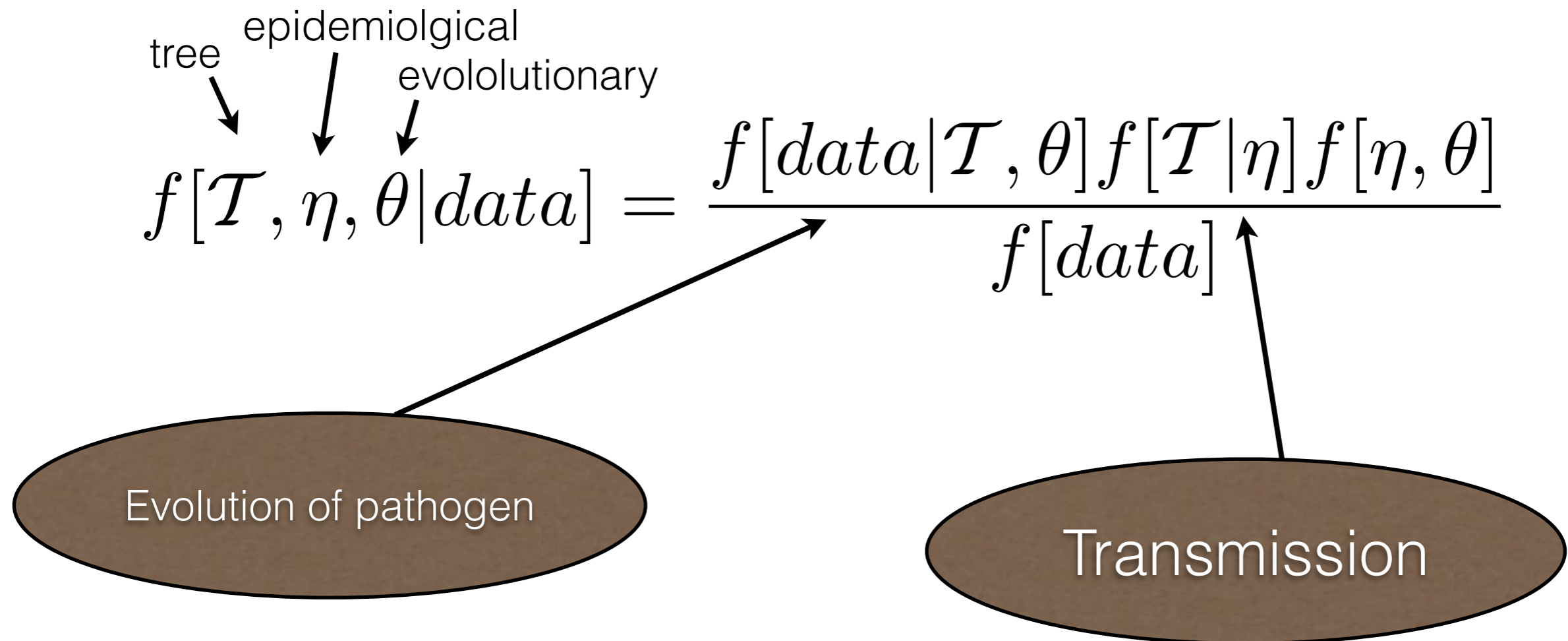
evolutionary

$$f[\mathcal{T}, \eta, \theta | data] = \frac{f[data | \mathcal{T}, \theta] f[\mathcal{T} | \eta] f[\eta, \theta]}{f[data]}$$

Evolution of pathogen

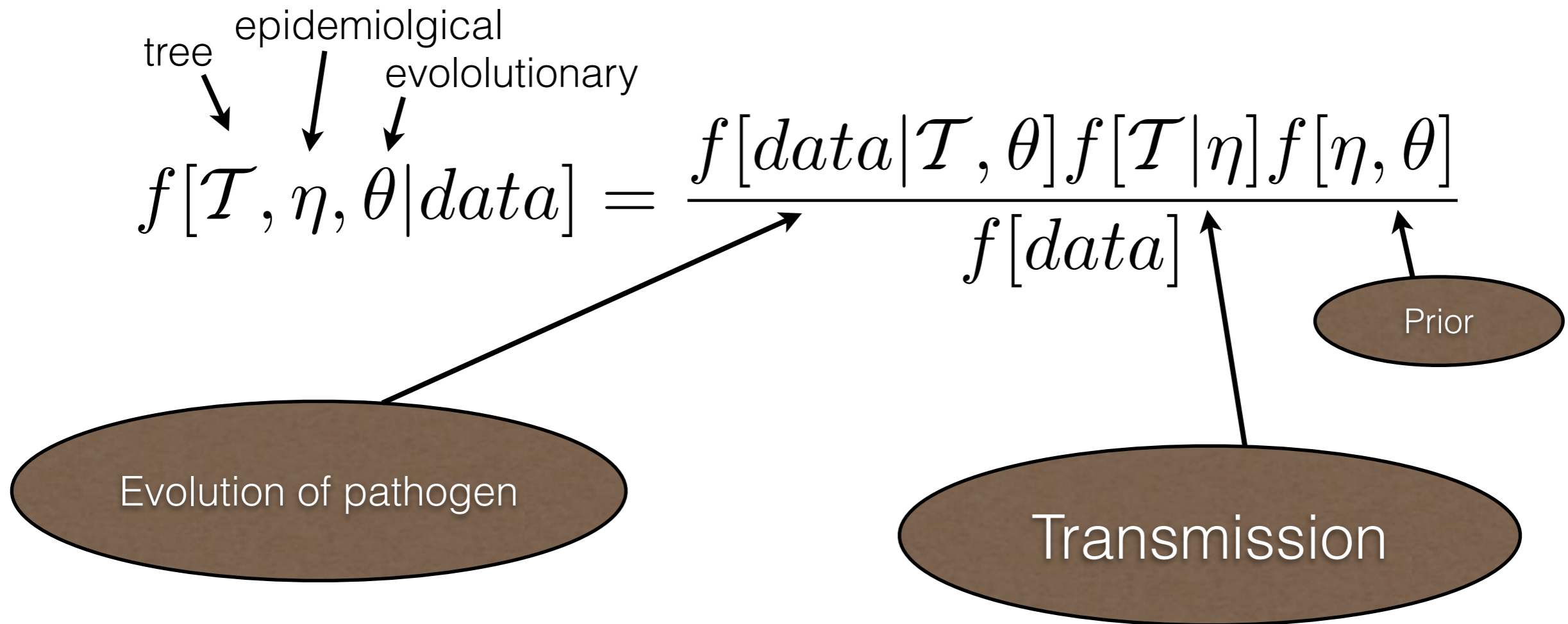
# Bayesian approach for estimating epidemiological parameters

---



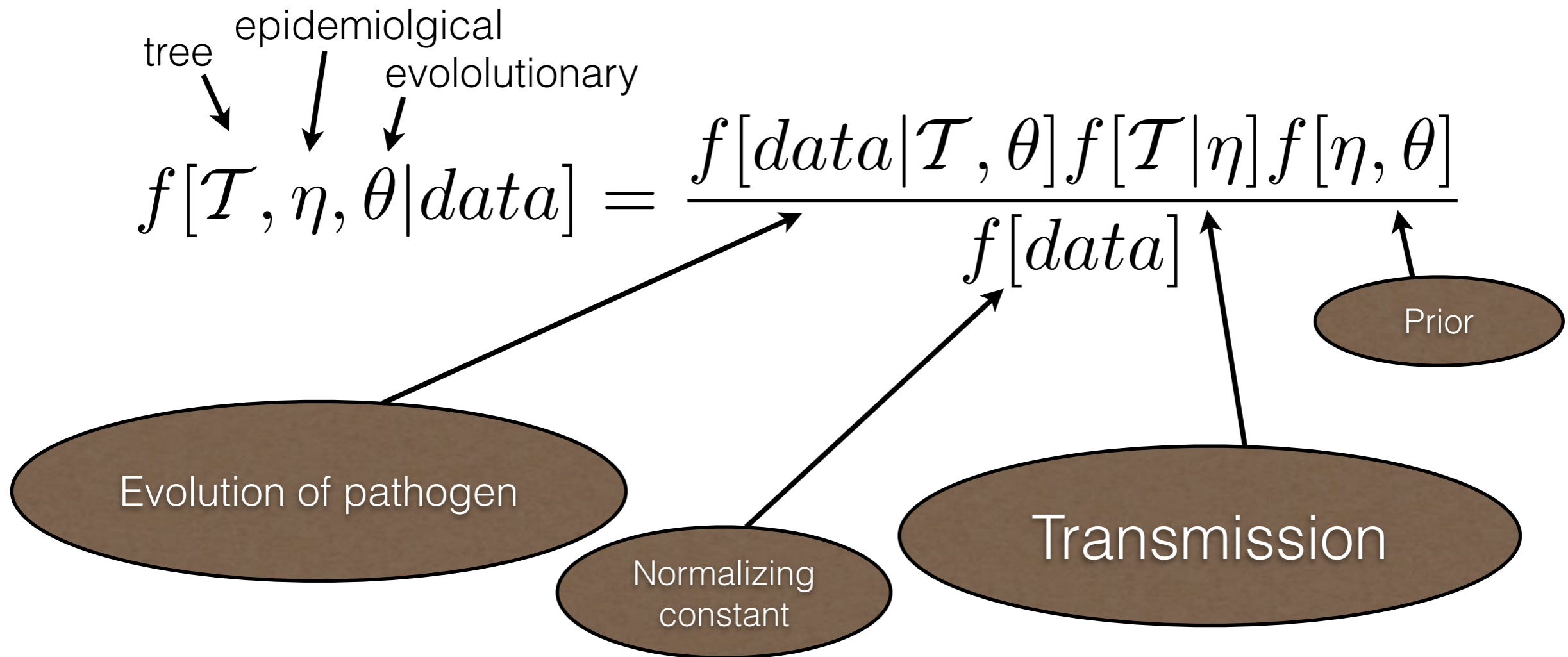
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---

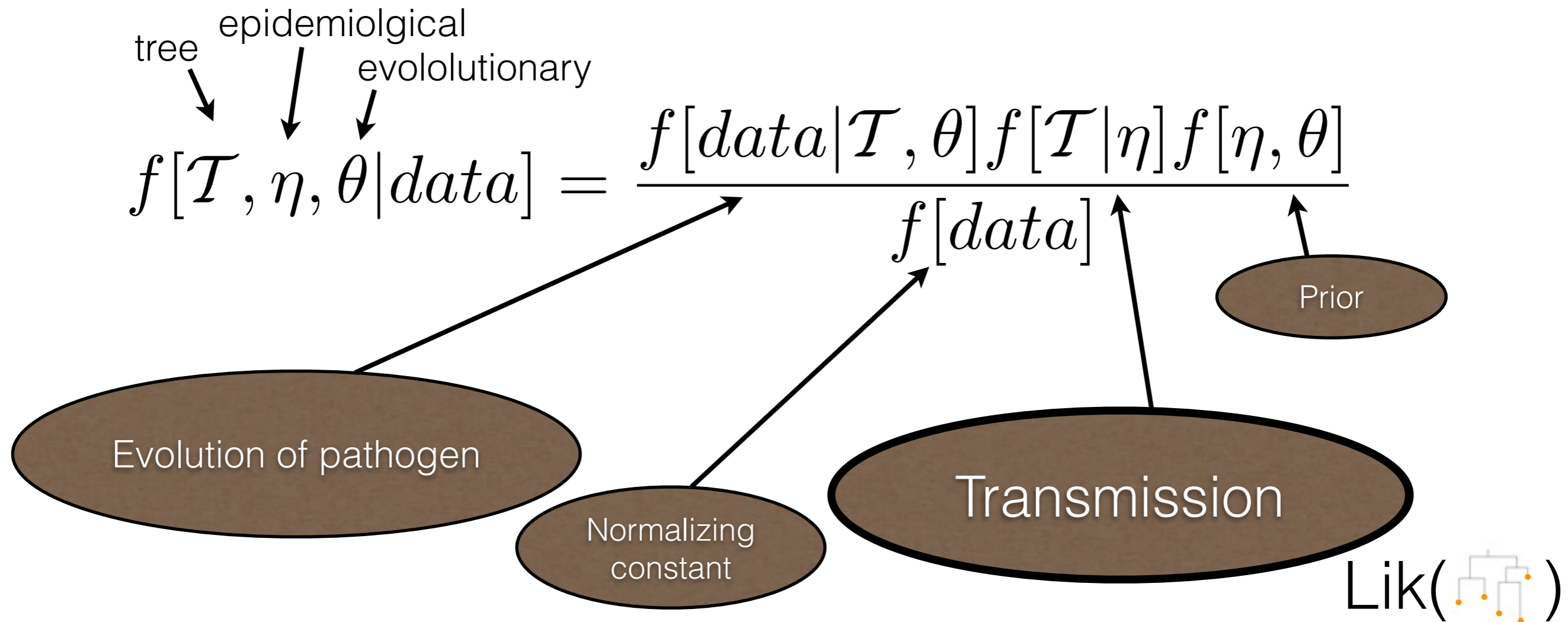


# Bayesian approach for estimating epidemiological parameters

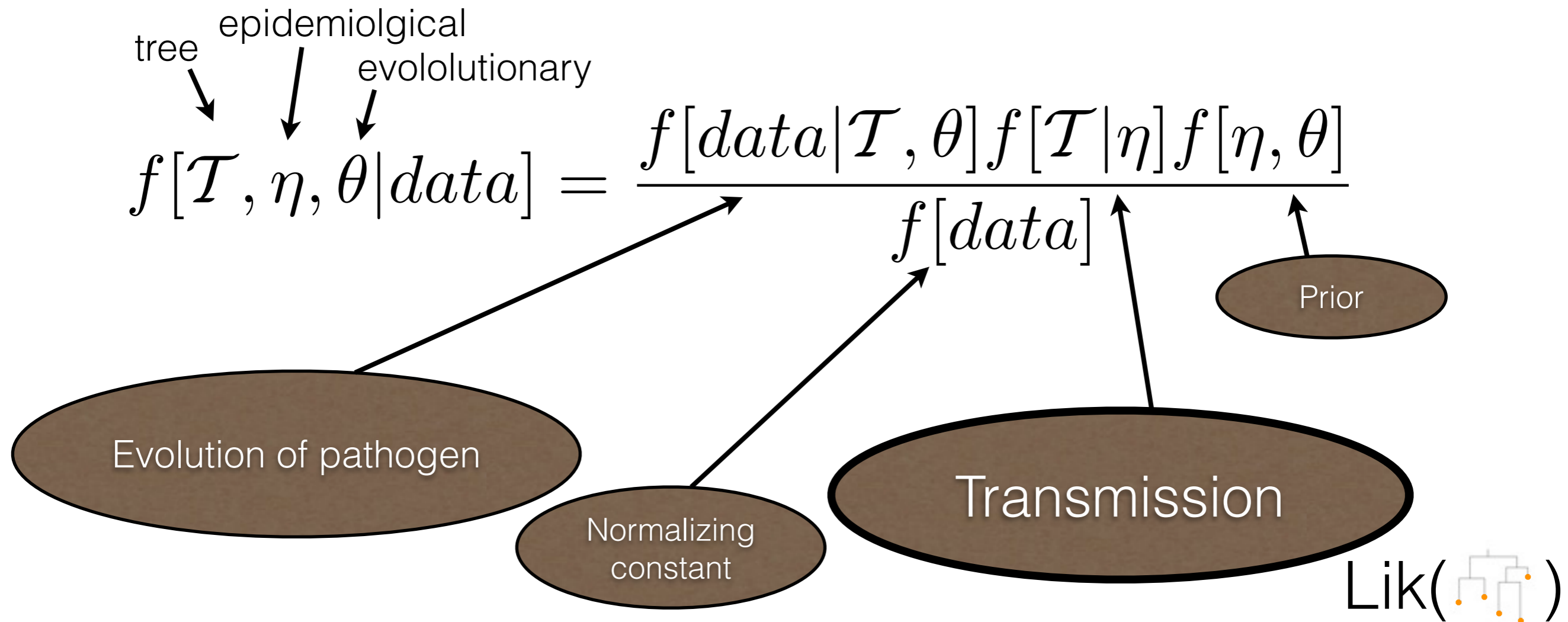
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# Bayesian approach for estimating epidemiological parameters



# Bayesian approach for estimating epidemiological parameters



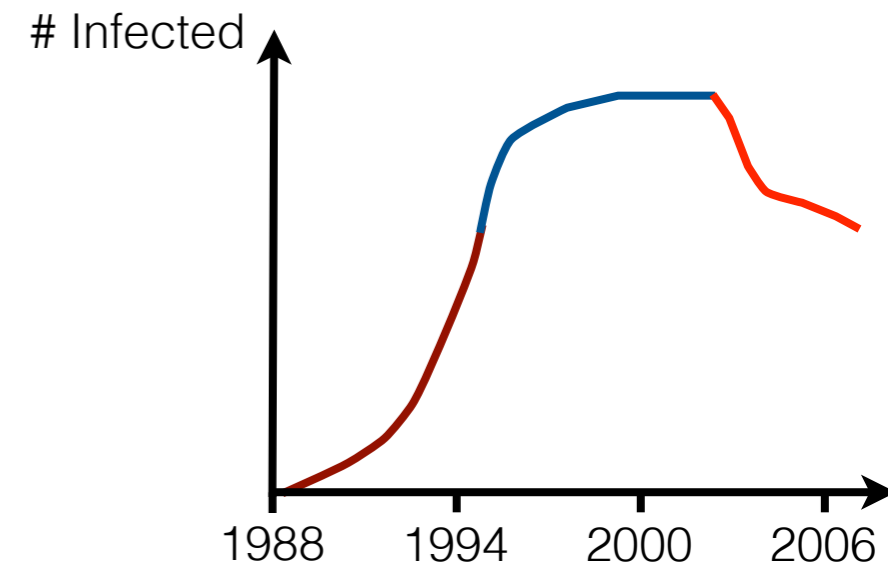
Implemented in Beast

Transmission model: coalescent or birth-death model



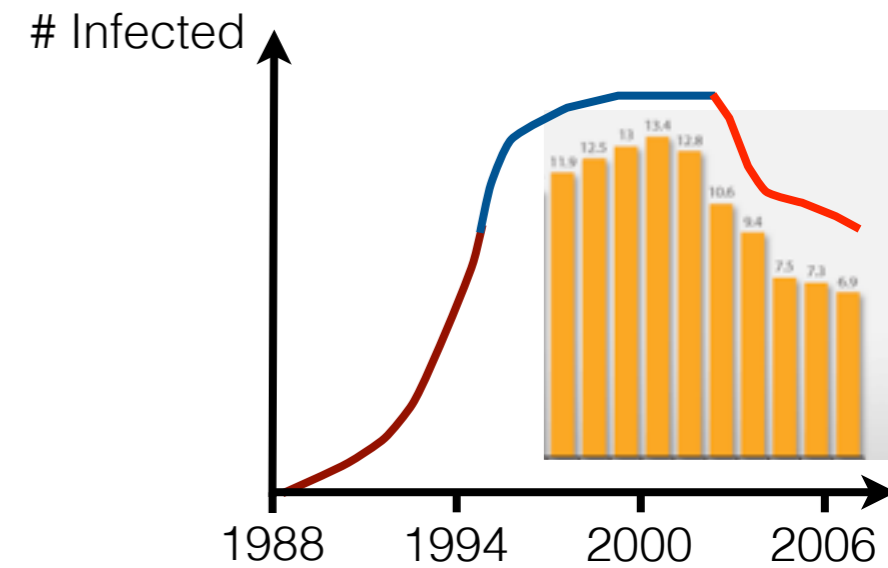
# Phylogenetic methods for different epidemic dynamics

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# Phylogenetic methods for different epidemic dynamics

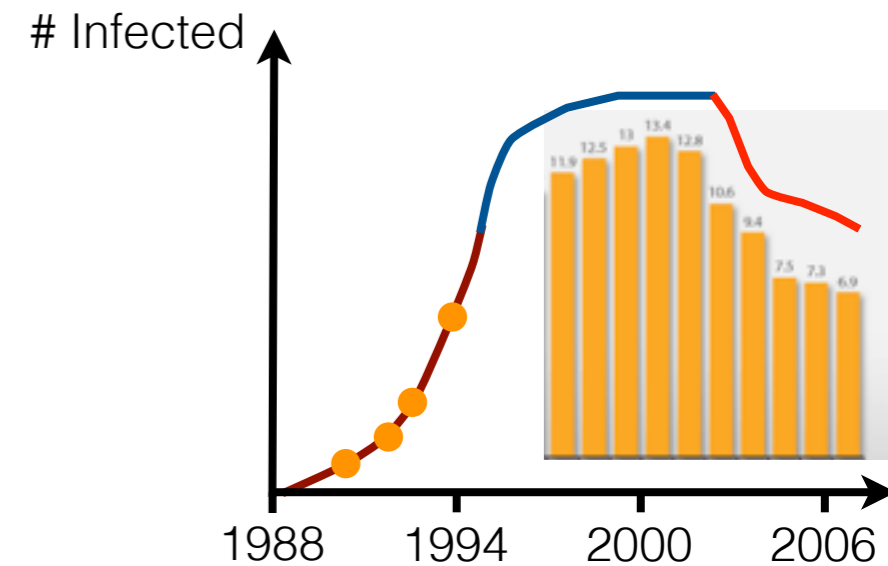
---



# Phylogenetic methods for different epidemic dynamics

## 1. ...for analyzing epidemic outbreaks

- ▶ *C*: Drummond et al. (*Genetics*, 2002)
- ▶ *BD*: Stadler et al. (*MBE*, 2012)



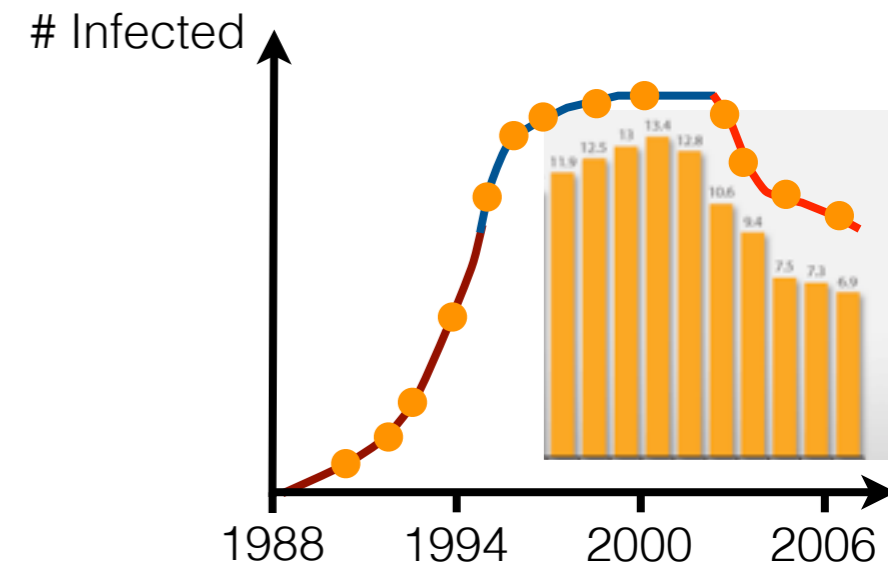
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## 2. ...for identifying epidemiological changes over time

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# Phylogenetic methods for different epidemic dynamics

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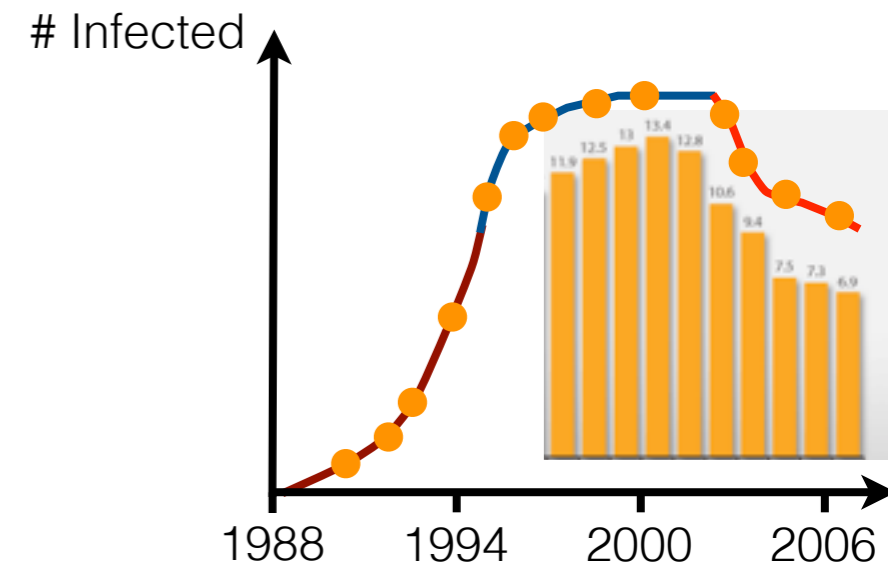
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## 3. ...accounting for SIR model dynamics

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# Phylogenetic methods for different epidemic dynamics

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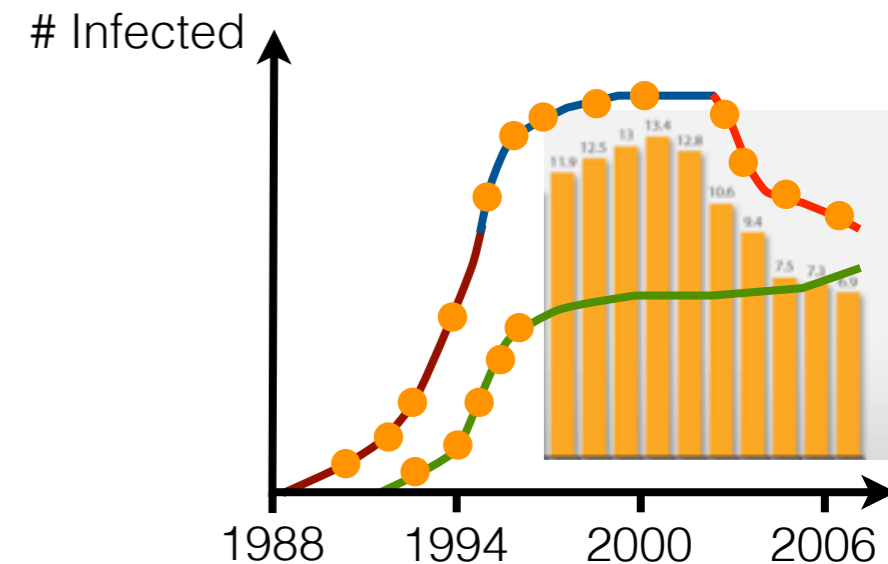
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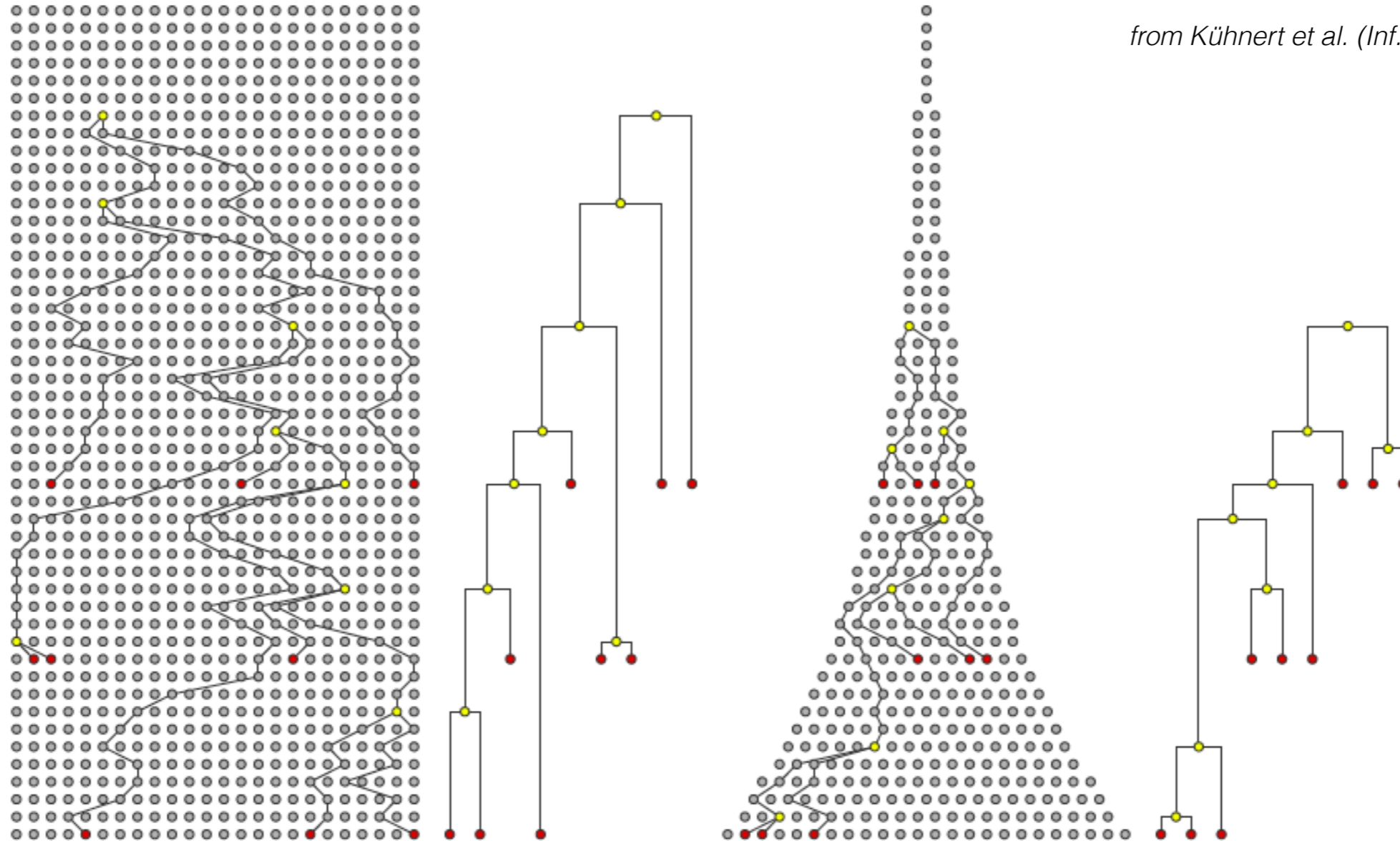
## 4. ...accounting for host population structure

- ▶ *C*: Volz (*Genetics*, 2012)
- ▶ *BD*: Stadler & Bonhoeffer (*Phil. Trans. Roy. Soc. B*, 2013)



# Part A

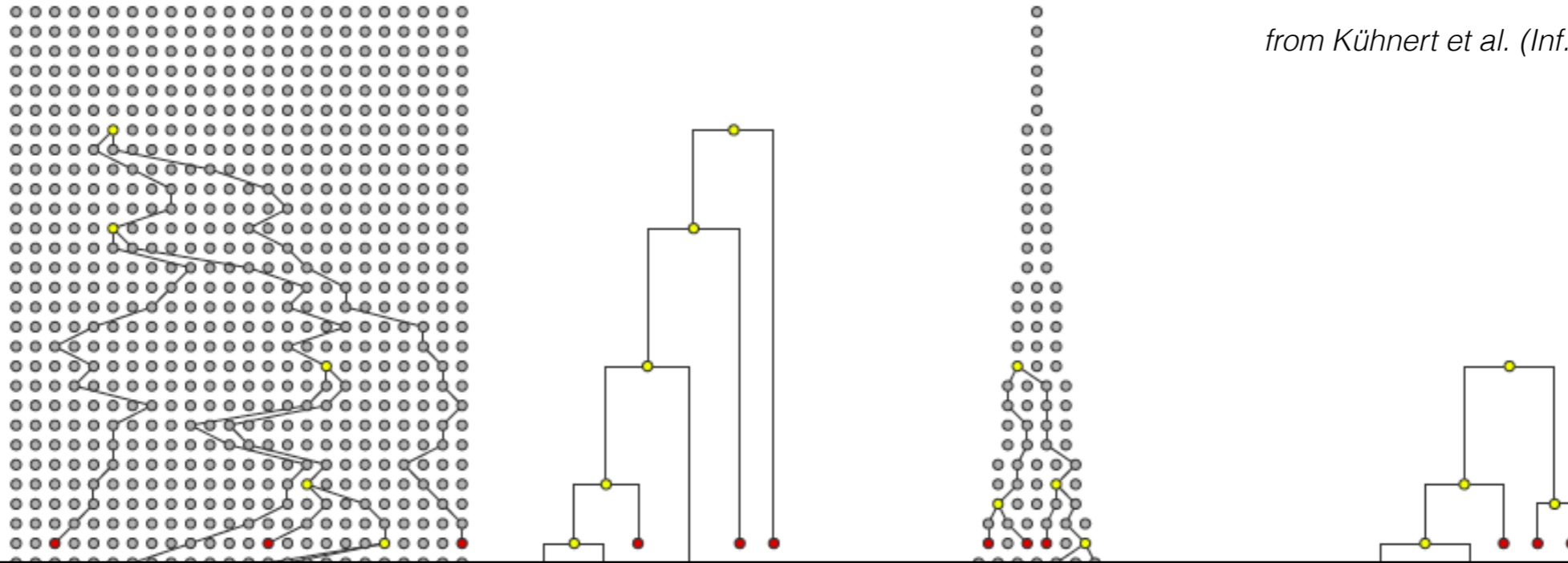
## Coalescent as a model for transmission



from Kühnert et al. (*Inf. Gen. Evol.*, 2011)

# Part A

## Coalescent as a model for transmission



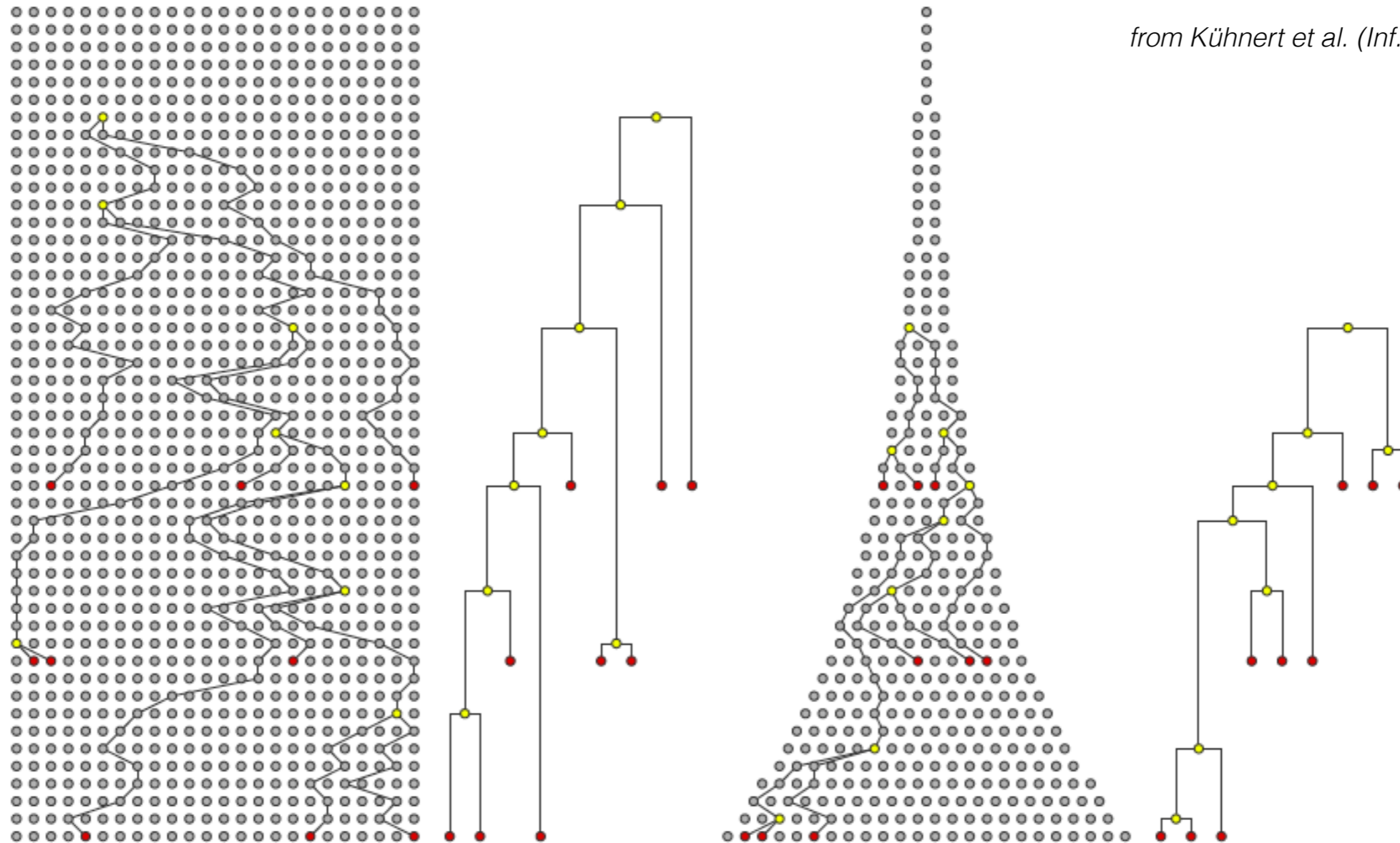
Lik (  ) ?





# Part A

## Coalescent as a model for transmission



from Kühnert et al. (*Inf. Gen. Evol.*, 2011)

$$f_G(g|\theta) = \frac{1}{\theta^{n-1}} \cdot \prod_{i=2}^{2n-1} e^{(-k_i(k_i-1)/2\theta)(t_i - t_{i-1})}$$

$$f_G(g|\theta, r) = \frac{1}{\theta^{n-1}} \cdot \prod_{i=2}^{2n-1} e^{r t_i} e^{(-k_i(k_i-1)/2\theta r)(\sigma t_i - \sigma t_{i-1})}$$

# Estimating $R_0$ from sequencing data

---

Hepatitis C

Little known before first isolation, ie. pre-1989.

How can we determine basic reproductive number  $R_0$ ?

# Estimating $R_0$ from sequencing data

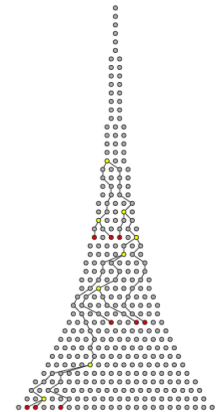
---

Hepatitis C

Little known before first isolation, ie. pre-1989.  
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Inference

40-100 sequences per subtype  
Fit exponential-growth coalescent to sequences and obtain growth rate  $r$  (i.e.  $\eta=r$ )  
 $R_0 = rD + 1$  (where  $D$  is expected time of infectiousness)



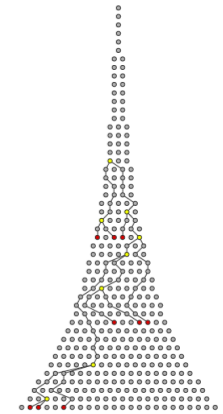
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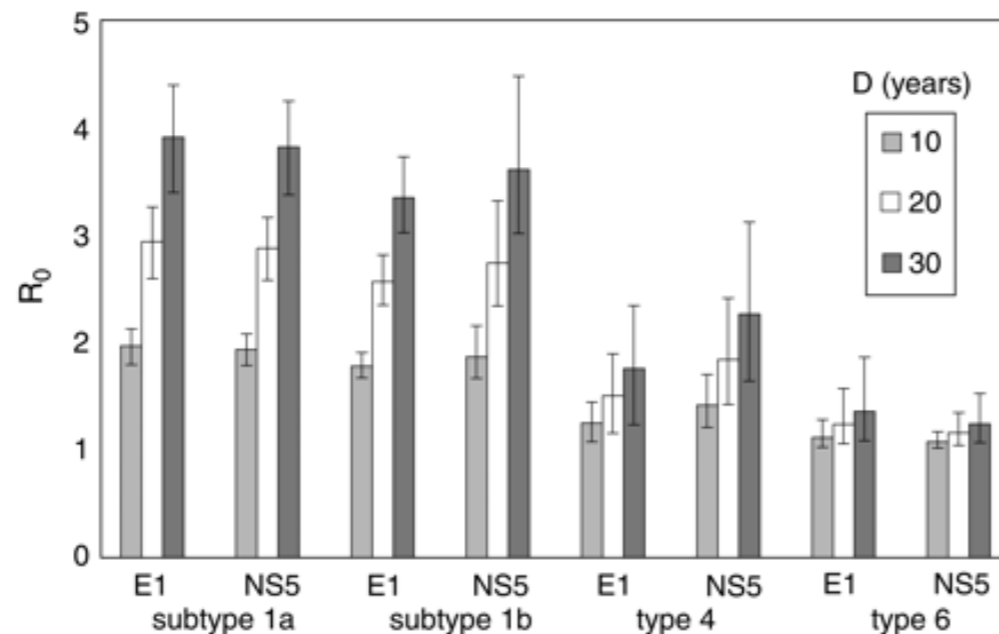
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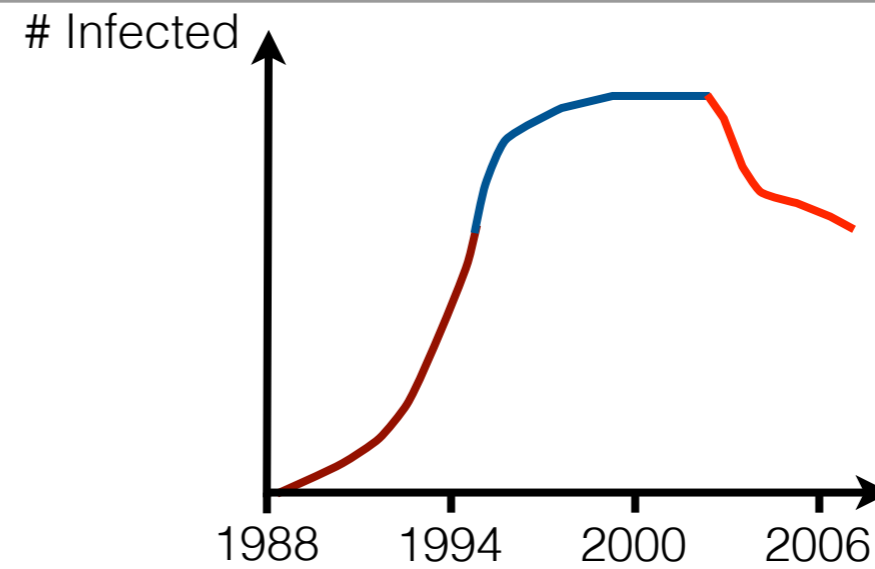


Results



# Bayesian skyline plot relaxes constant growth rate

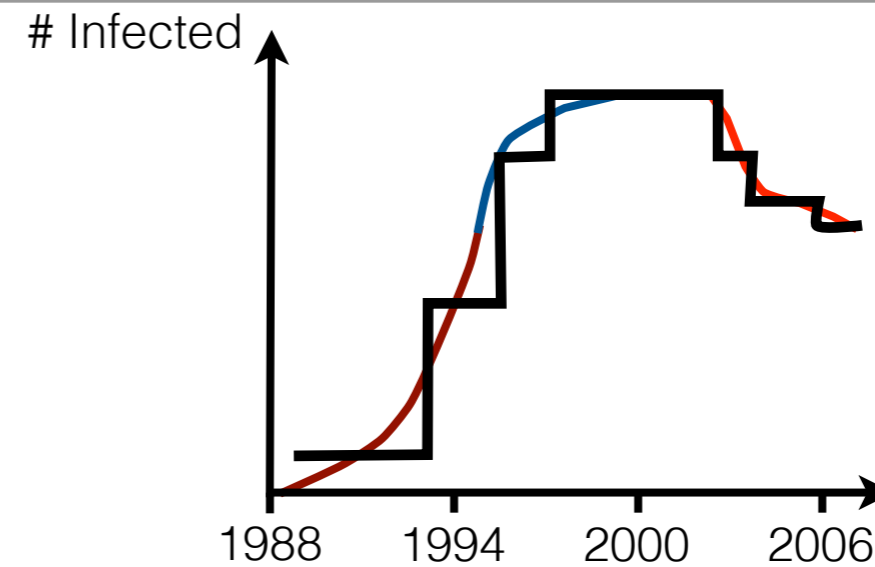
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# Bayesian skyline plot relaxes constant growth rate

Assump-  
tion

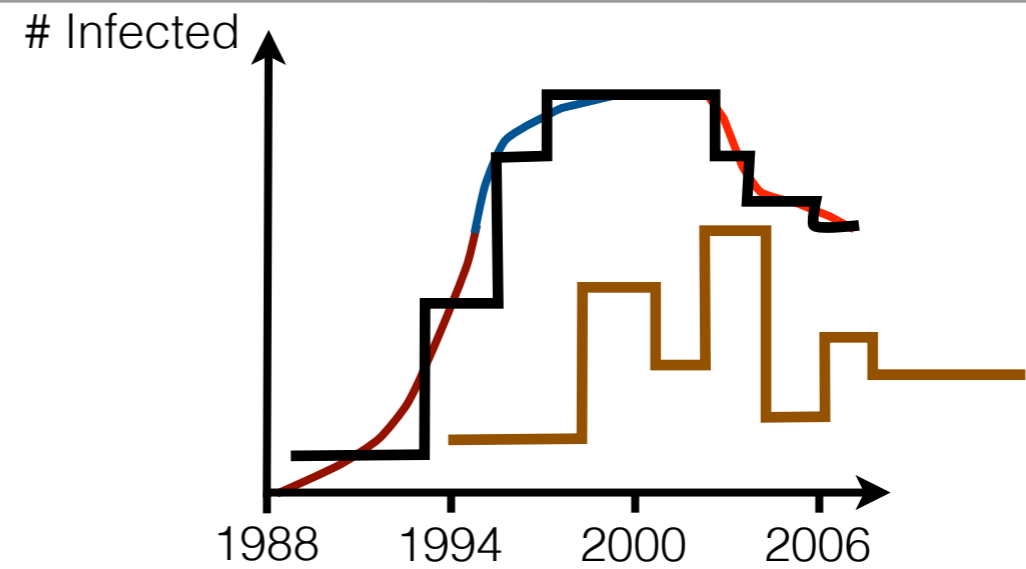
Piecewise constant  
population size



# Bayesian skyline plot relaxes constant growth rate

Assump-  
tion

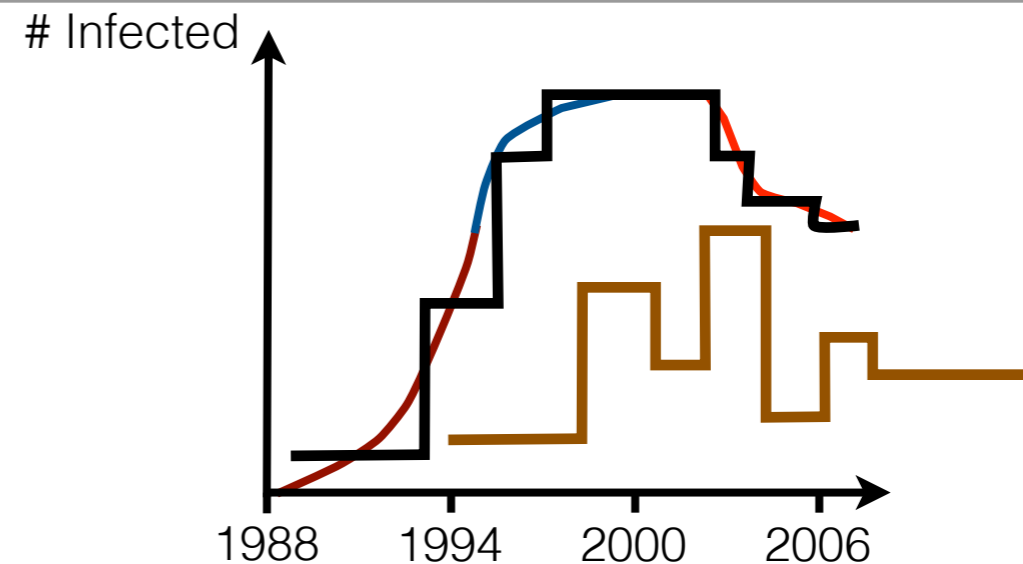
Piecewise constant  
population size



# Bayesian skyline plot relaxes constant growth rate

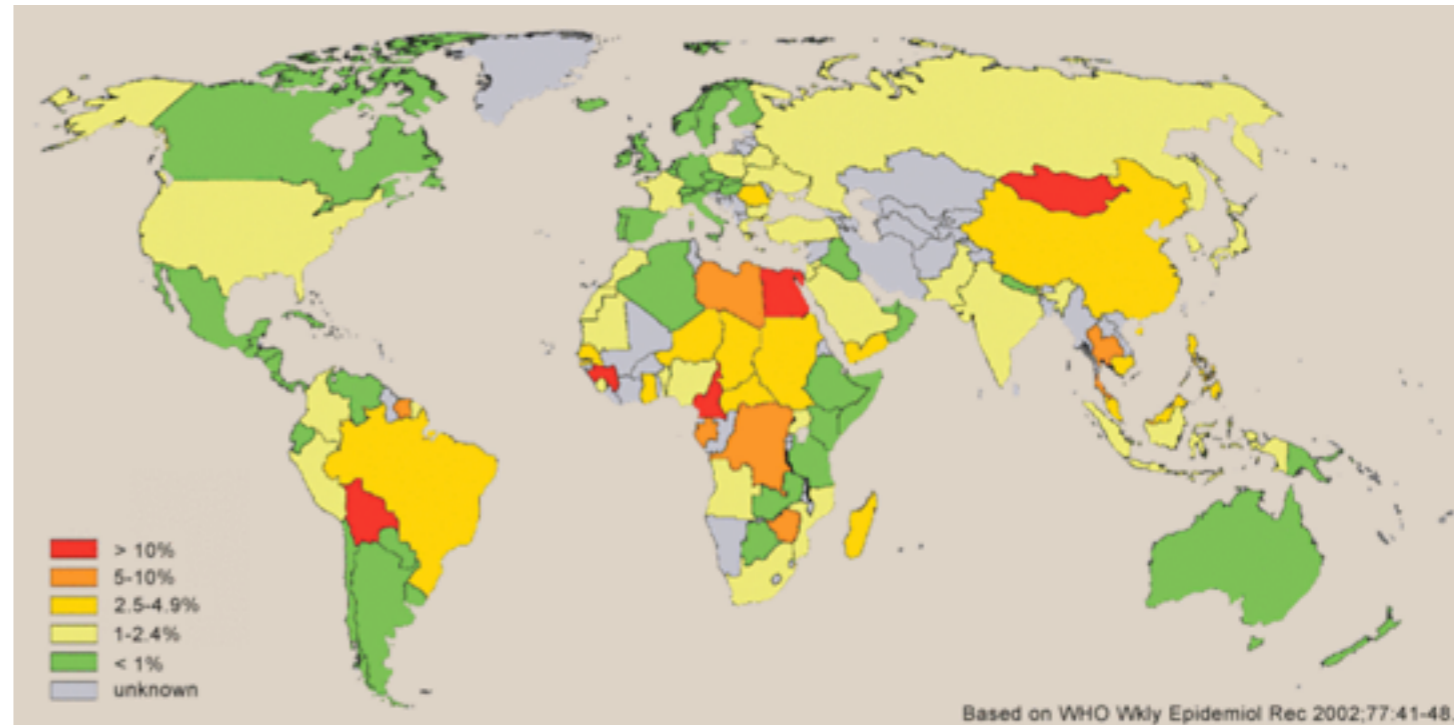
Assumption

Piecewise constant population size



HCV in Egypt

- ▶ Egypt highest HCV prevalence worldwide (about 13 %)
- ▶ Neighboring countries low prevalence
- ▶ When did the high prevalence emerge?
- ▶ Why?

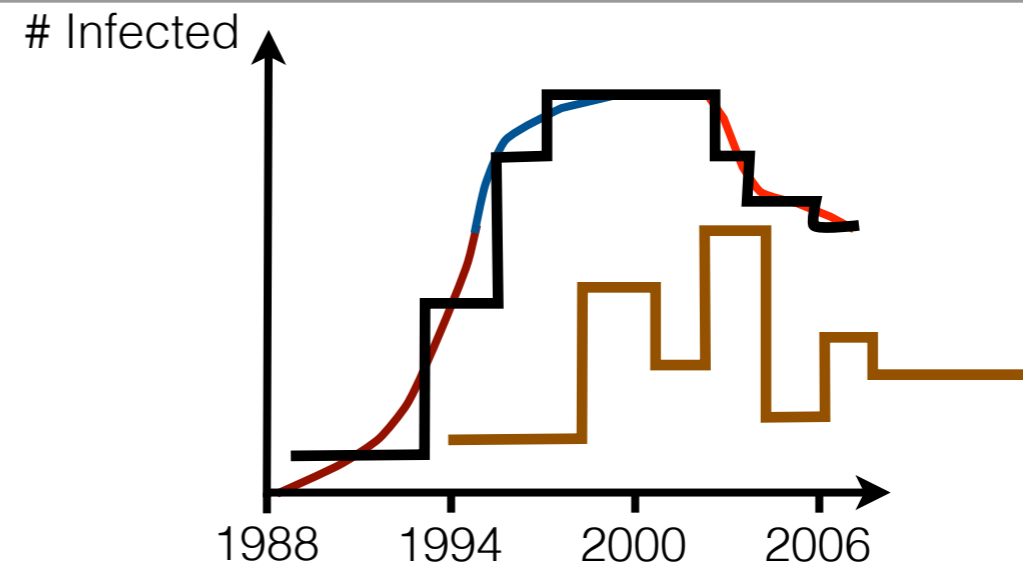




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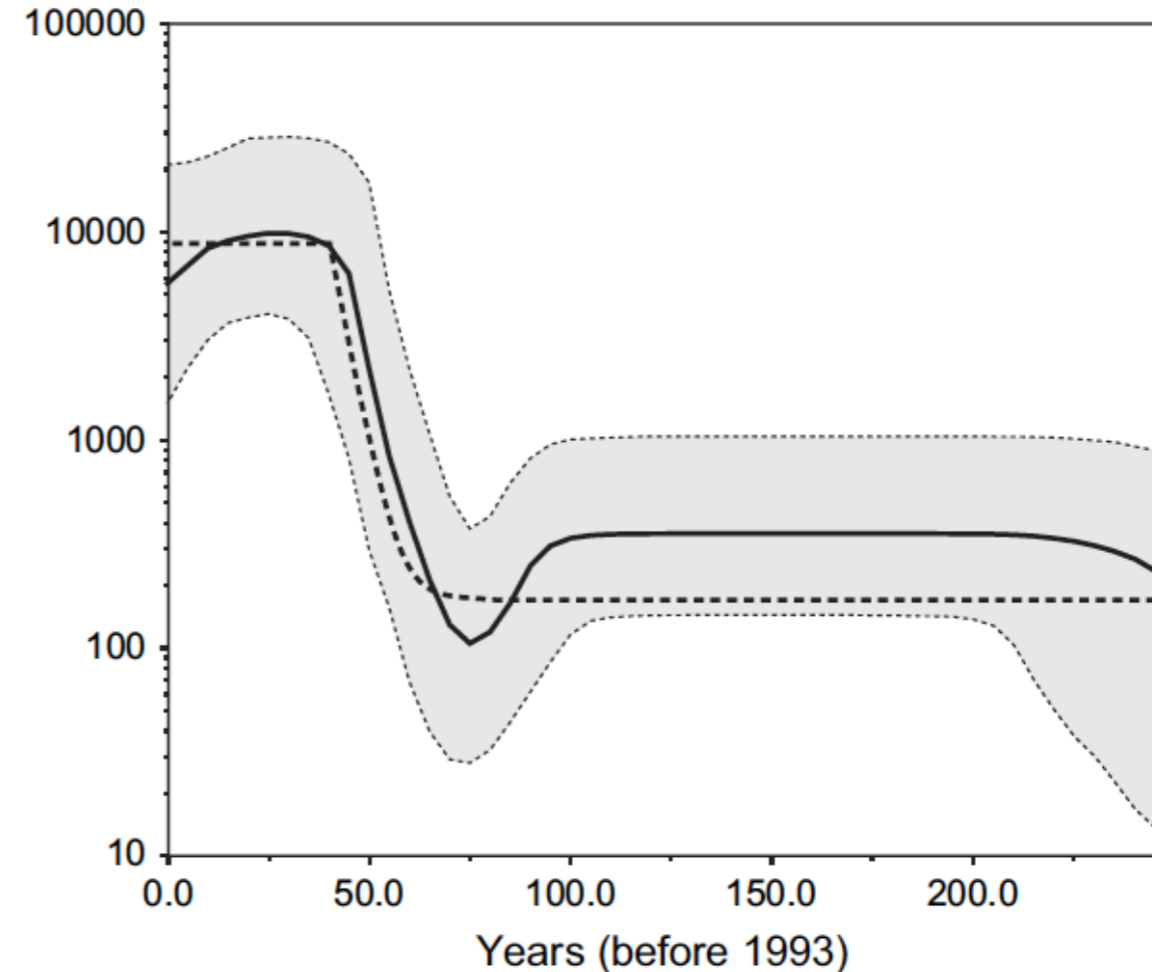
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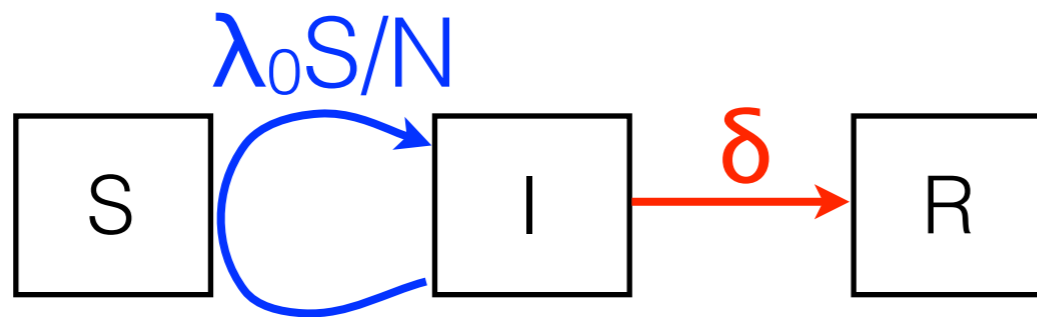
Coales-  
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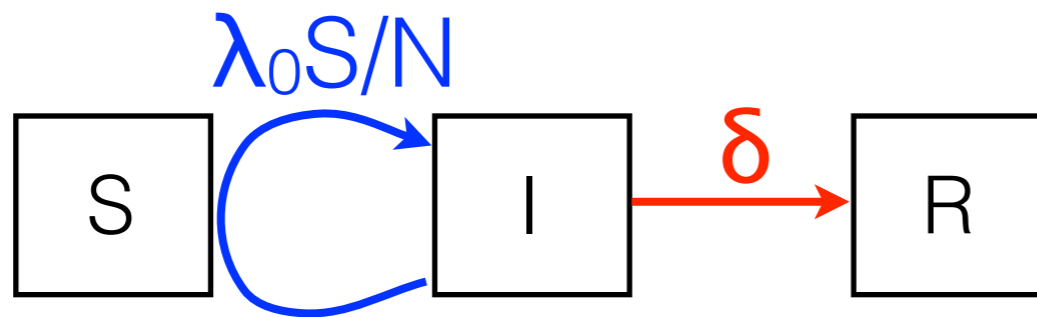


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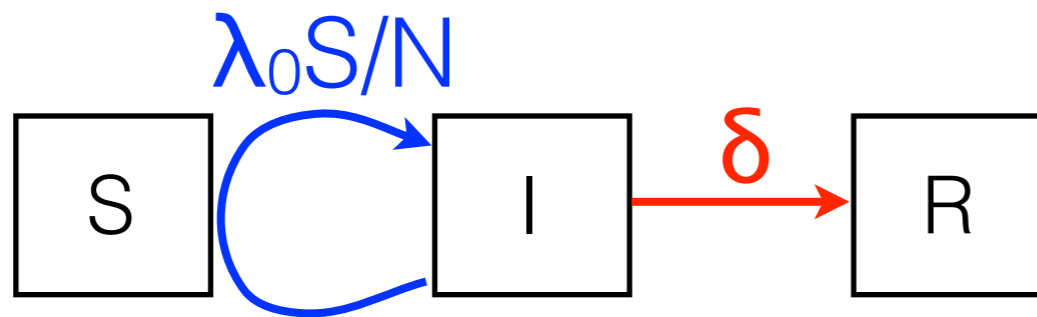
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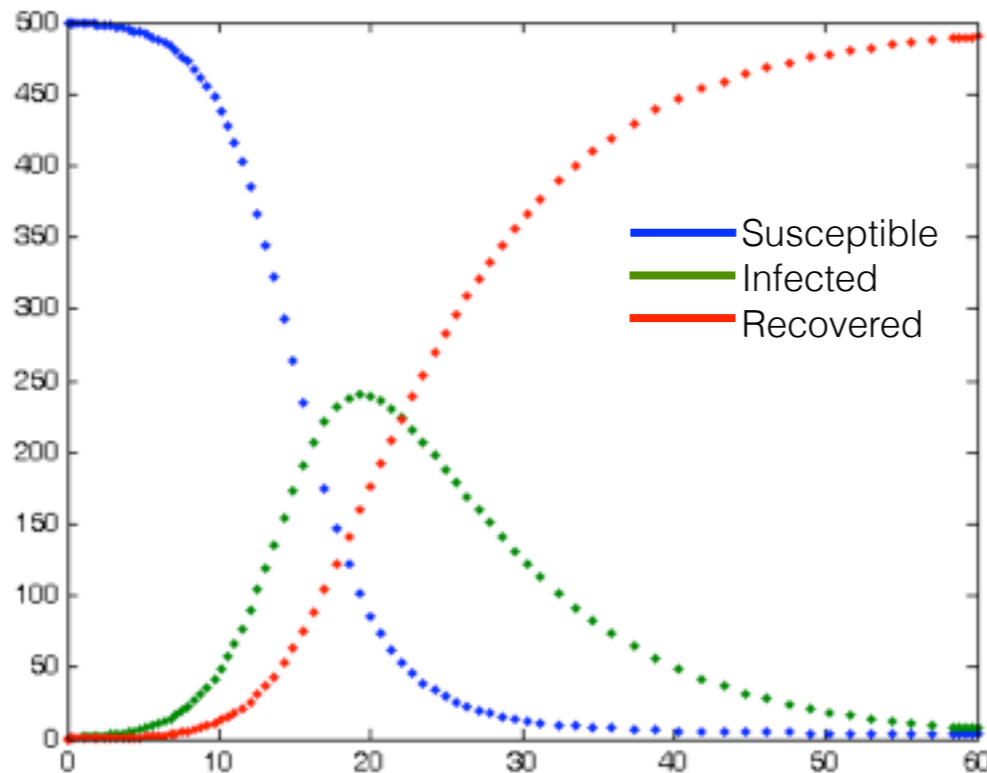
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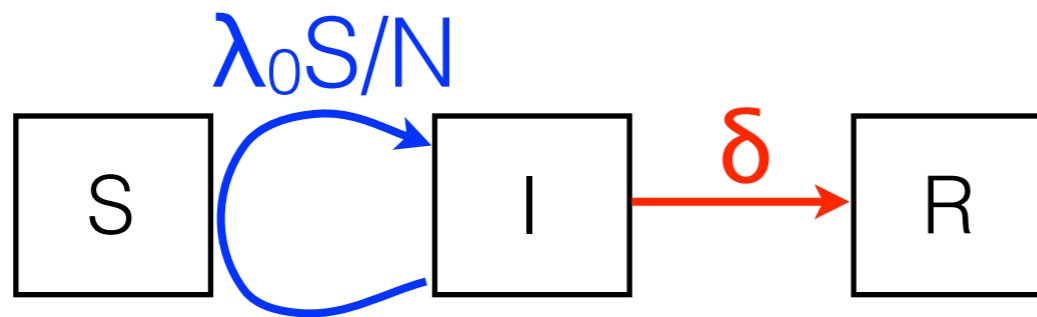
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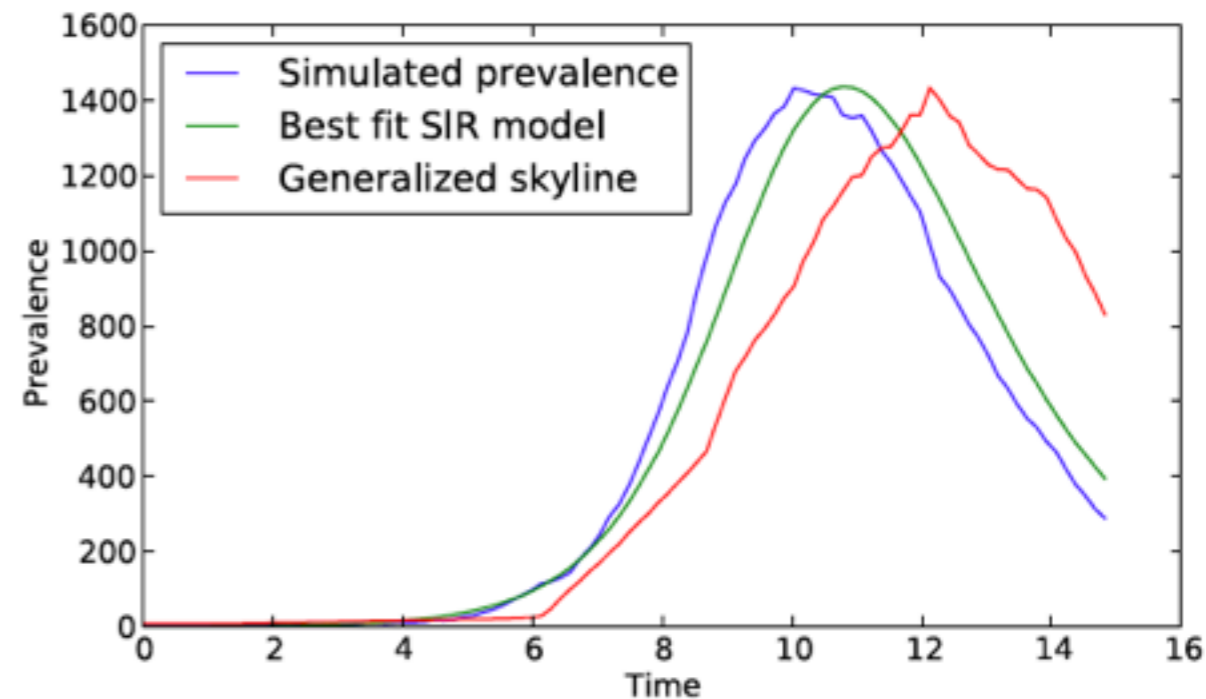
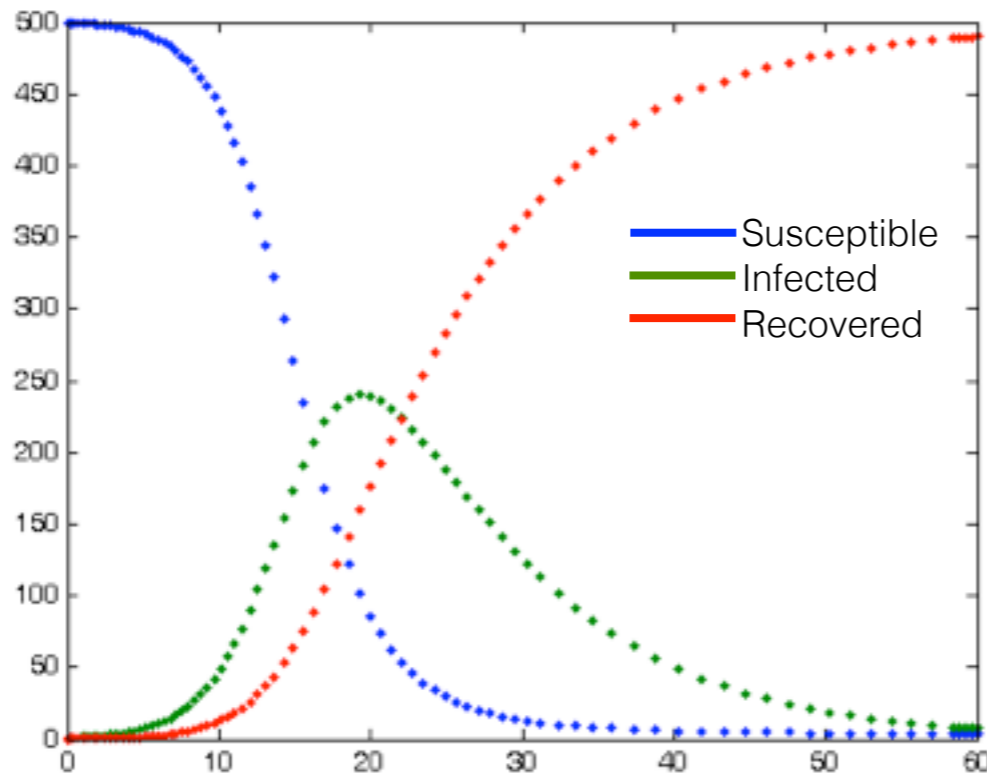
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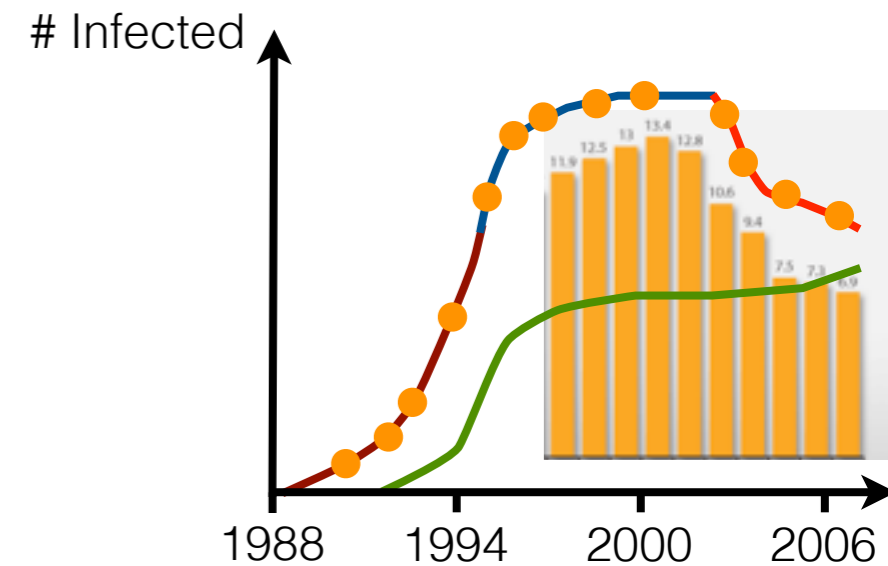
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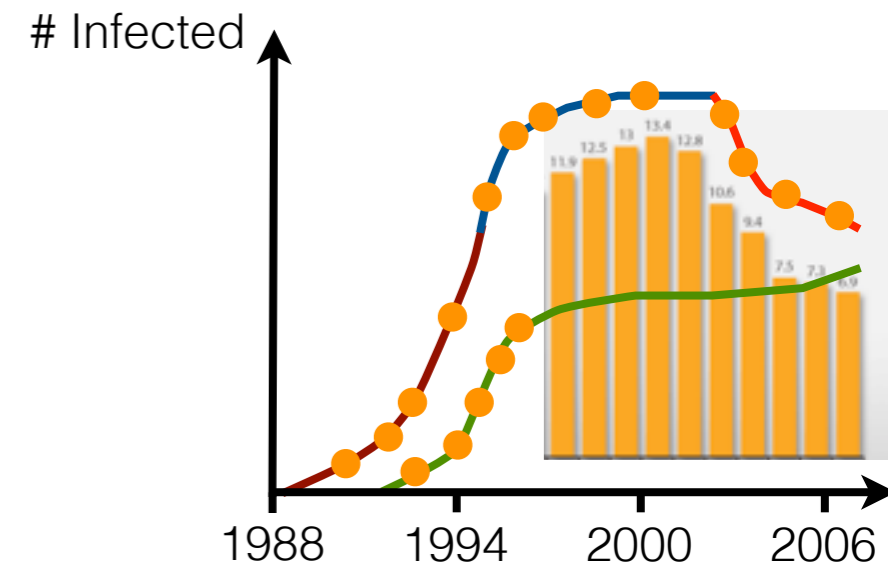
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1. ...for analyzing epidemic outbreaks
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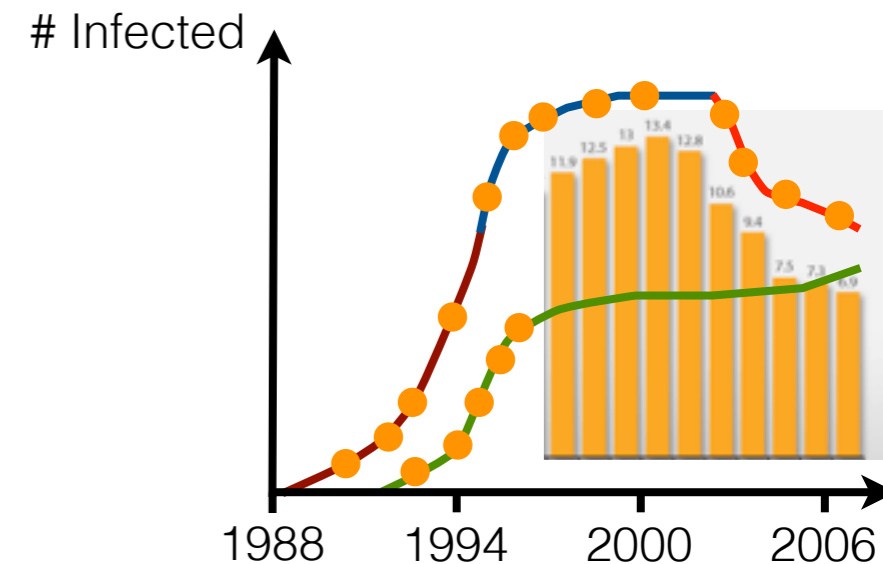
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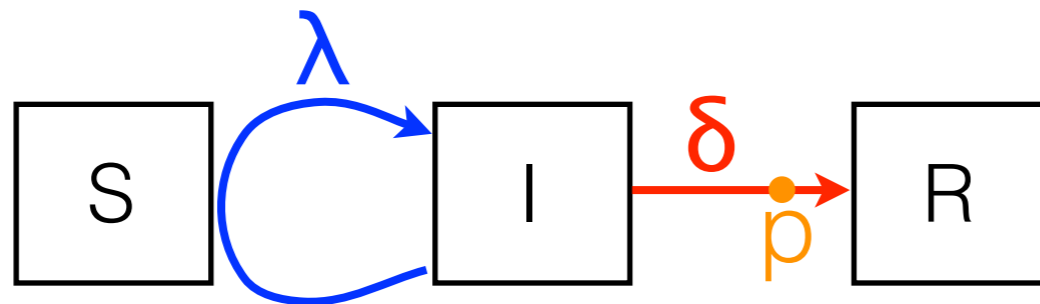
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# Part 2

## Birth-death model for transmission

Birth-death  
model



- transmission rate  $\lambda$
- “becoming-non-infectious” rate  $\delta$
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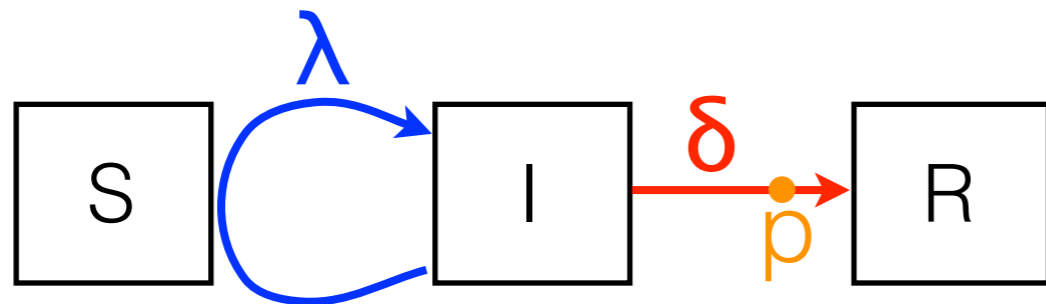
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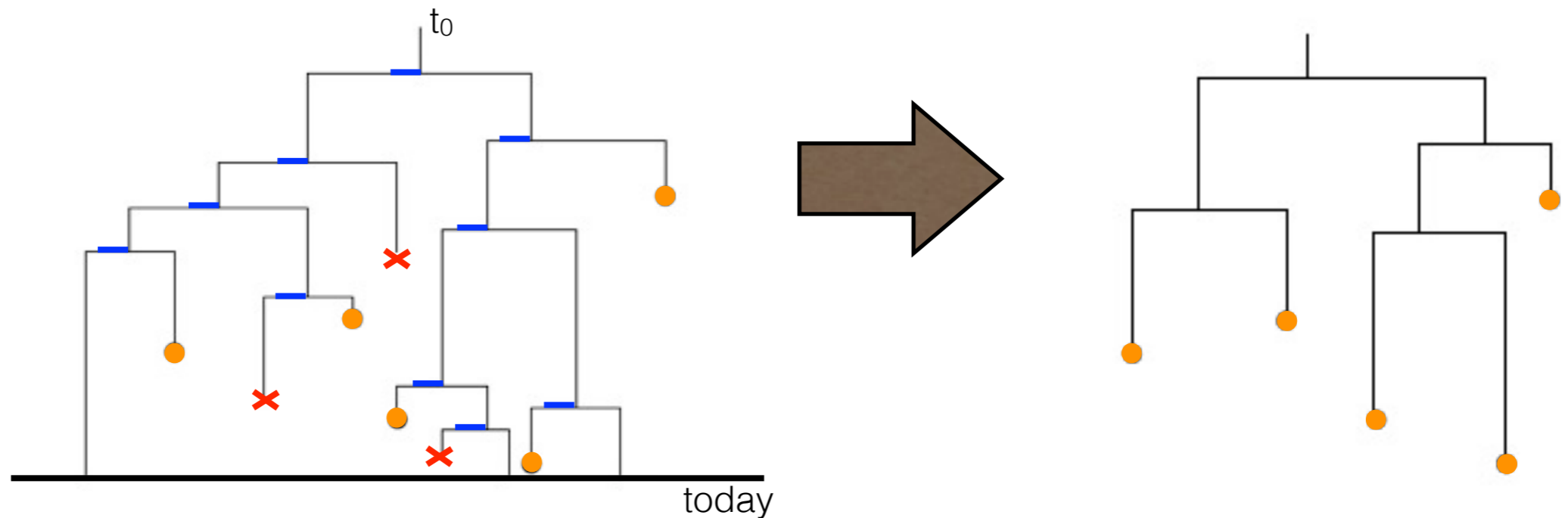


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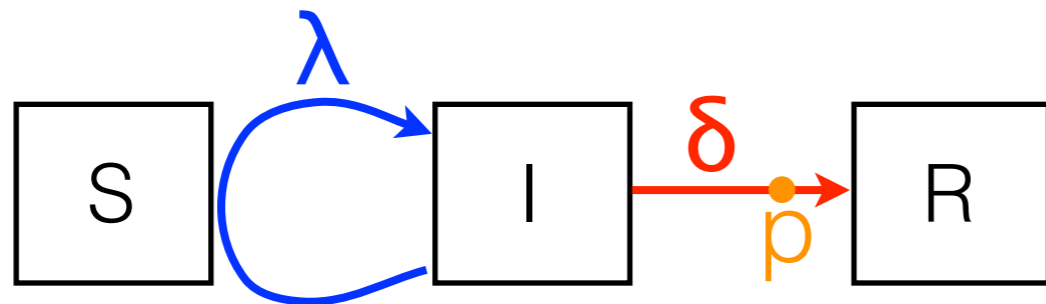
Phylogenetic trees



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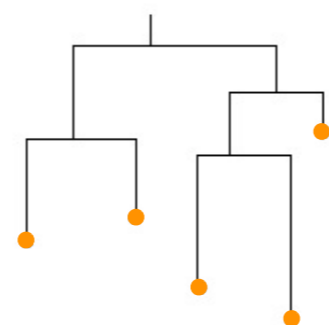
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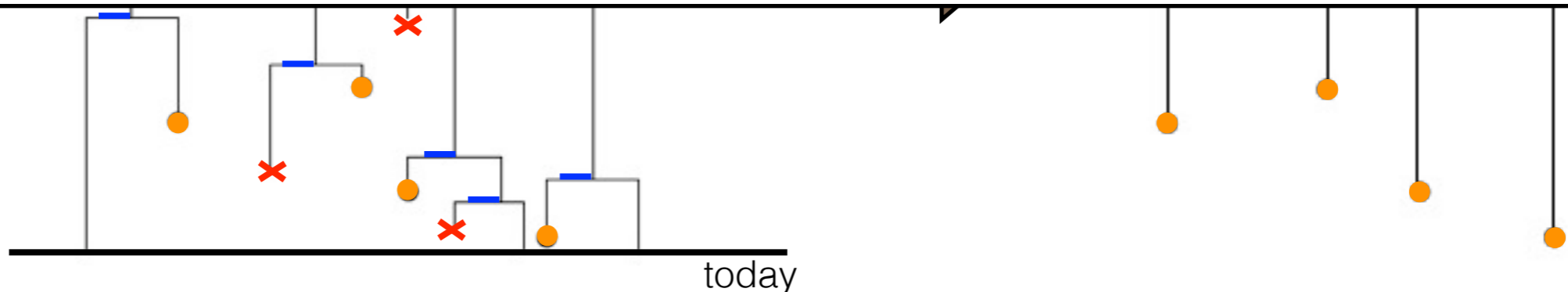
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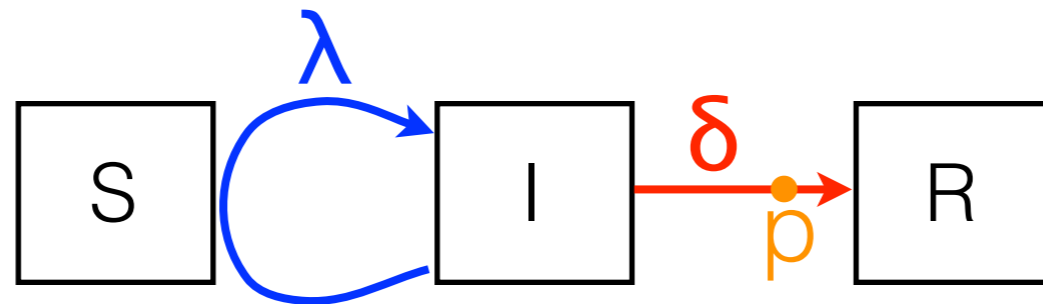
Lik (  ) ?

genetic trees



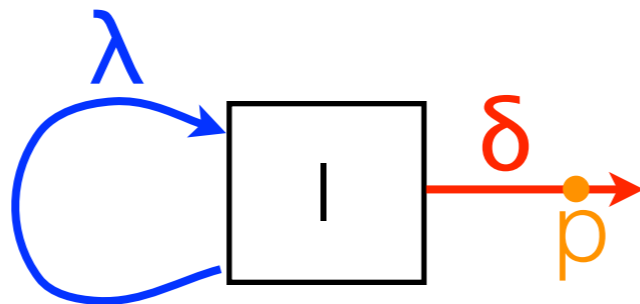
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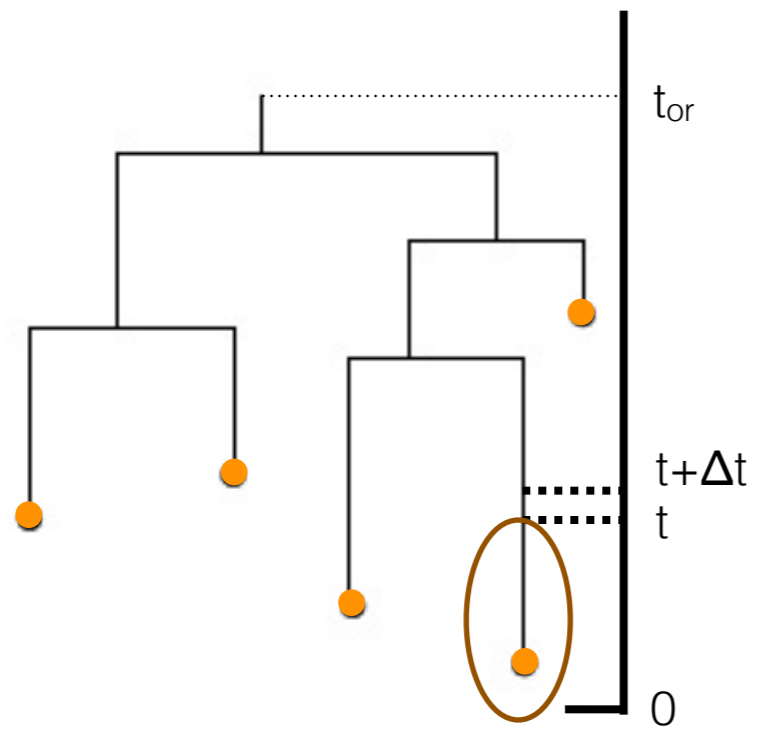
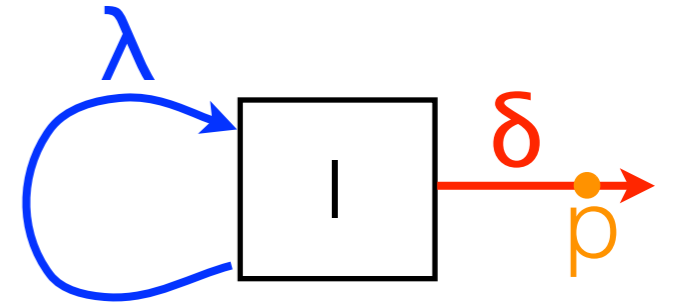


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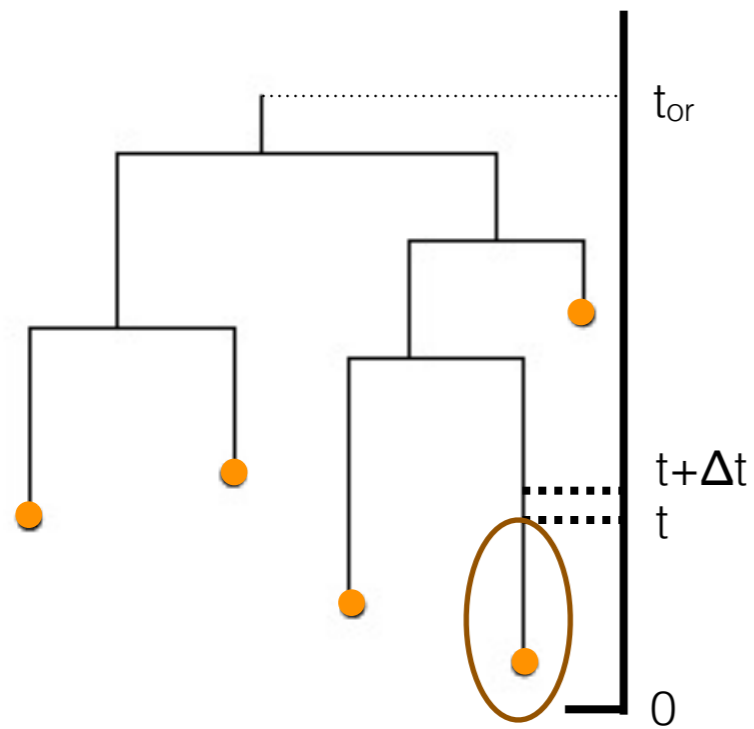
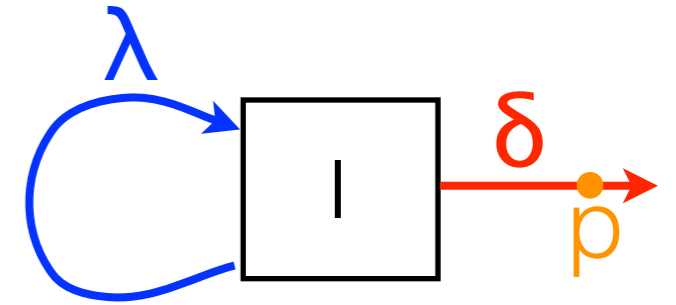
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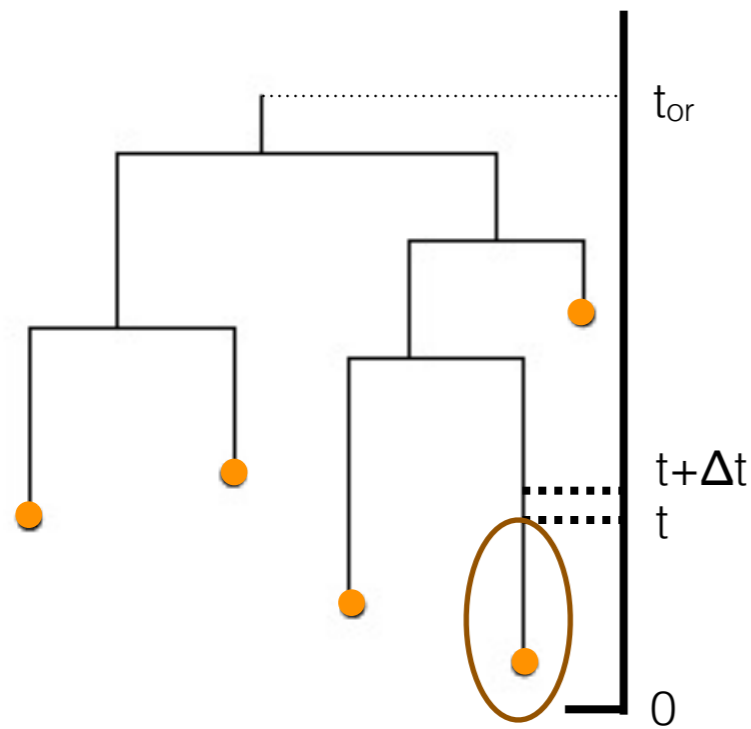
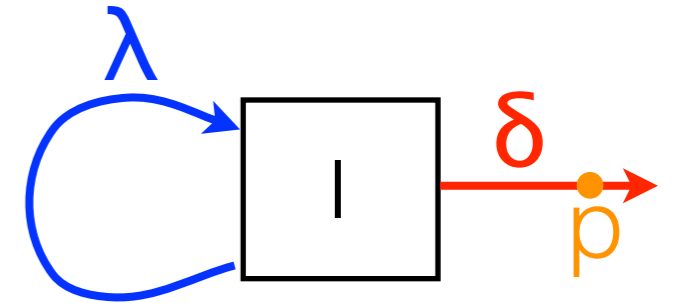
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$p(t)$ : probability density that a given individual at time  $t$  produces an descending tree as observed.



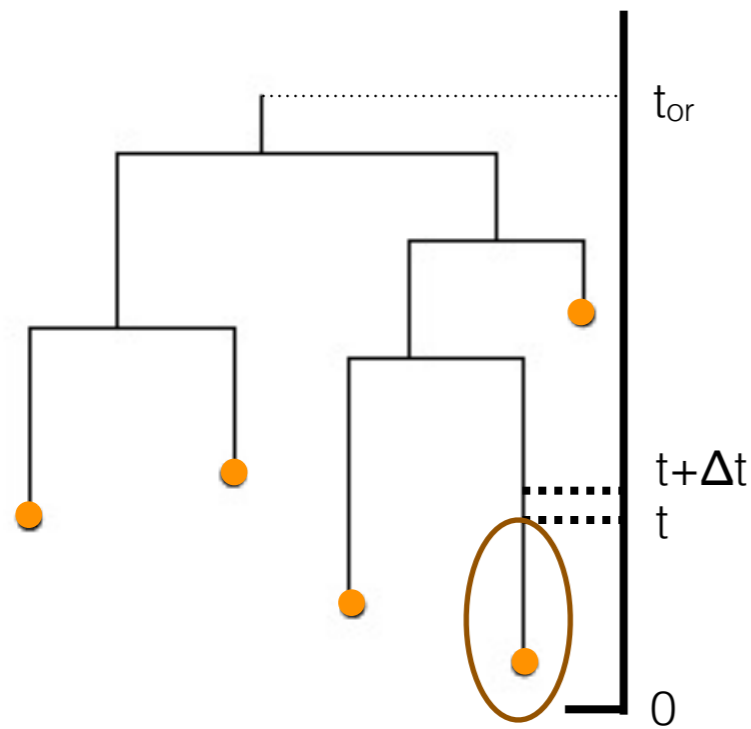
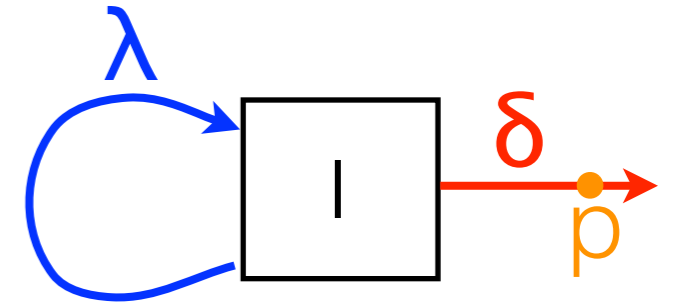
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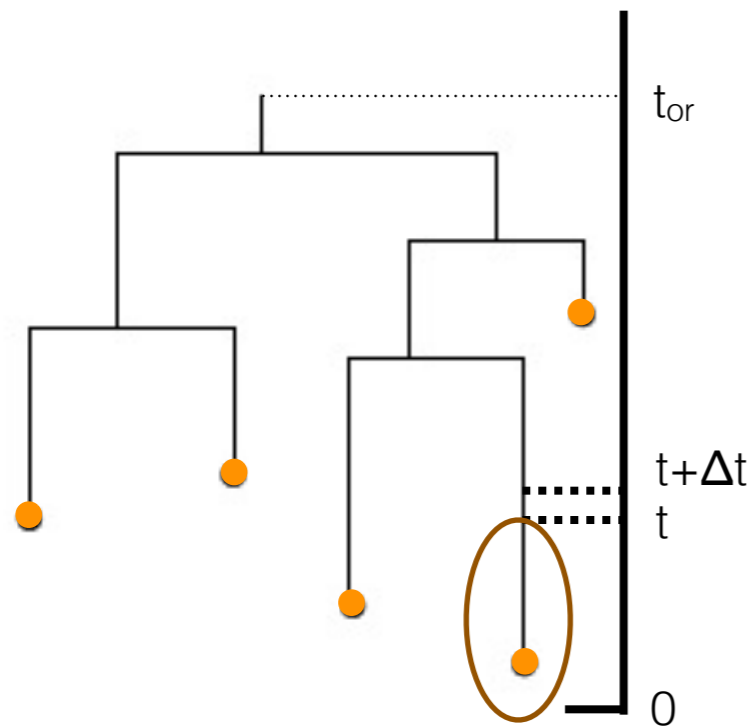
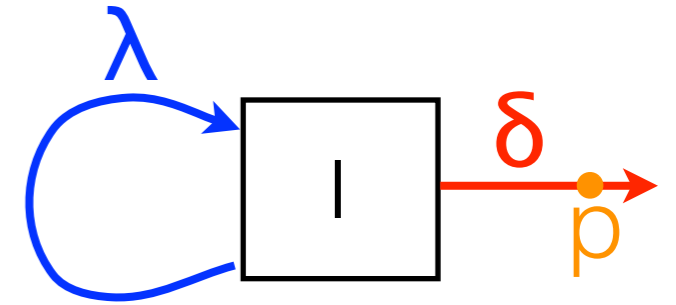


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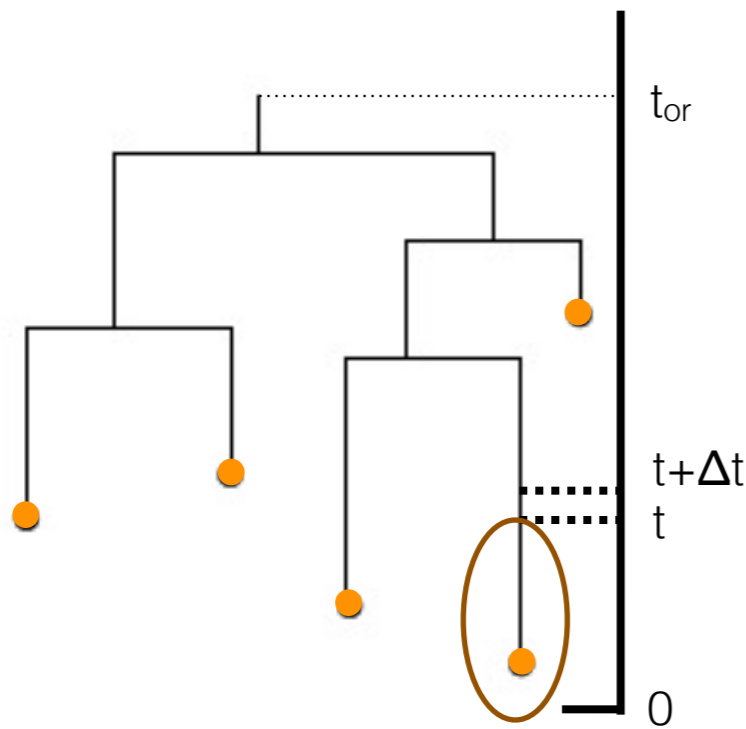
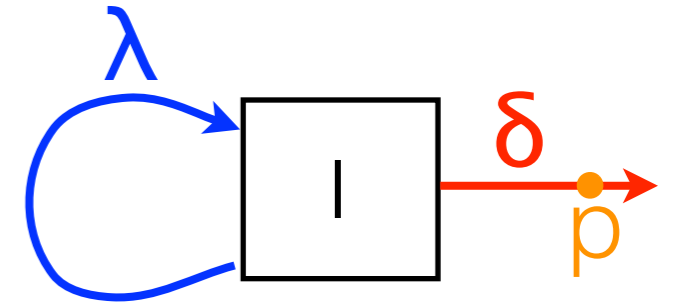
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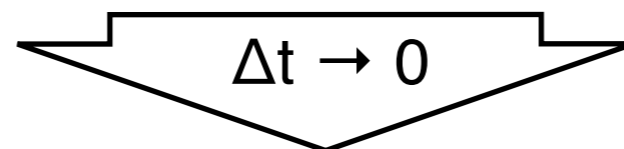


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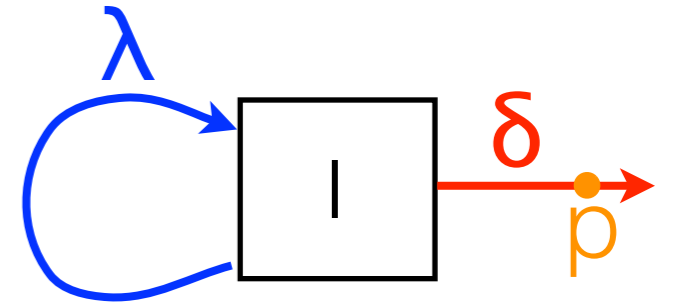
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$$\frac{d}{dt}p(t) = -(\lambda + \delta)p(t) + 2\lambda p_0(t)p(t)$$

# Tree likelihood



$$\text{Lik} \left( \begin{array}{c} \text{---} \\ | \\ \text{---} \\ | \quad | \\ \text{---} \quad \text{---} \\ | \quad | \quad | \quad | \\ \bullet \quad \bullet \quad \bullet \quad \bullet \end{array} \right) = \lambda^{m-1} \prod_{i=0}^{m-1} \frac{1}{q(x_i)} \prod_{i=1}^m p \delta q(y_i)$$

where

$$q(t) = 2(1 - c_2^2) + e^{-c_1 t} (1 - c_2)^2 + e^{c_1 t} (1 + c_2)^2$$

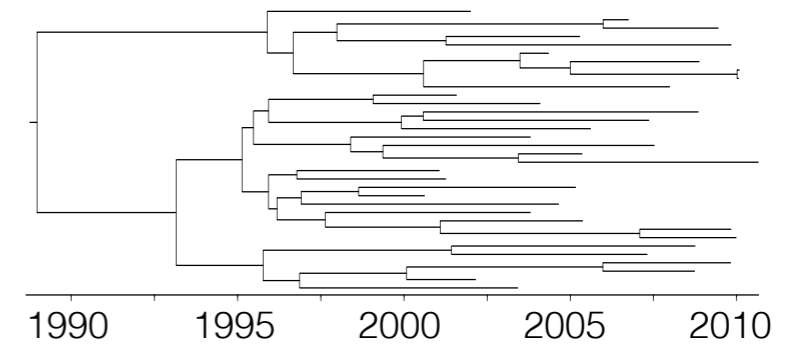
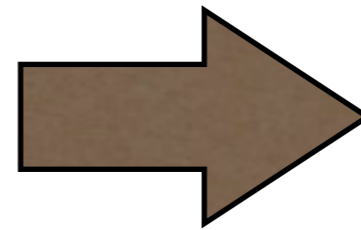
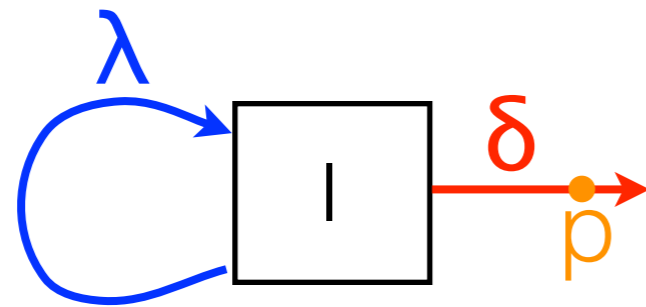
$$c_1 = |\sqrt{(\lambda - \delta)^2 + 4p\lambda\delta}|$$

$$c_2 = -\frac{\lambda - \delta}{c_1}$$

and  $x_i$  branching times,  $y_i$  sampling times.

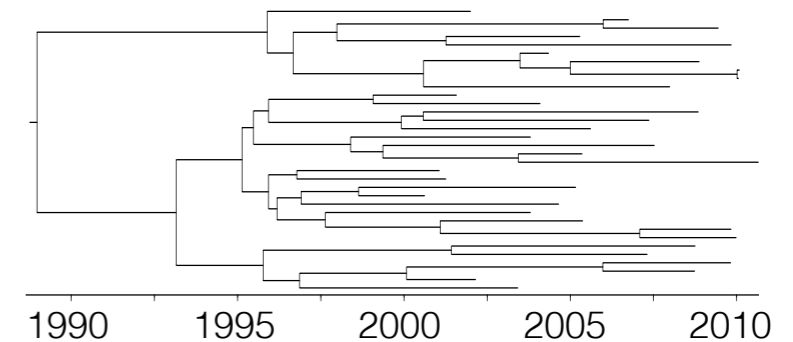
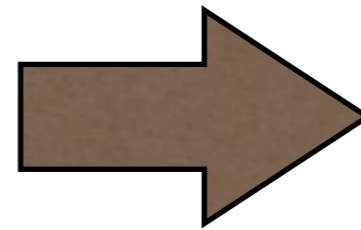
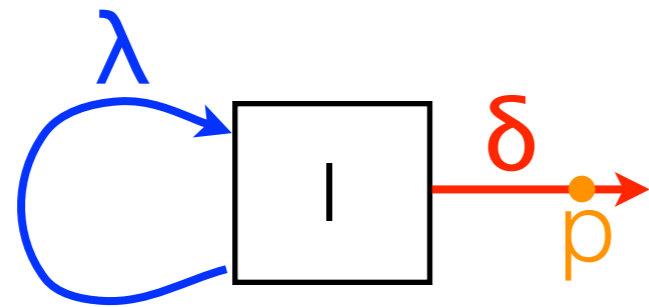
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Simulating  
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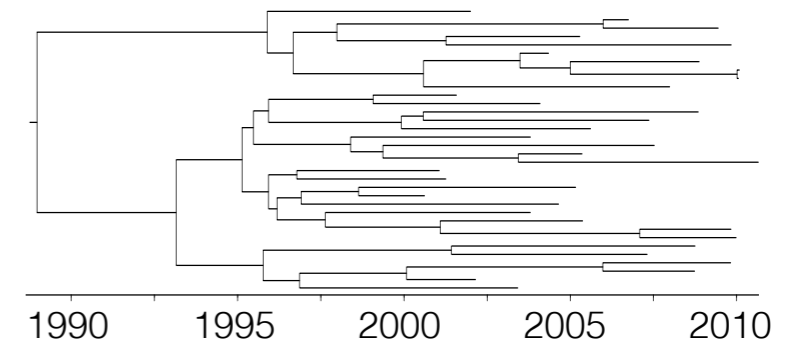
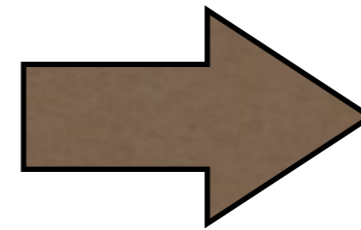
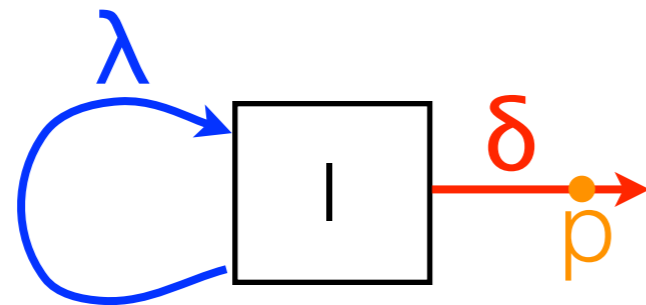
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# Simulation study: Comparing exact method to coalescent

Simulating epidemic outbreak



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Coalescent approximation

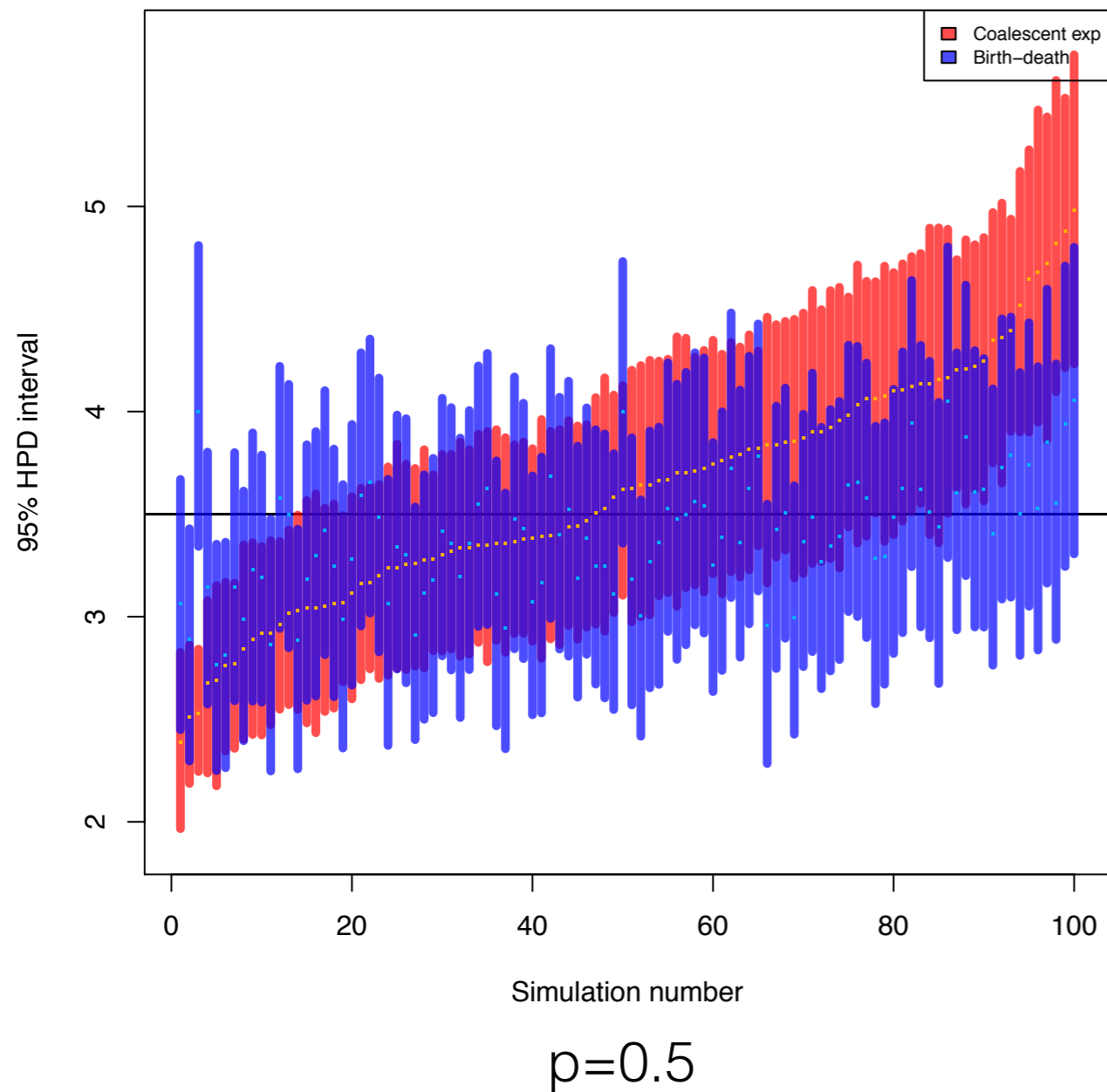
Parameterizes deterministic population size growth

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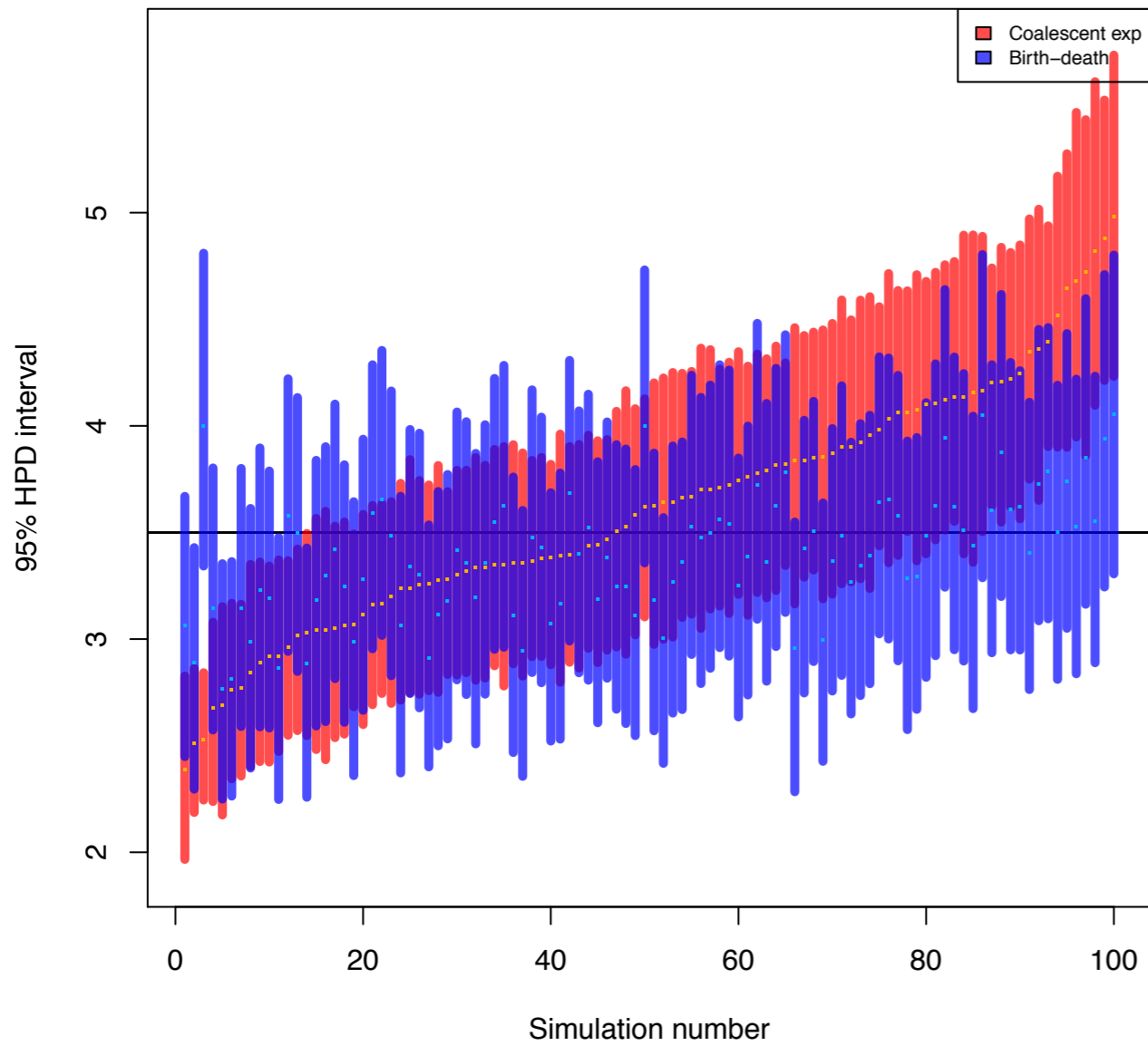
# Simulating birth-death trees

95% HPD growth rate interval



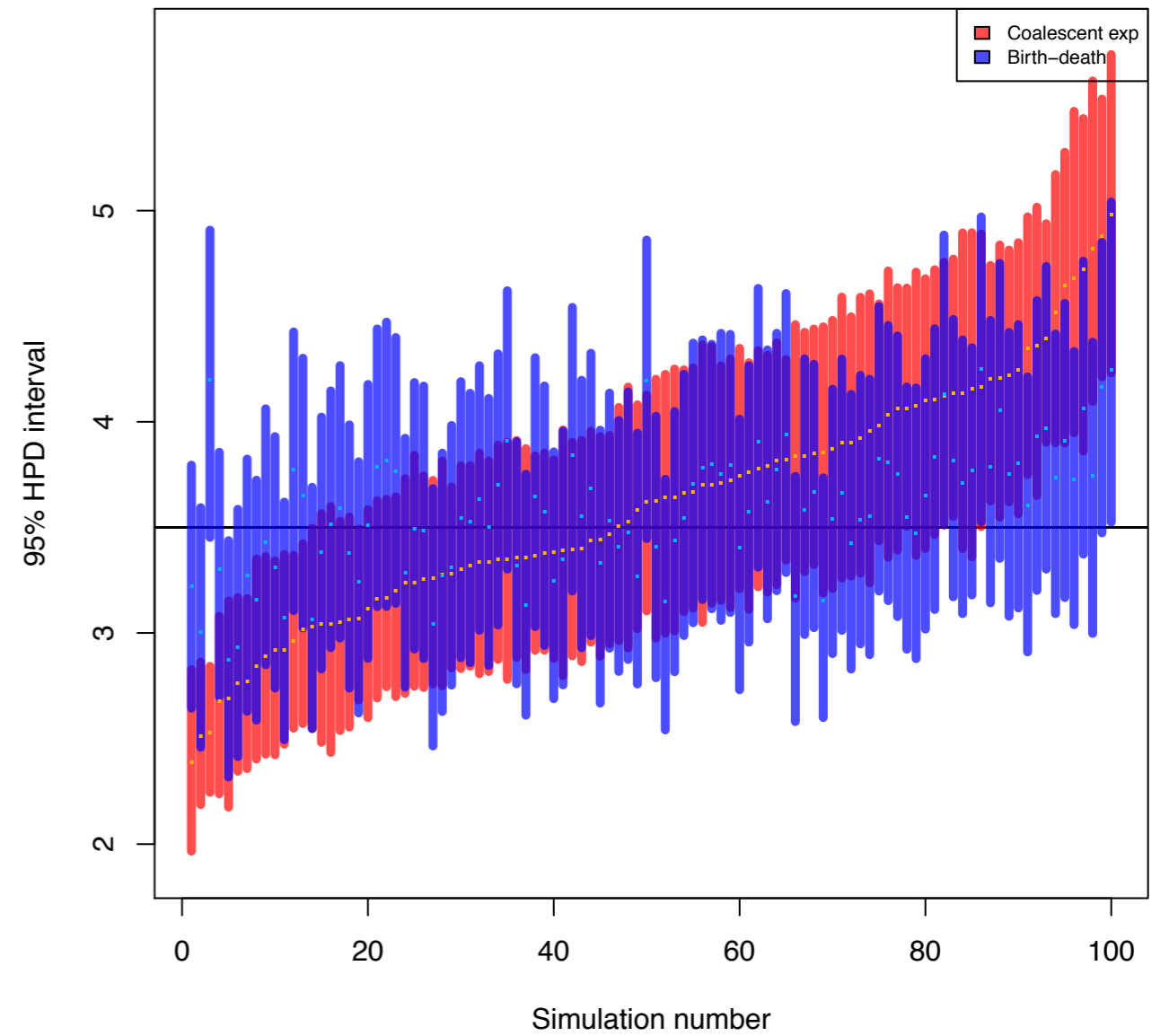
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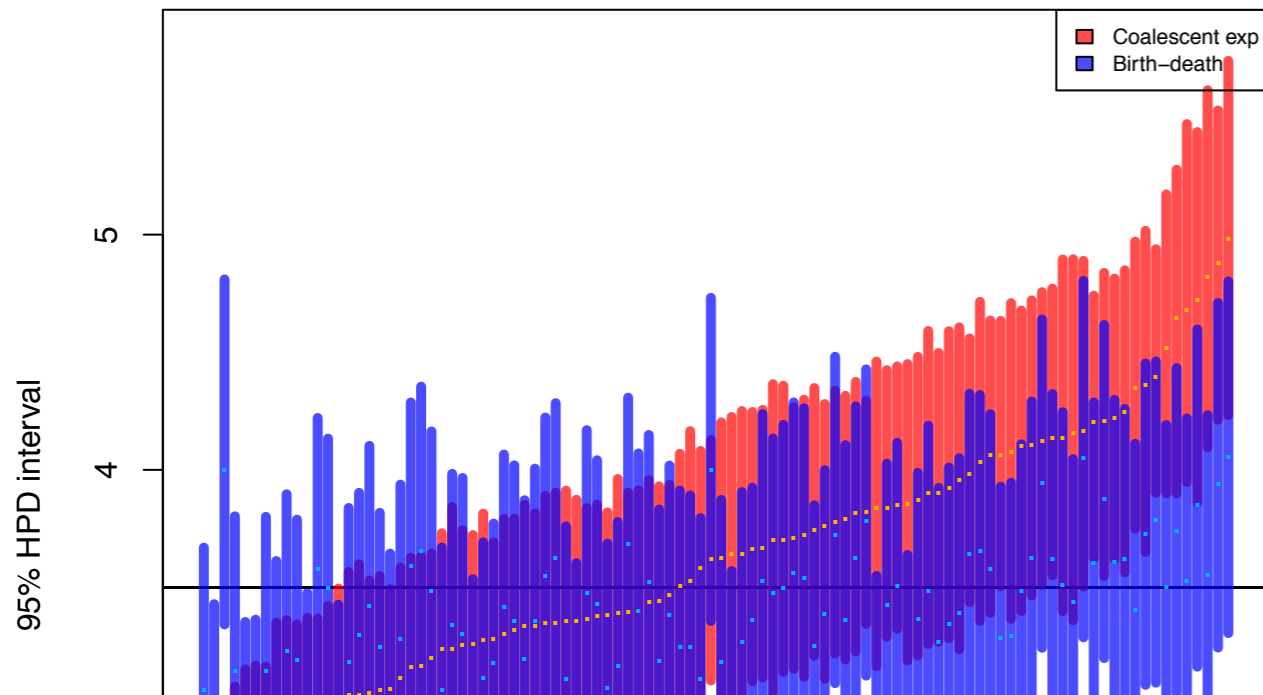
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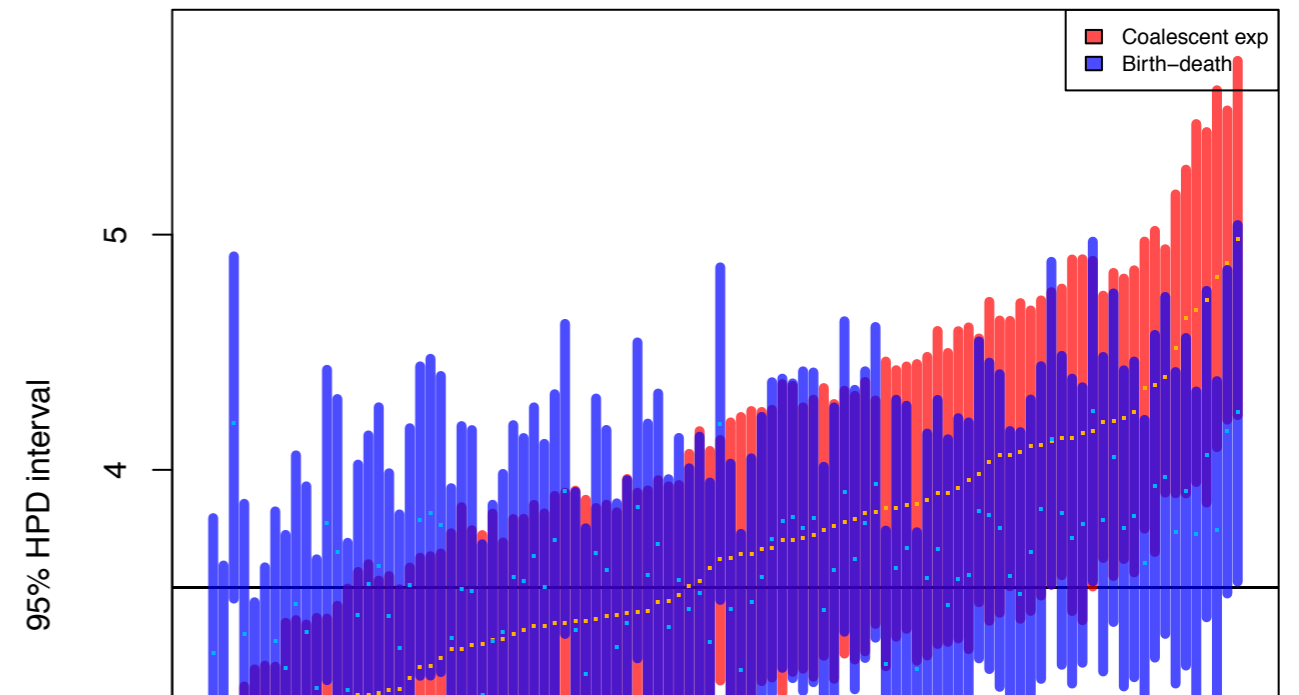
$p=0.01$

# Simulating birth-death trees

95% HPD growth rate interval



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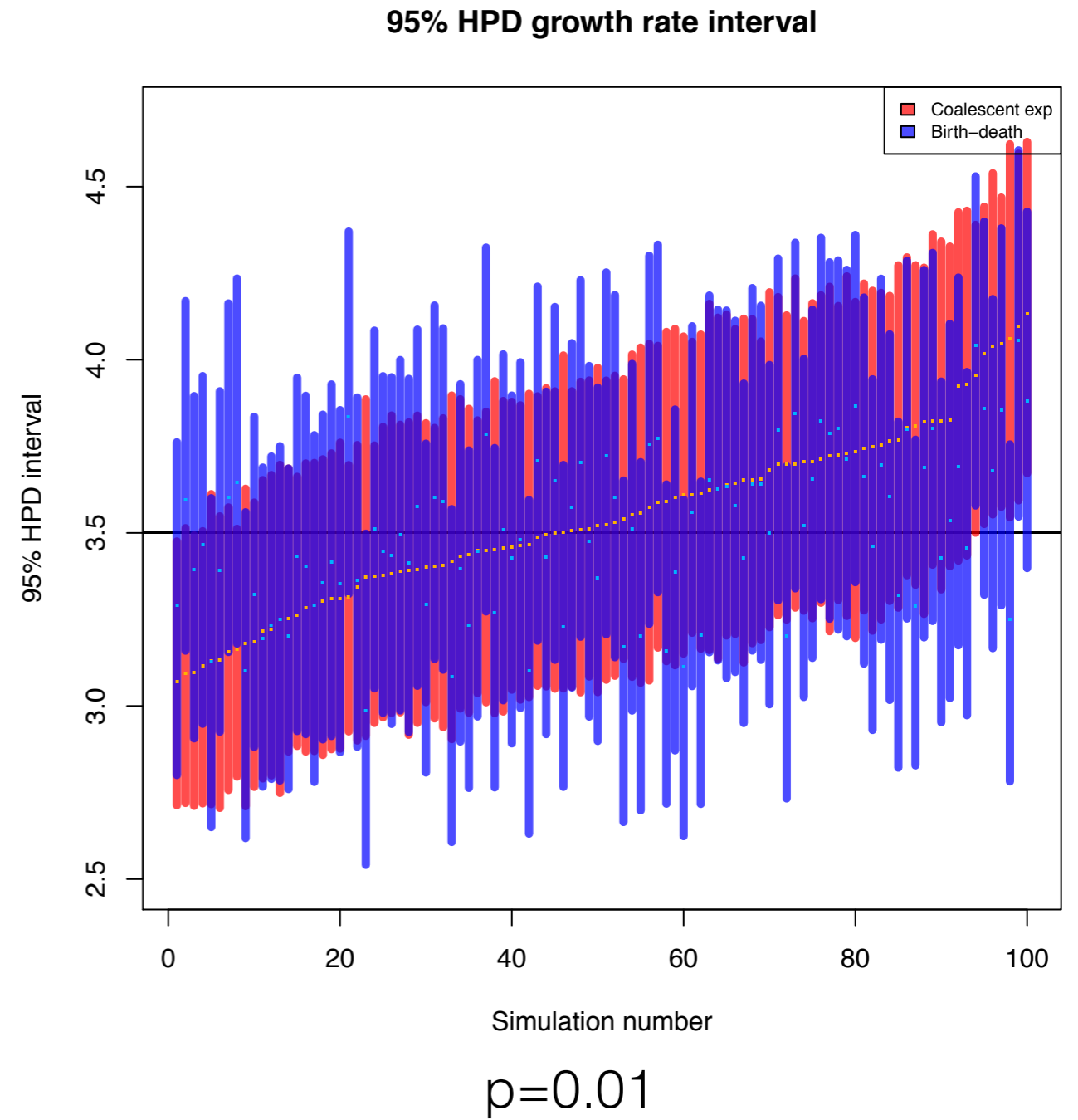
Reason for biases in coalescent?

- ▶ Coalescent overconfident also in case of rare sampling (small  $p$ )
- ▶ Thus deterministic population size in coalescent problematic?

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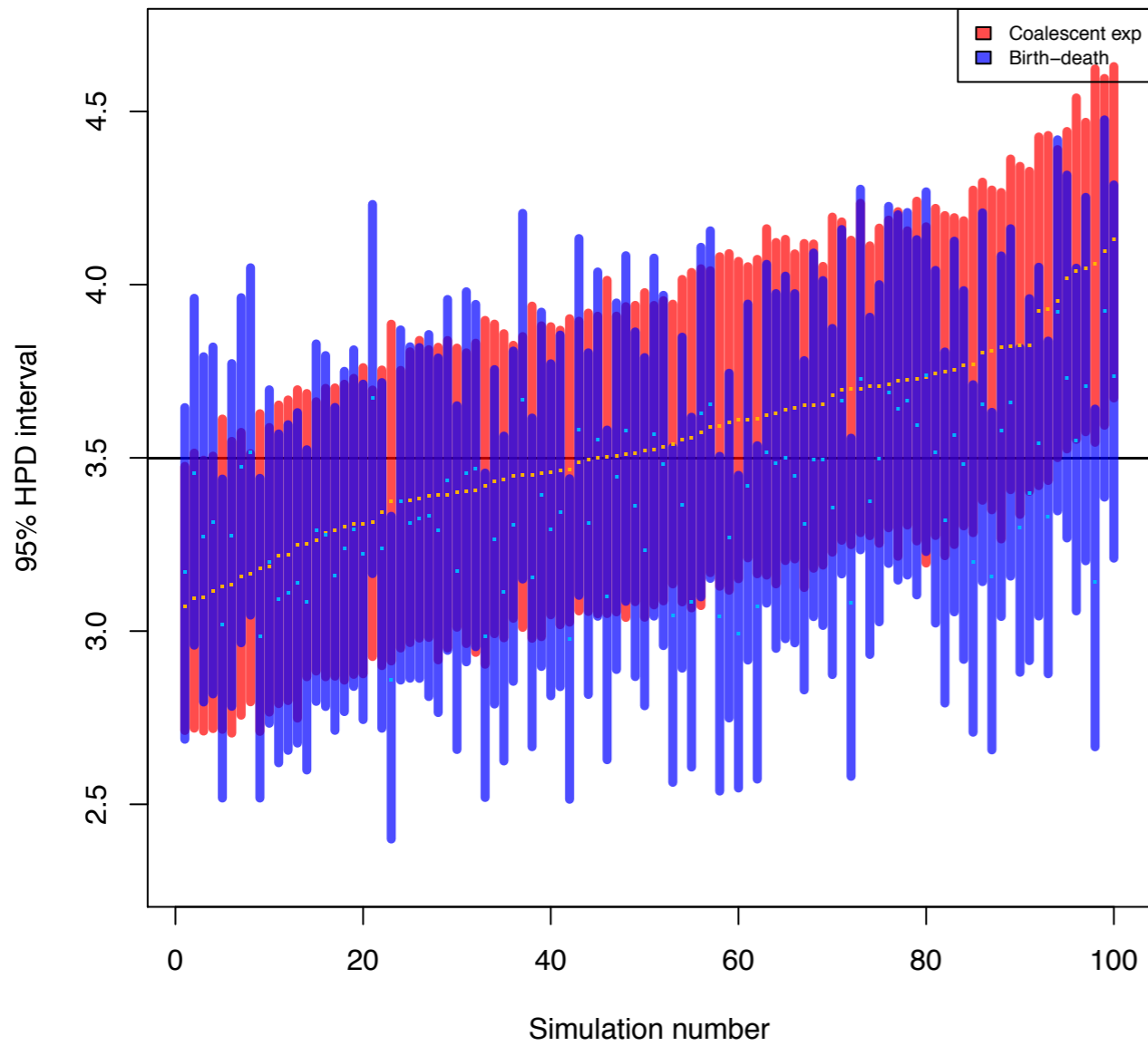
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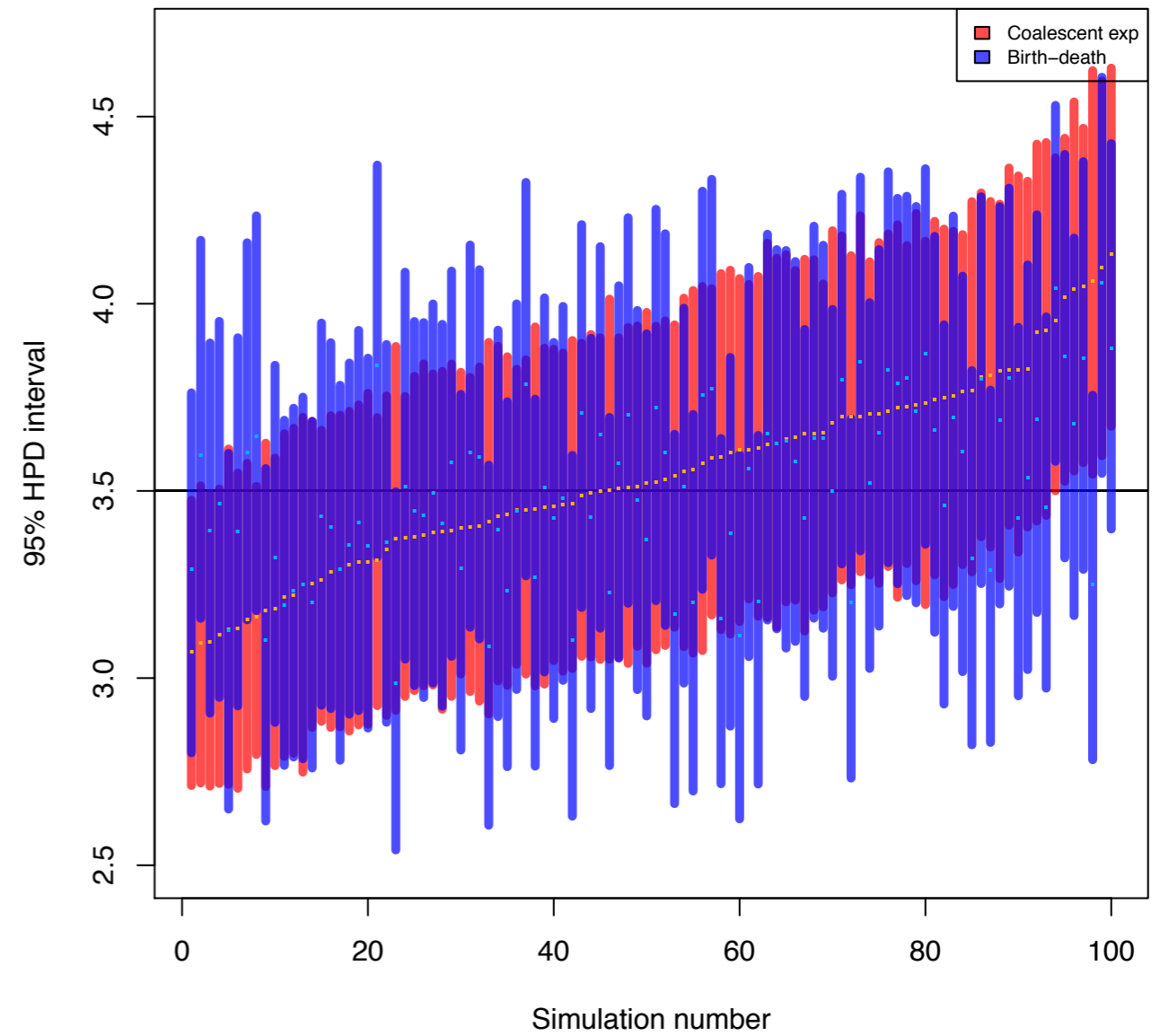
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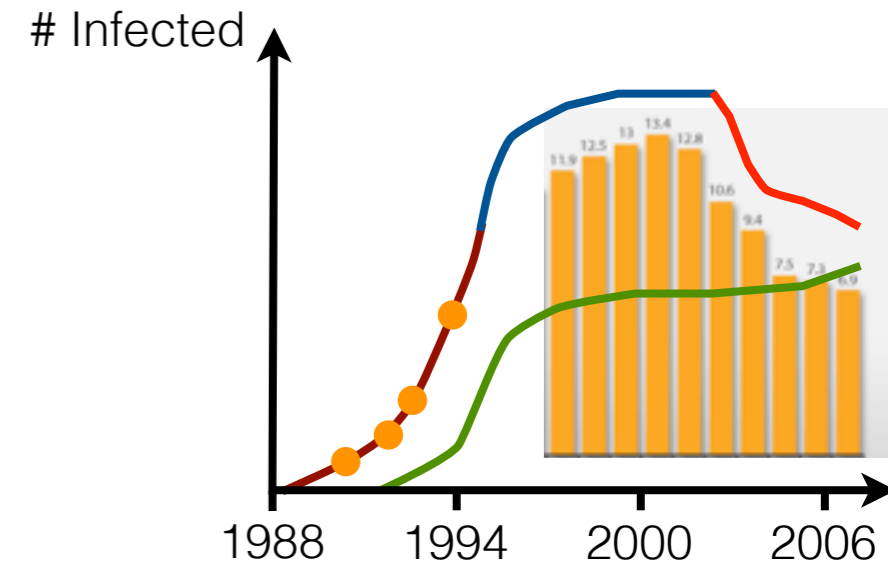
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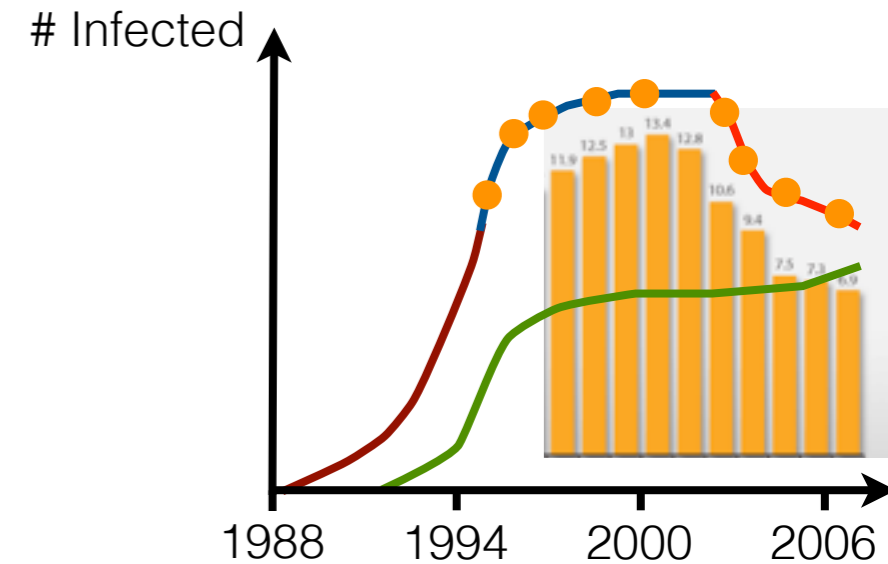
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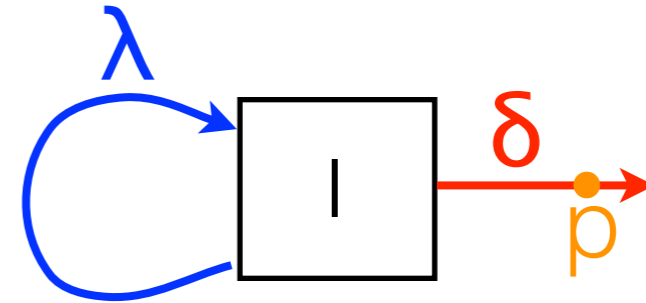
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# Birth-death-skyline plot

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Epidemiological rates may change through time:

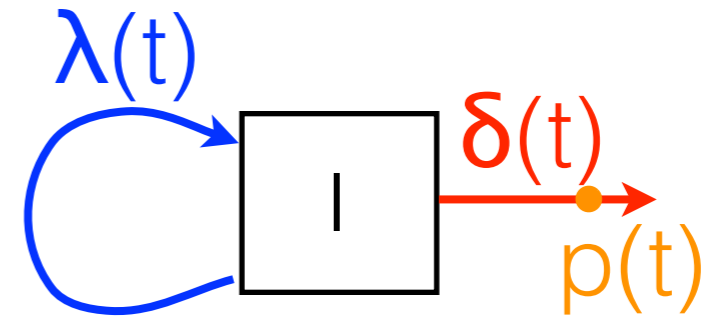




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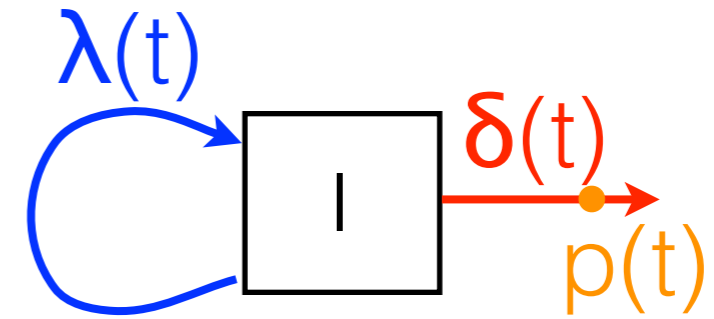
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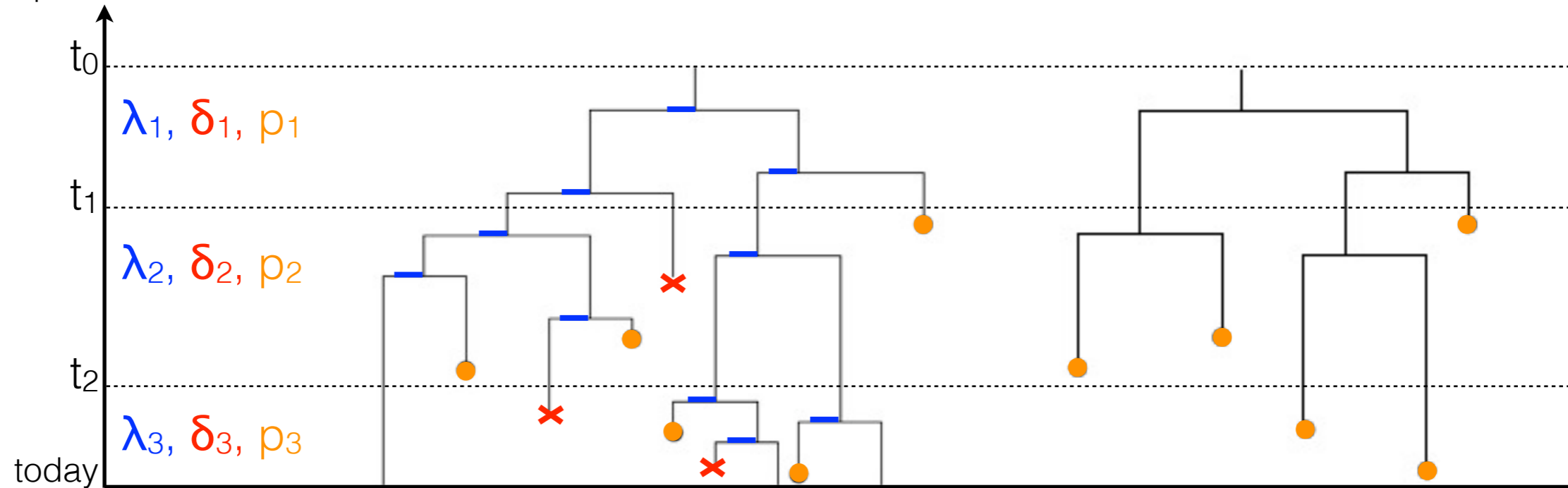


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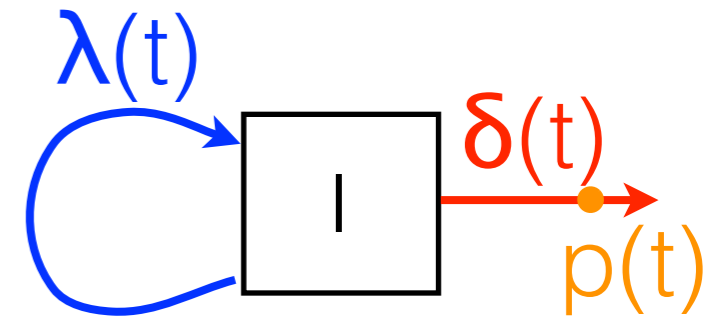
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Time in past



# Hepatitis C virus in Egypt

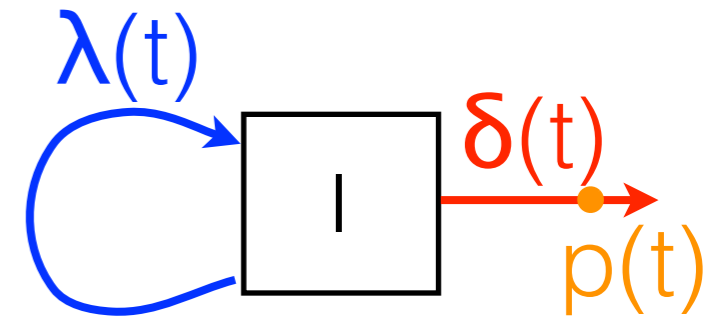


Effective reproductive number  **$R_e(t)$**

generalizes

Basic reproductive number  **$R_0 = R_e(0)$**

# Hepatitis C virus in Egypt



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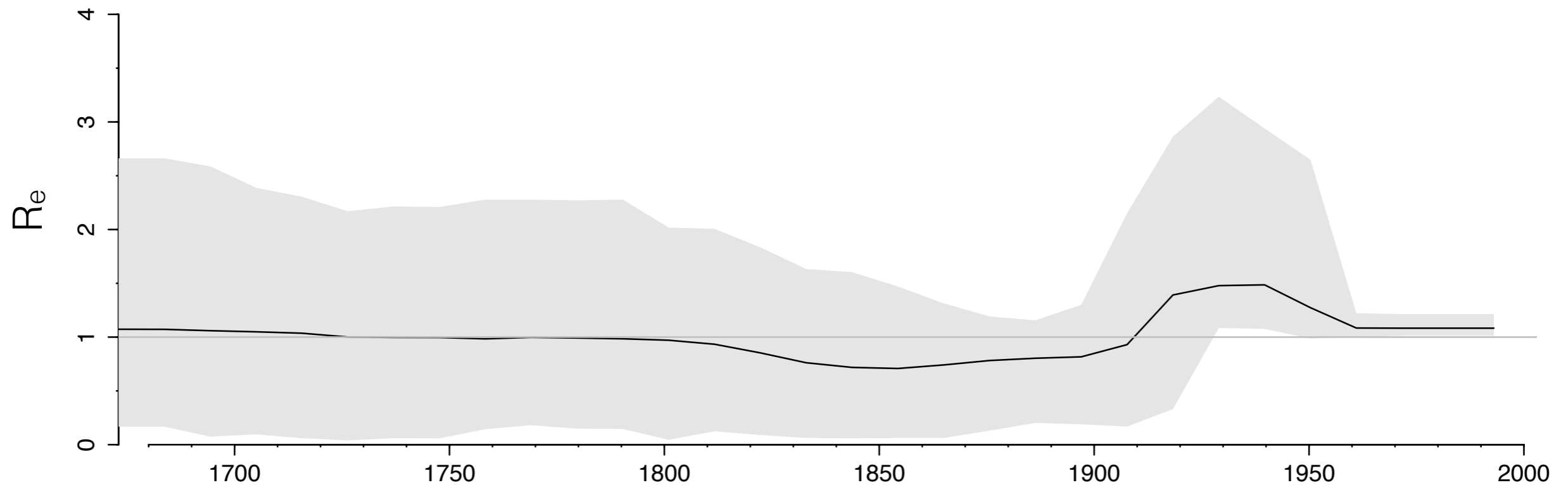
Basic reproductive number  $R_0 = R_e(0)$

Analysis of 63 seq:

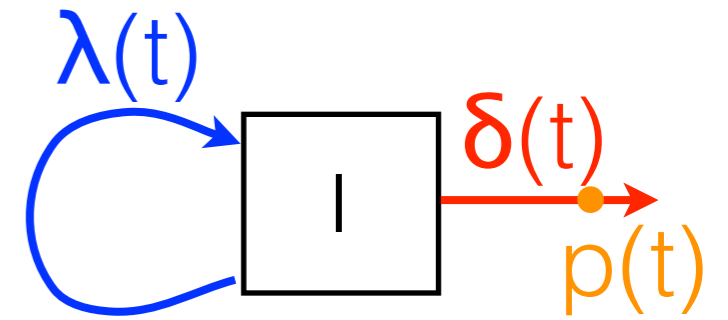
$$R_e(t) = \lambda(t)/\delta(t)$$

— median

■ 95% HPD interval



# Hepatitis C virus in Egypt



Effective reproductive number  $R_e(t)$

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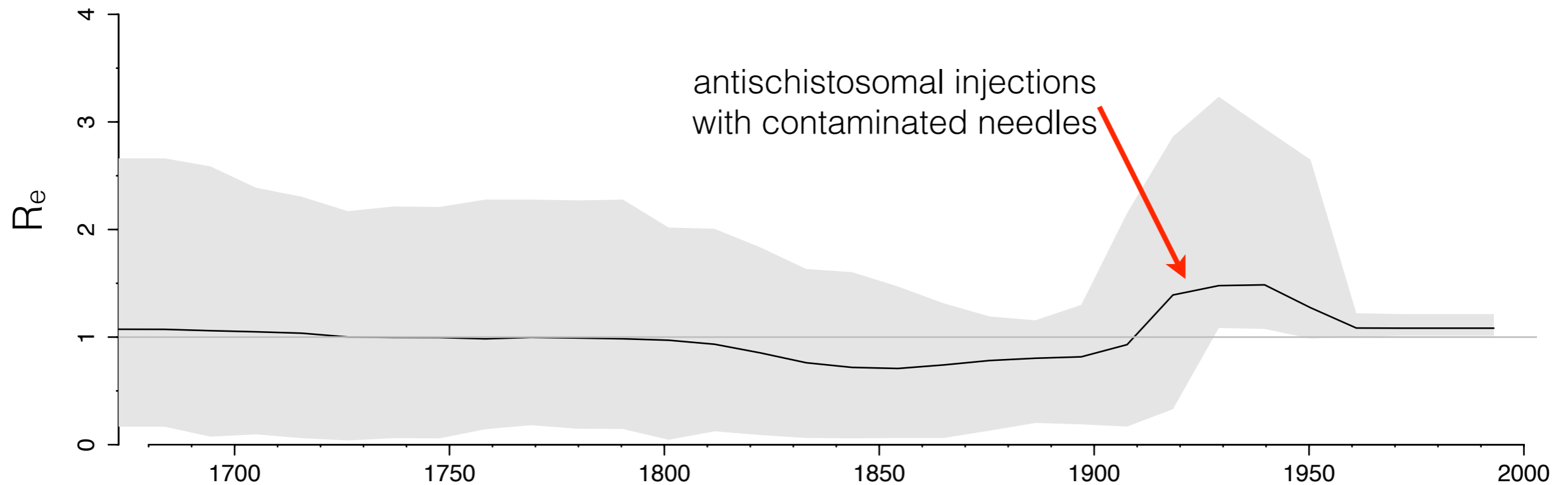
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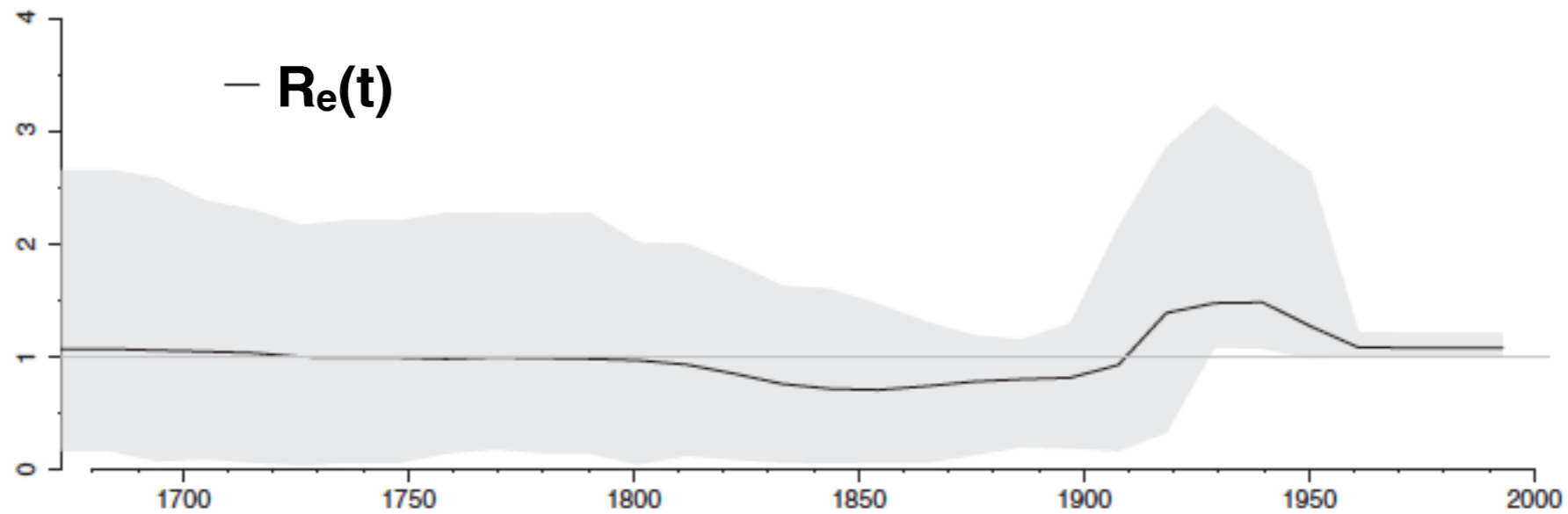
■ 95% HPD interval



# The two skyline models

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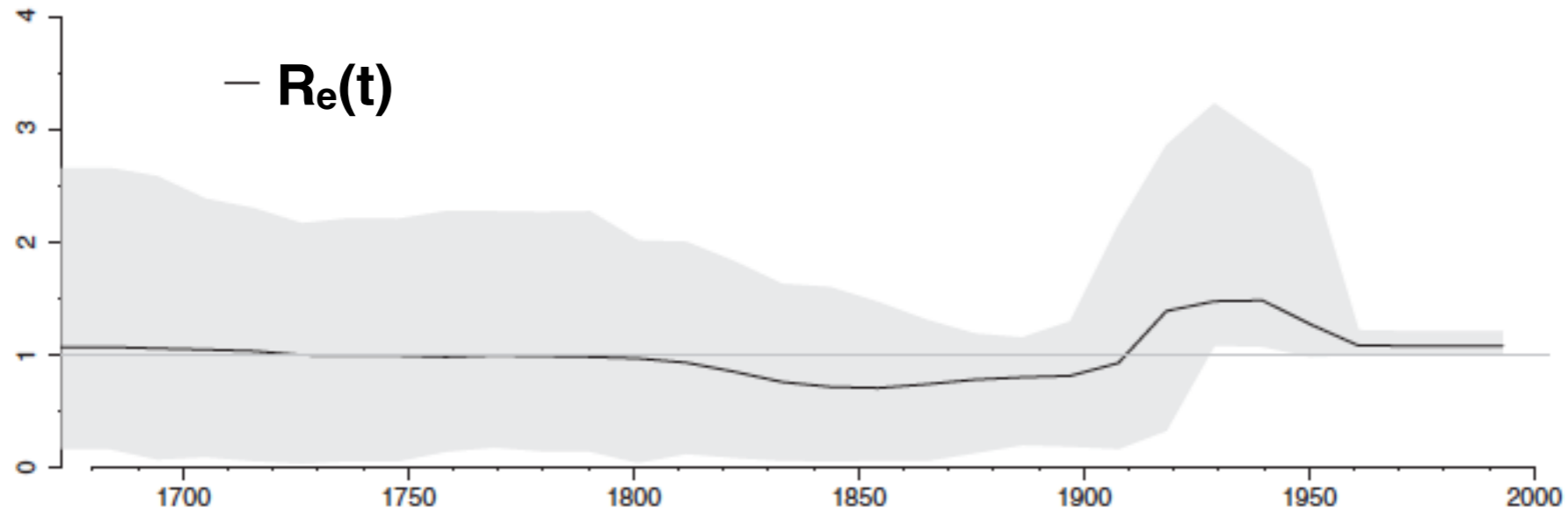
Birth-death skyline plot: effective reproductive number



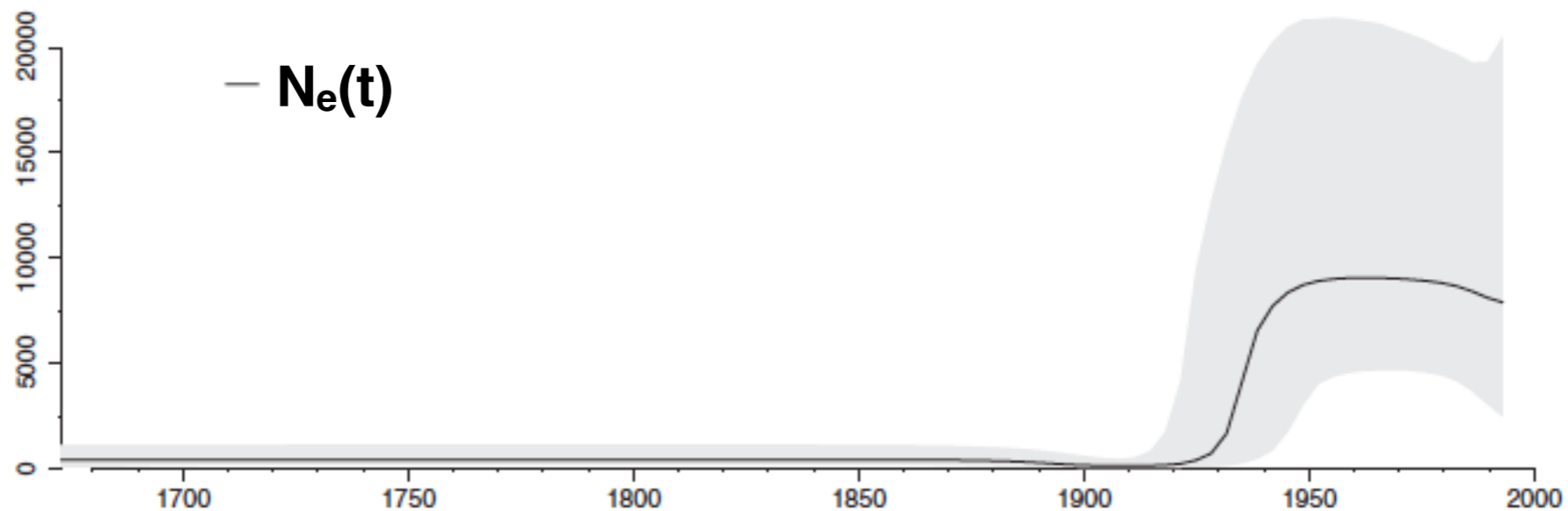
# The two skyline models

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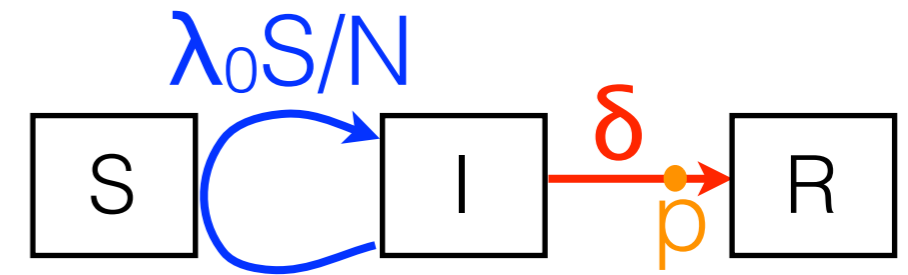
Birth-death skyline plot: effective reproductive number



Coalescent skyline plot: effective population size



### 3) SIR models



#### **SIR simulation (trees with 200 tips sampled):**

population size:  $N=5000$ , start with one infected,  $N=S+I+R$

$$\lambda(S) = \lambda_0 S/N$$

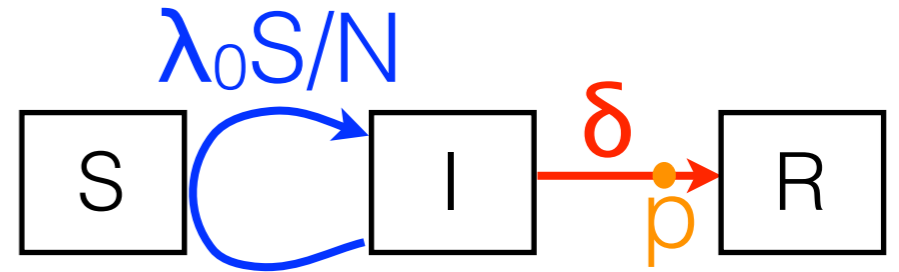
$$R_0 = \lambda_0/\delta = 4$$

host recovery rate:  $\delta = 0.5$

sampling probability:  $p = 0.05$



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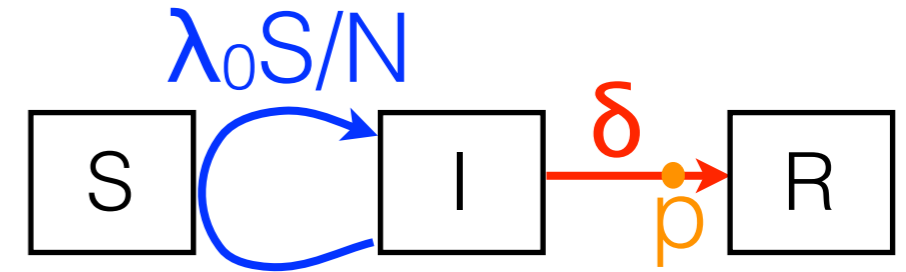
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**Inference:** 10 intervals for  $\lambda$ ,  $\delta$  and  $p$  constant across interval  
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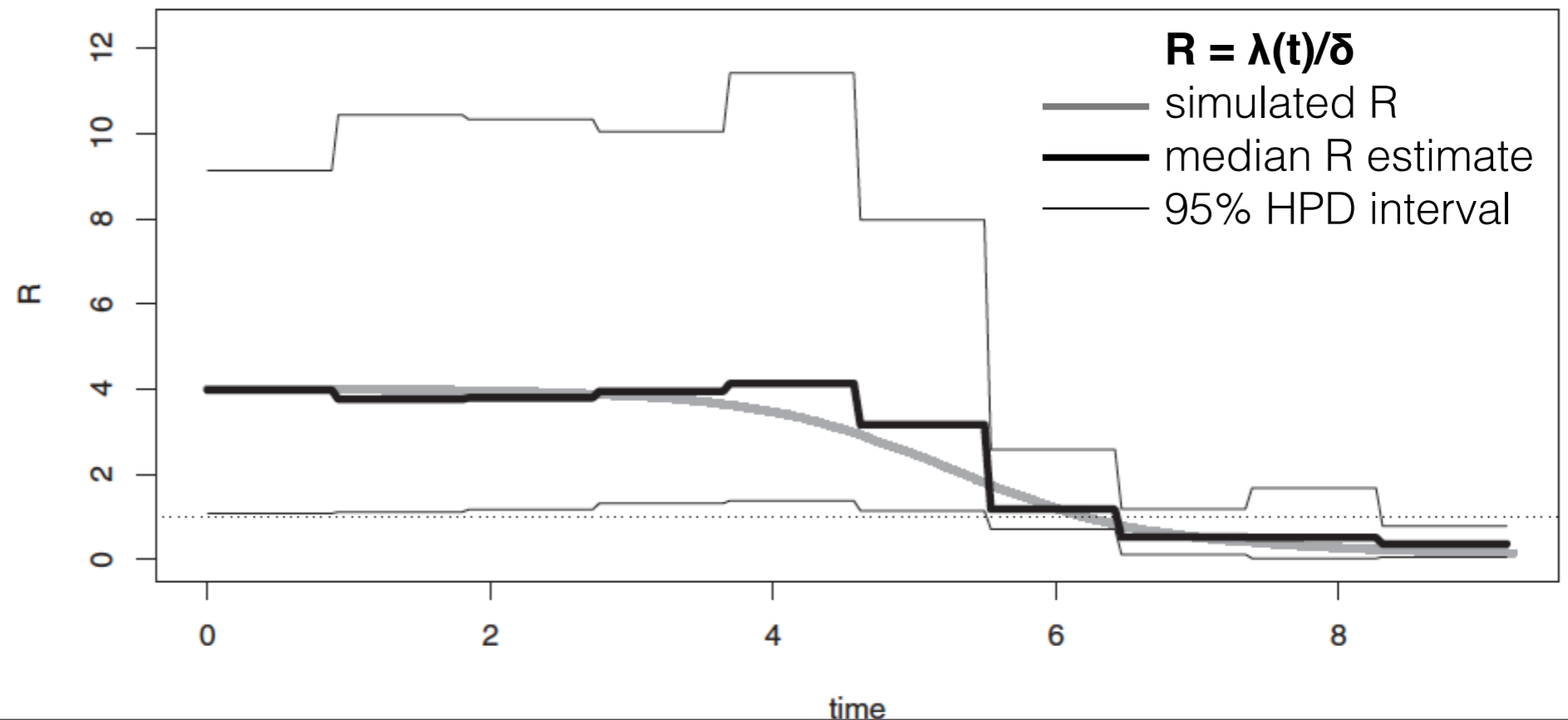
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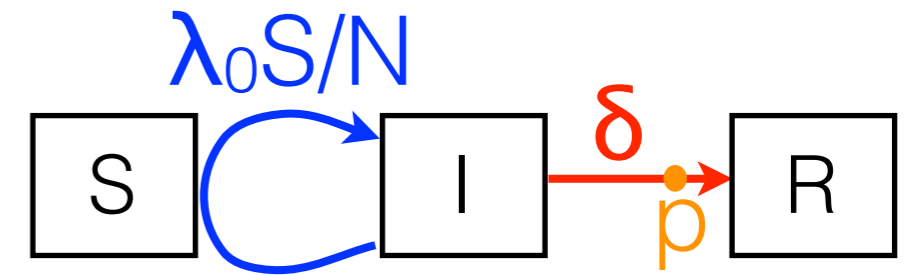
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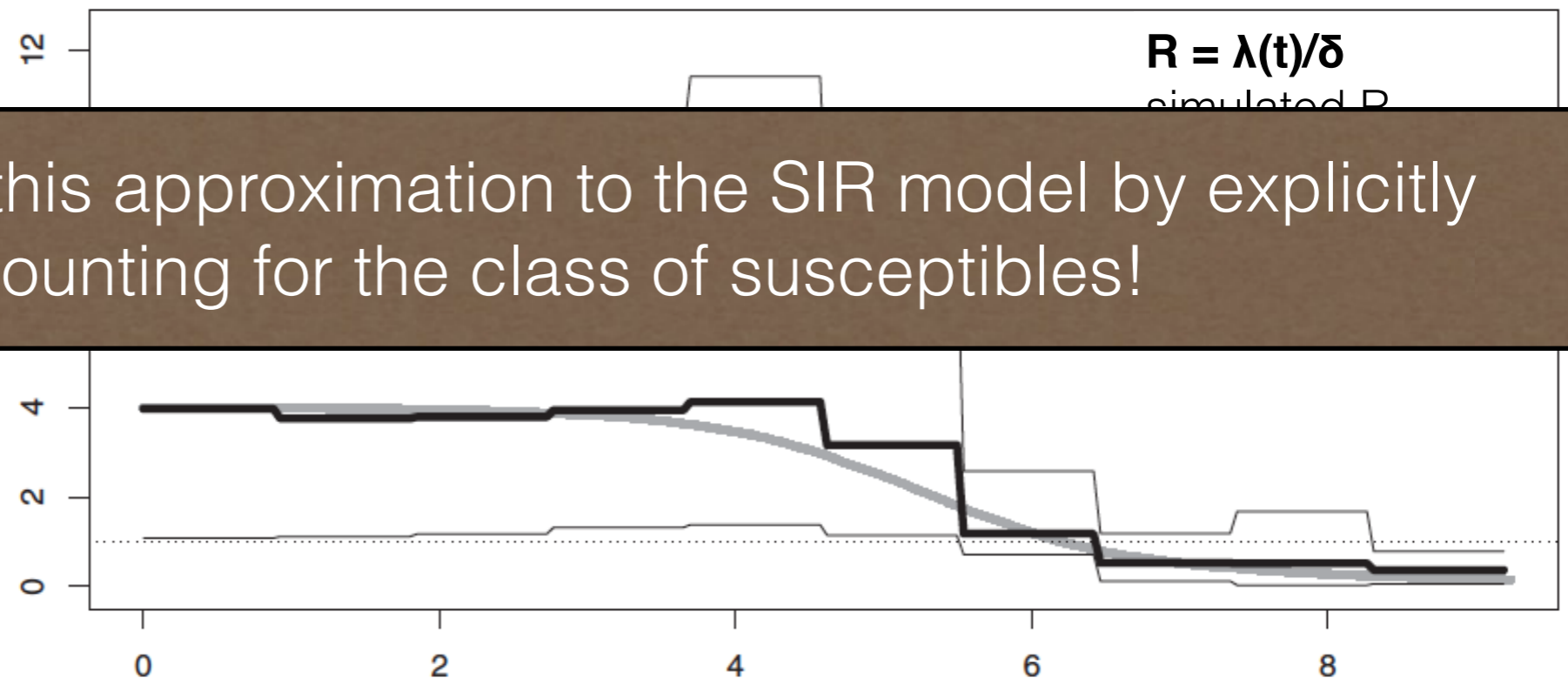
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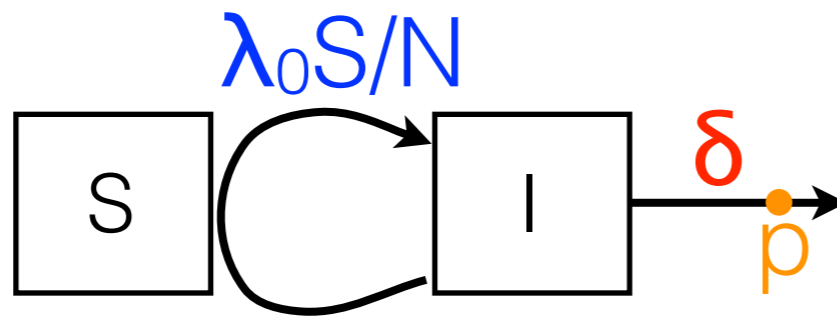


We improved this approximation to the SIR model by explicitly accounting for the class of susceptibles!

# SI dynamics - exact method

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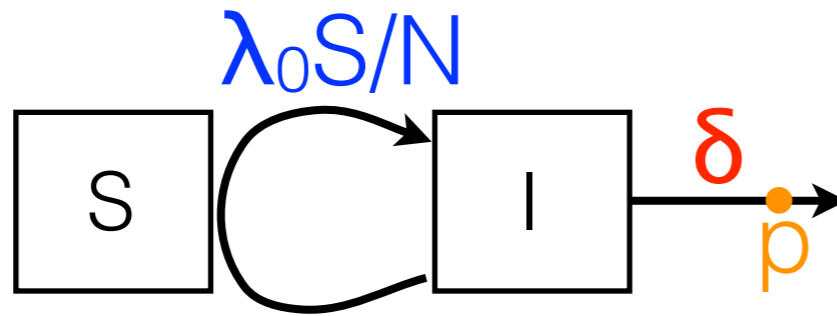
Para-  
meters



$$\mathbf{N} = S + I \text{ (constant)}$$

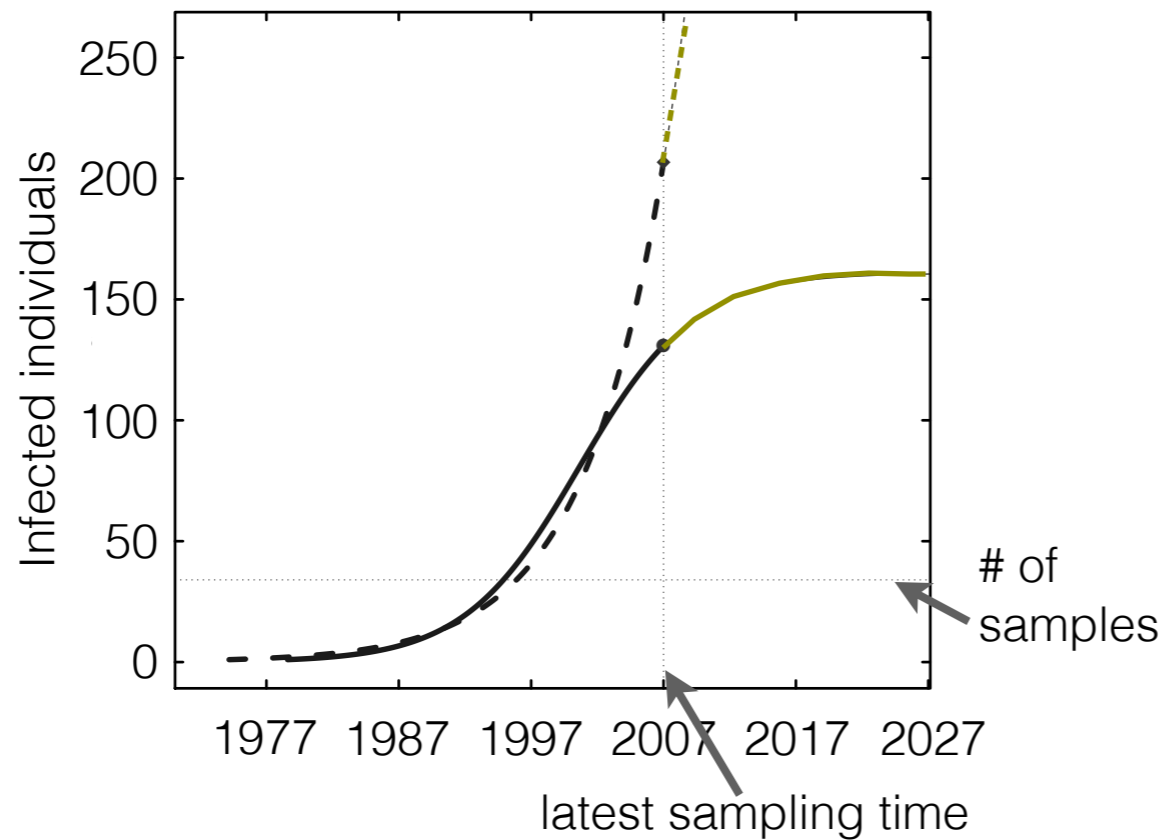
# SI dynamics - exact method

Parameters



$$N = S + I \text{ (constant)}$$

HIV transmission cluster in Switzerland

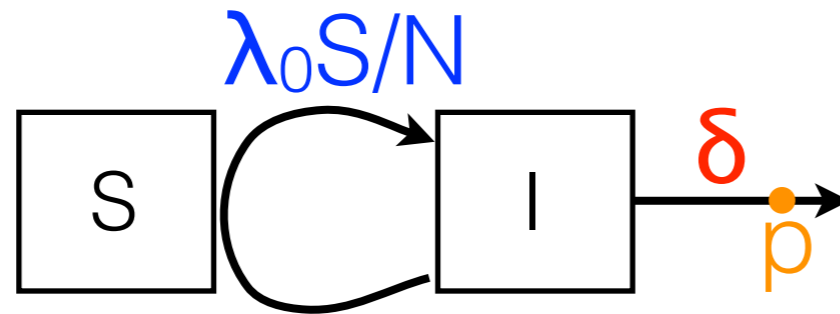


— SI model

- - - epidemic outbreak model

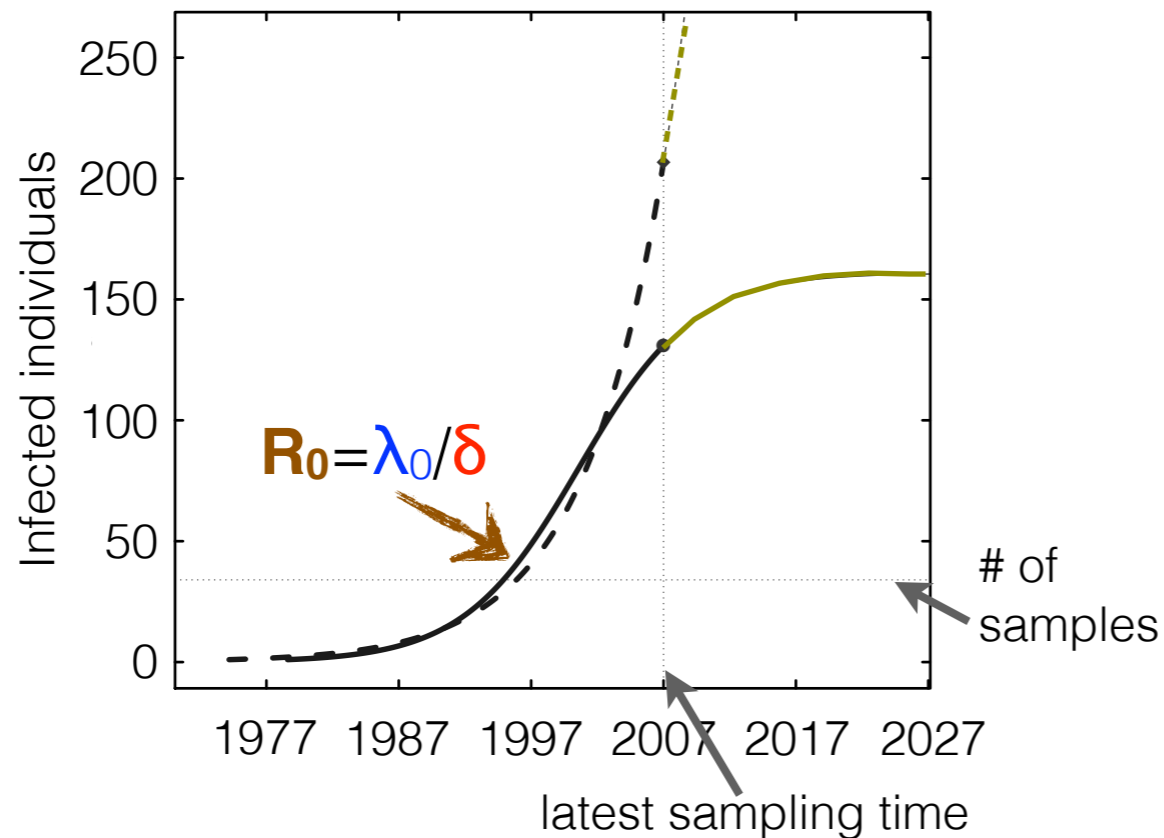
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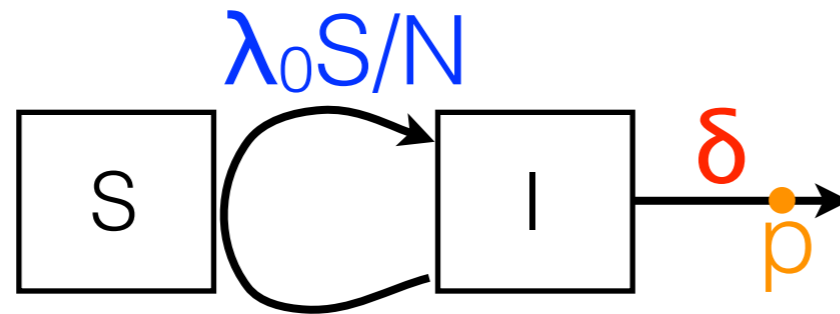


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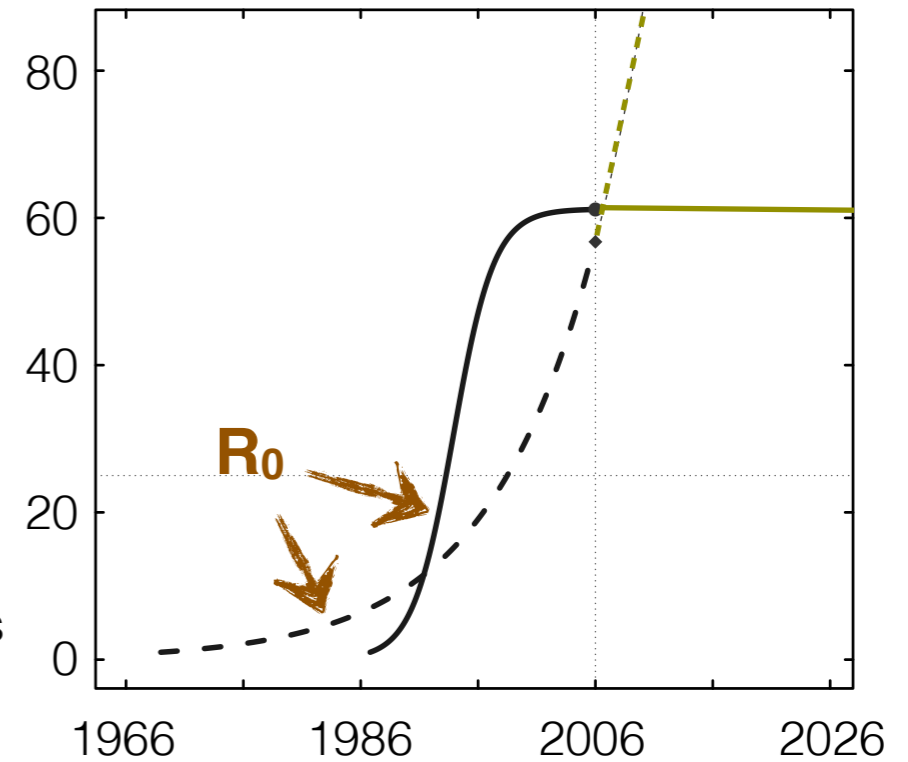
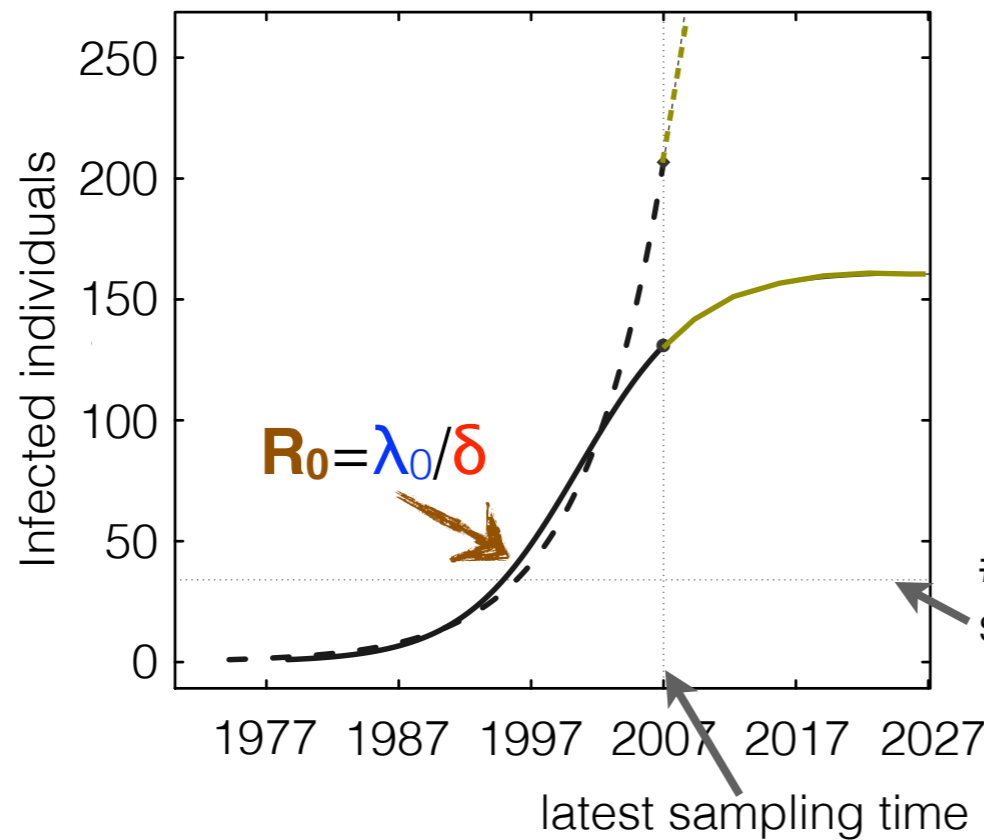
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Parameters



$N = S + I$  (constant)

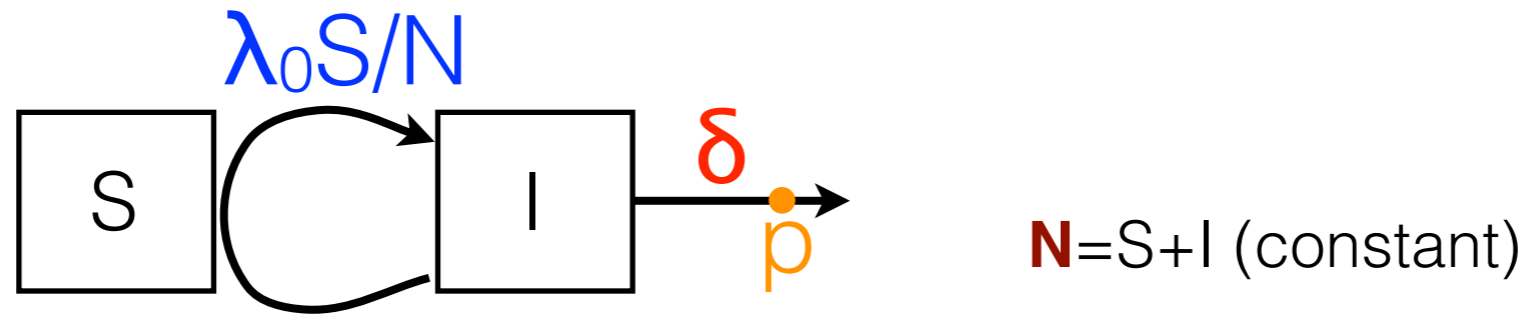
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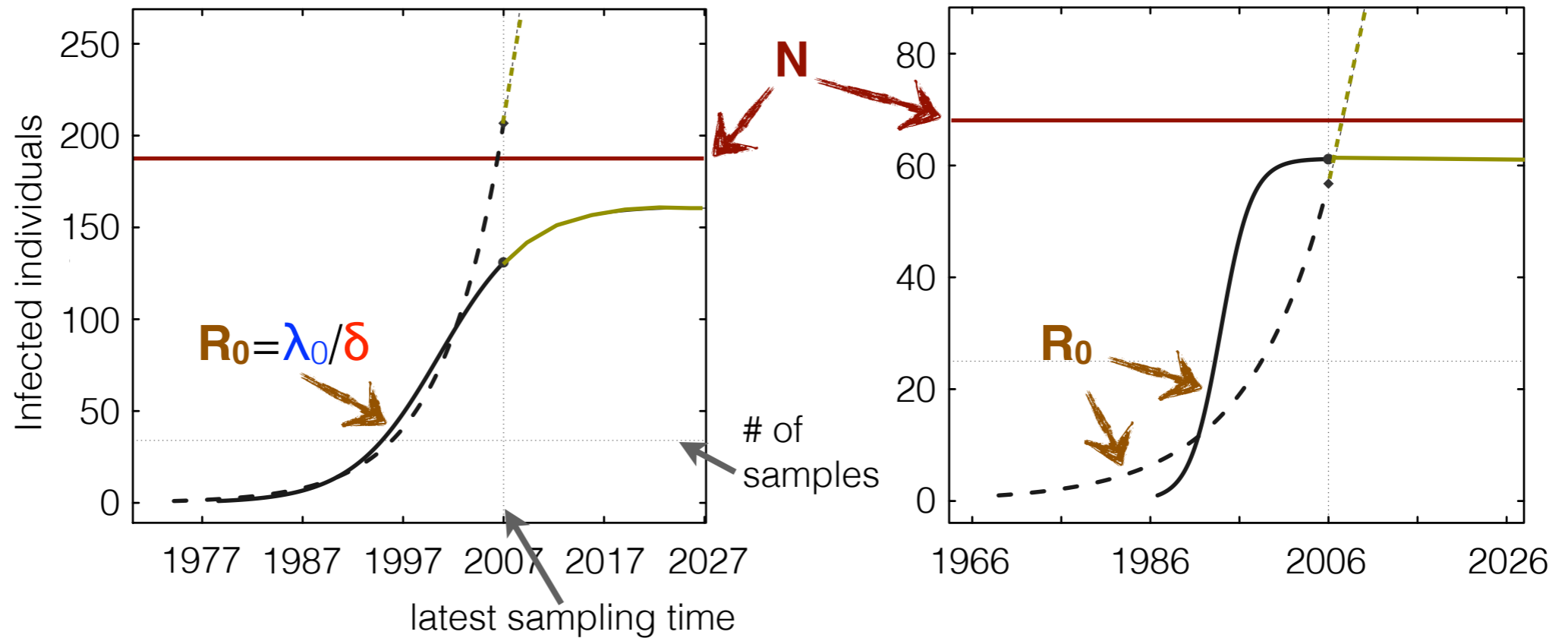
— SI model  
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# SI dynamics - exact method

Parameters



HIV transmission cluster in Switzerland



— SI model  
 - - - epidemic outbreak model



# SIR models: Birth-death or coalescent?

---

Coales-  
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imation

Volz et al., Genetics, 2009

So far sampling at one time point, not in Beast

Tim Vaughan implements it in Beast for comparison

# SIR models: Birth-death or coalescent?

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Coalescent  
approximation

Volz et al., Genetics, 2009

So far sampling at one time point, not in Beast

Tim Vaughan implements it in Beast for comparison

Birth-death  
approximation

BDSIR add-on in Beast v2.0

Simulations show good performance

Flexible framework (SI, SIS, SIR, SEIR, etc)

**Poster: Denise Kühnert**

# SIR models: Birth-death or coalescent?

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Coalescent approximation

Volz et al., Genetics, 2009

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Birth-death approximation

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Simulations show good performance

Flexible framework (SI, SIS, SIR, SEIR, etc)

**Poster: Denise Kühnert**

Birth-death exact

expoTree (R package)

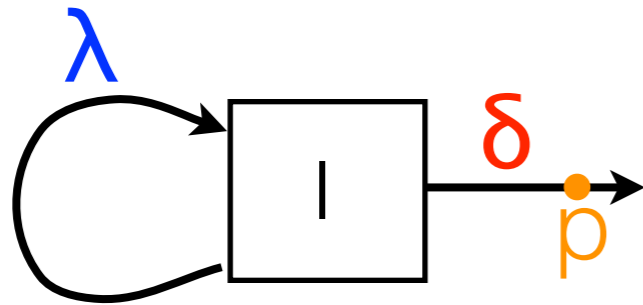
Promising to estimate overall population size  $N=S+I$

Future study will identify potential limitations of approximate method

**Poster: Gabriel Leventhal**

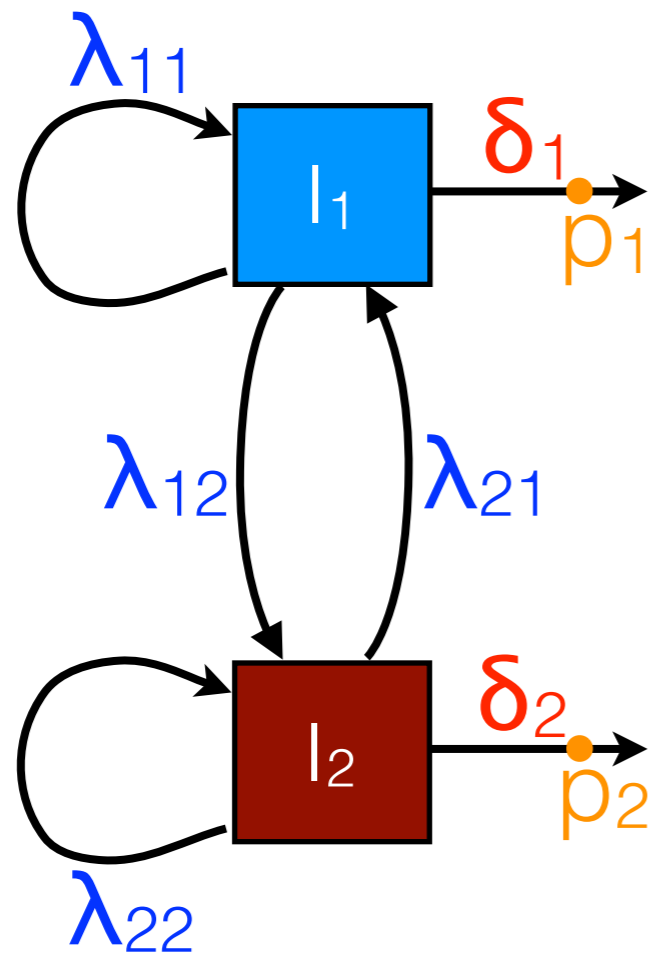
## 4) Host population structure

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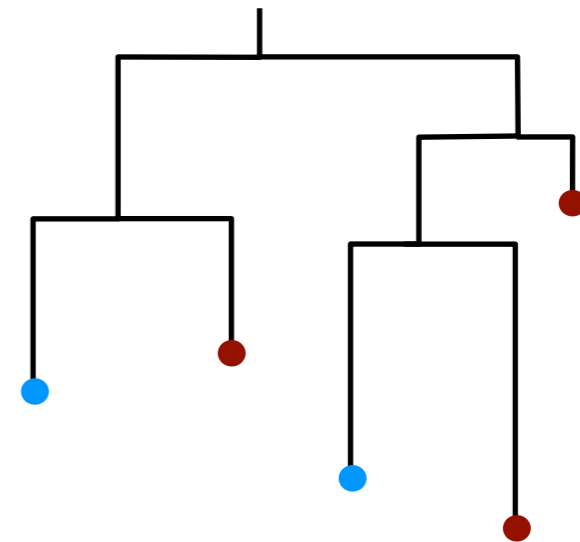
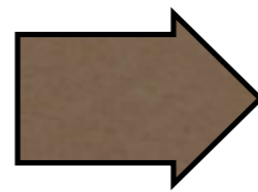
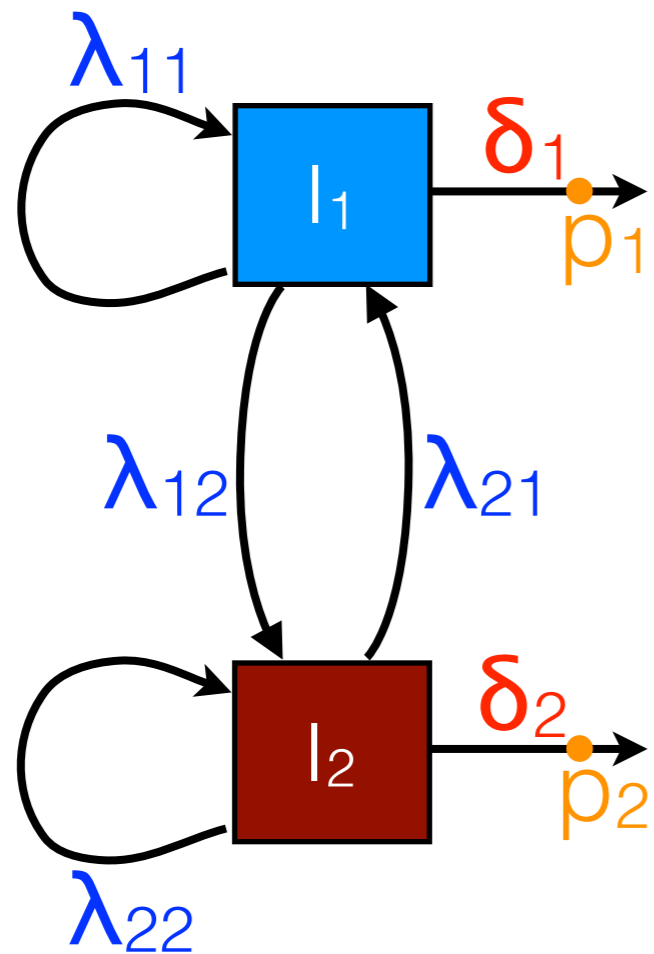
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# 4) Host population structure

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# Quantification of risk-group dependent spread of HIV

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Two states

Heterosexual

Intravenous drug user

# Quantification of risk-group dependent spread of HIV

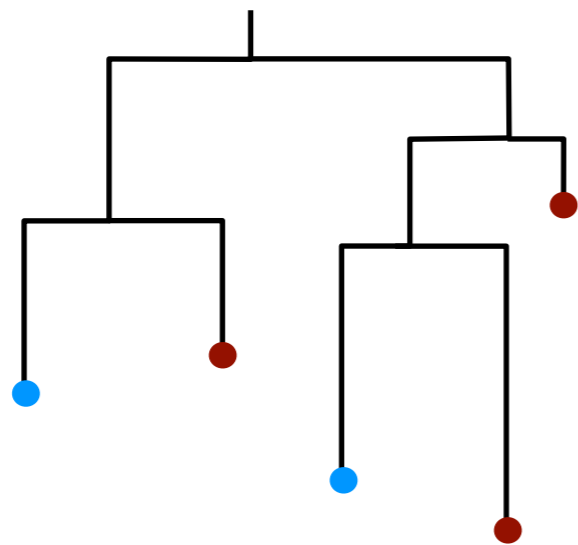
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Two states

Heterosexual

Intravenous drug user

Data



220 Latvian sequences from  
Balode et al. (2012)



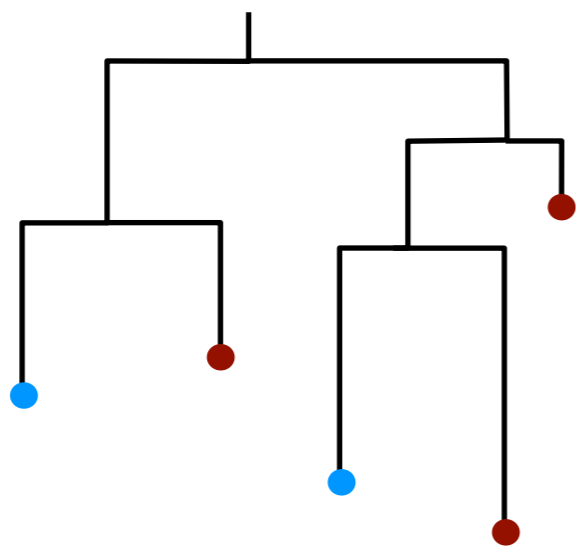
# Quantification of risk-group dependent spread of HIV

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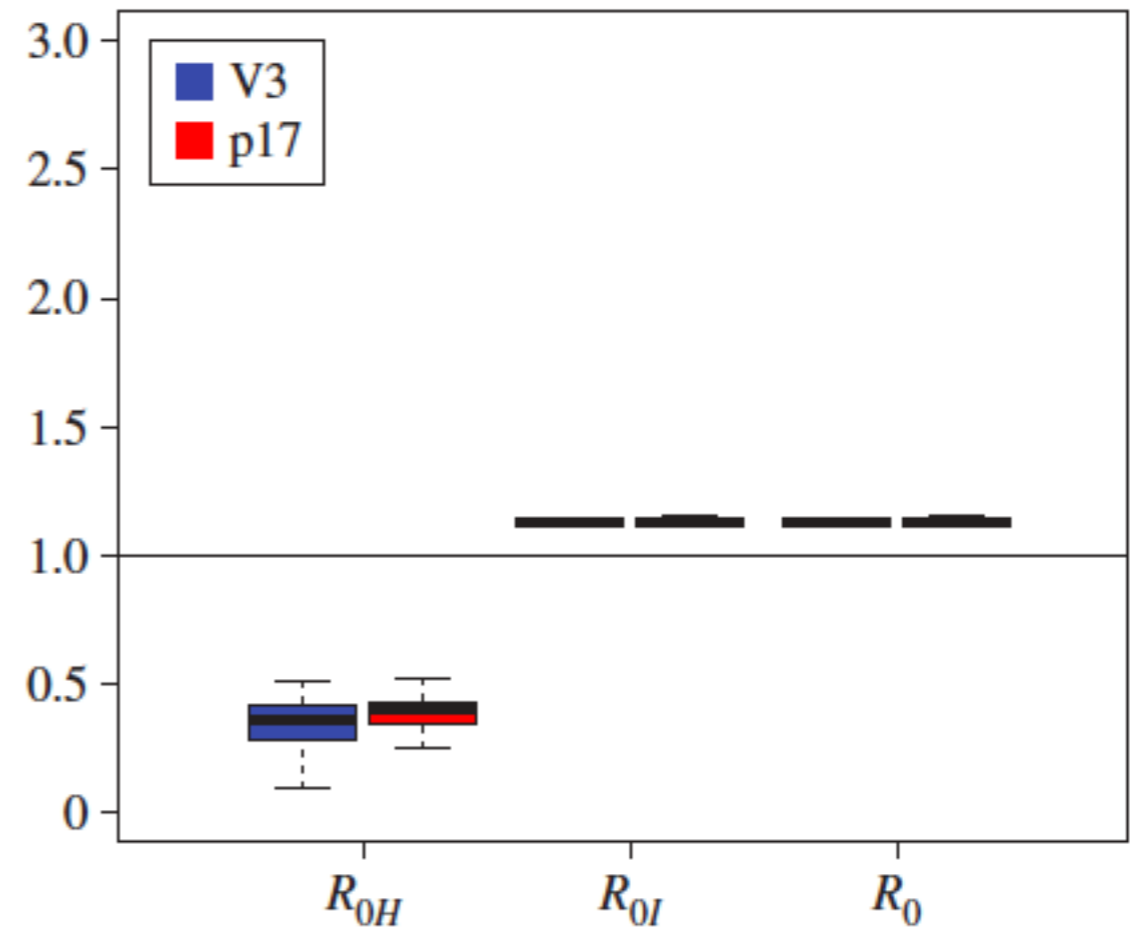
Heterosexual

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# Quantification of super-spreading in HIV

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**S**uper-spreader

**N**ormal-spreader

# Quantification of super-spreading in HIV

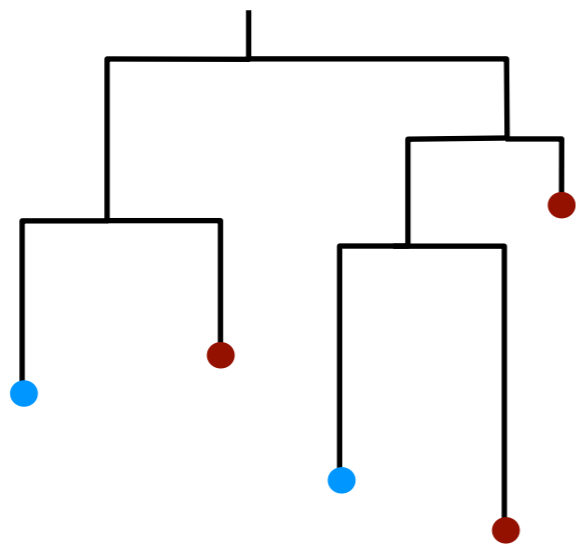
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40 Latvian sequences from  
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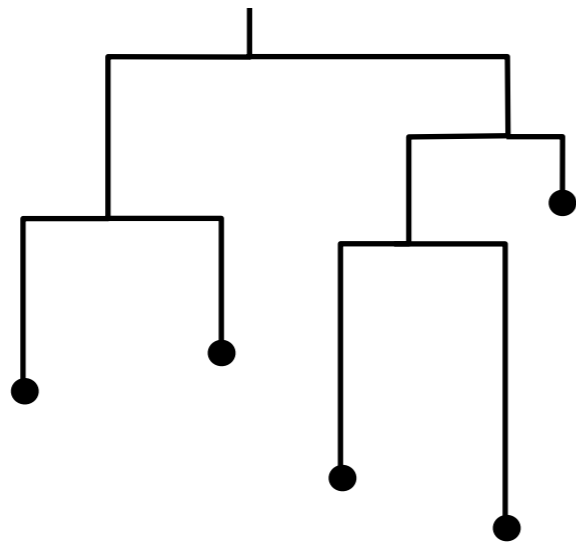
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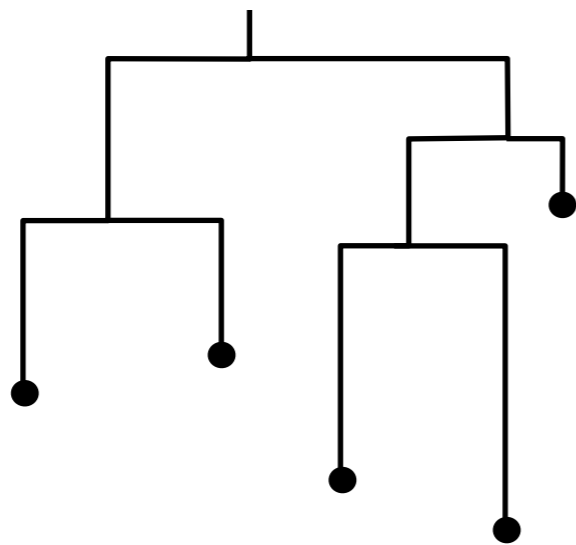
# Quantification of super-spreading in HIV

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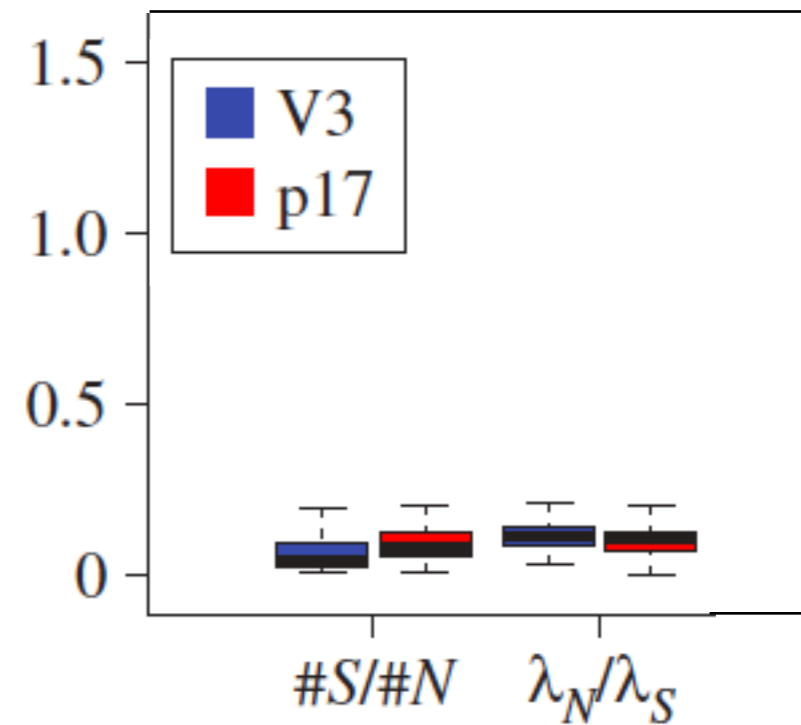
Super-spreader

Normal-spreader

Data



40 Latvian sequences from  
Balode et al. (2012)



# Key questions in infectious disease ecology approached through phylogenetics

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Human pathogens



Domestic animals & plants

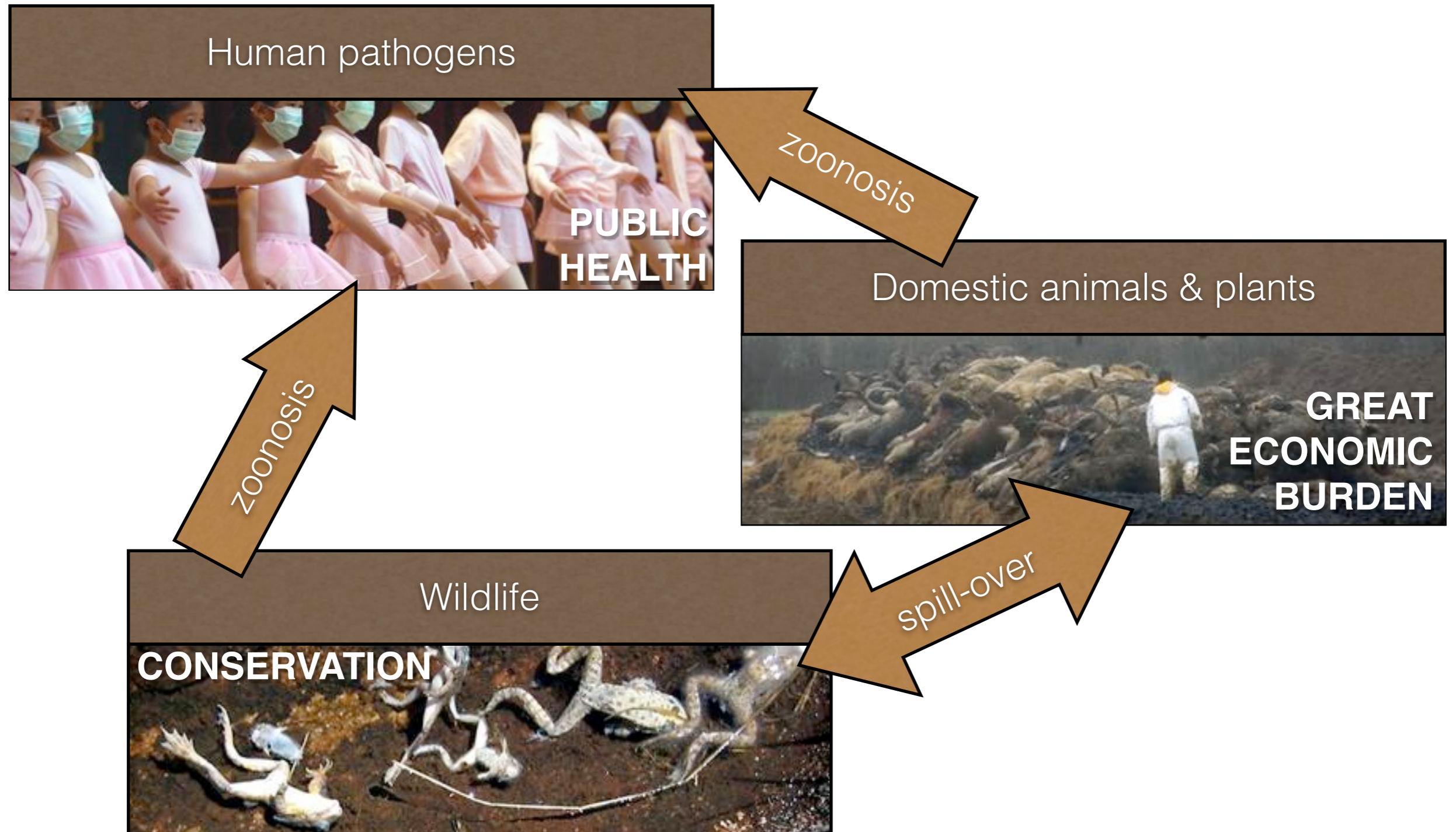


Wildlife

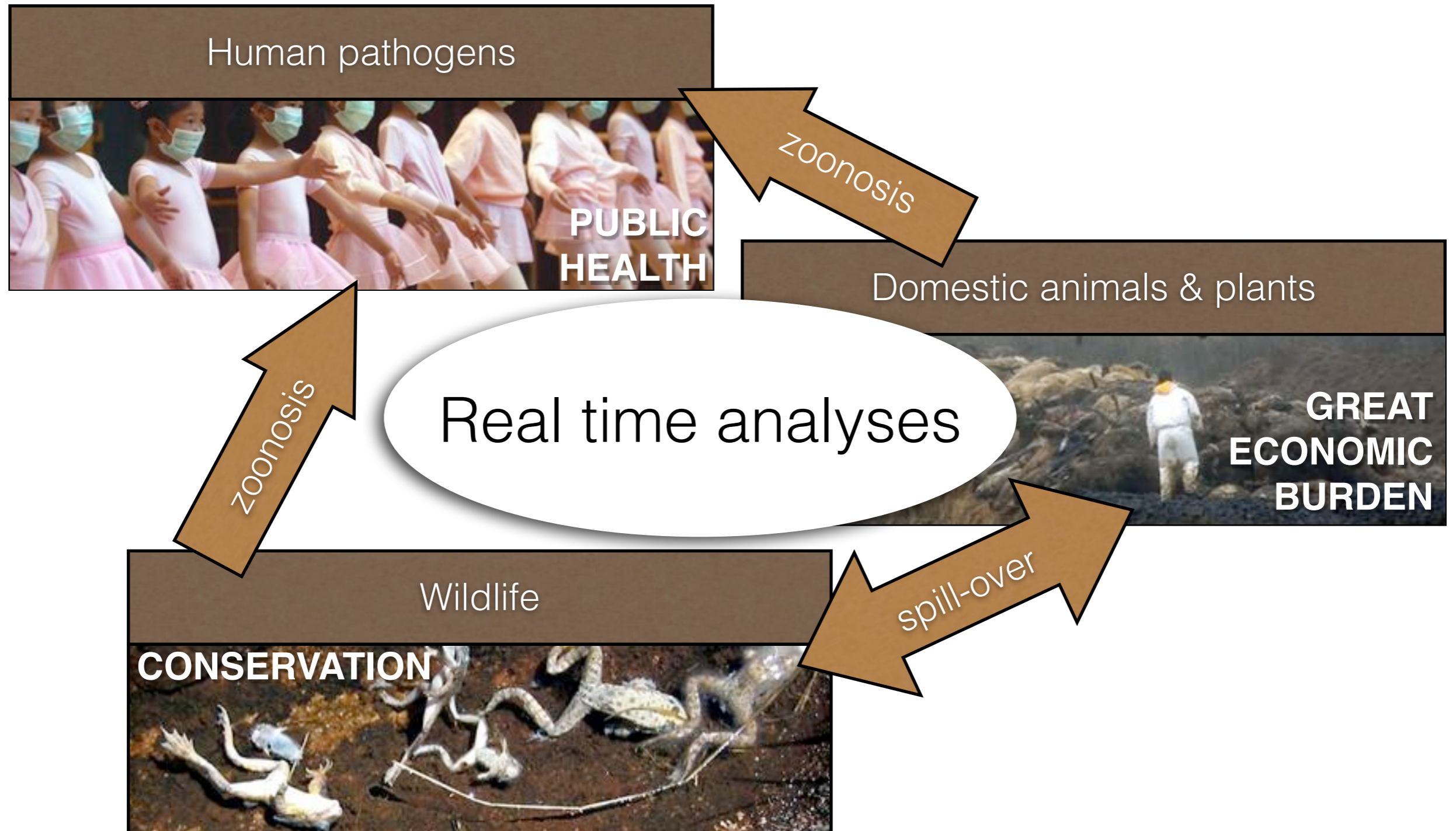
**CONSERVATION**



# Key questions in infectious disease ecology approached through phylogenetics



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# Phylogeny of Acknowledgements

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