



# Partial selective sweeps and genetic signatures of ongoing adaptation

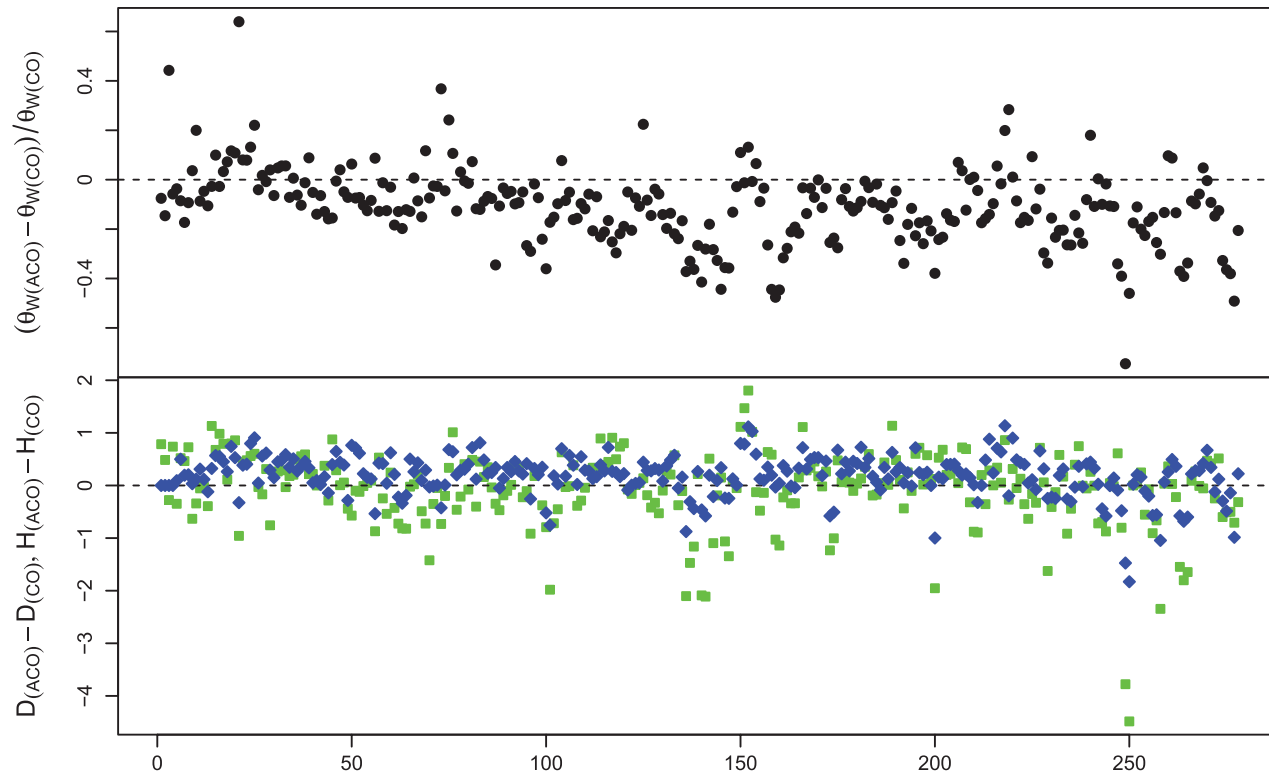
Luca Ferretti, Alex Klassmann,  
Sebastian Ramos-Onsins, Guillaume Achaz

The Pirbright Institute  
UPMC and Collège de France



# Signals of recent selection from sequences

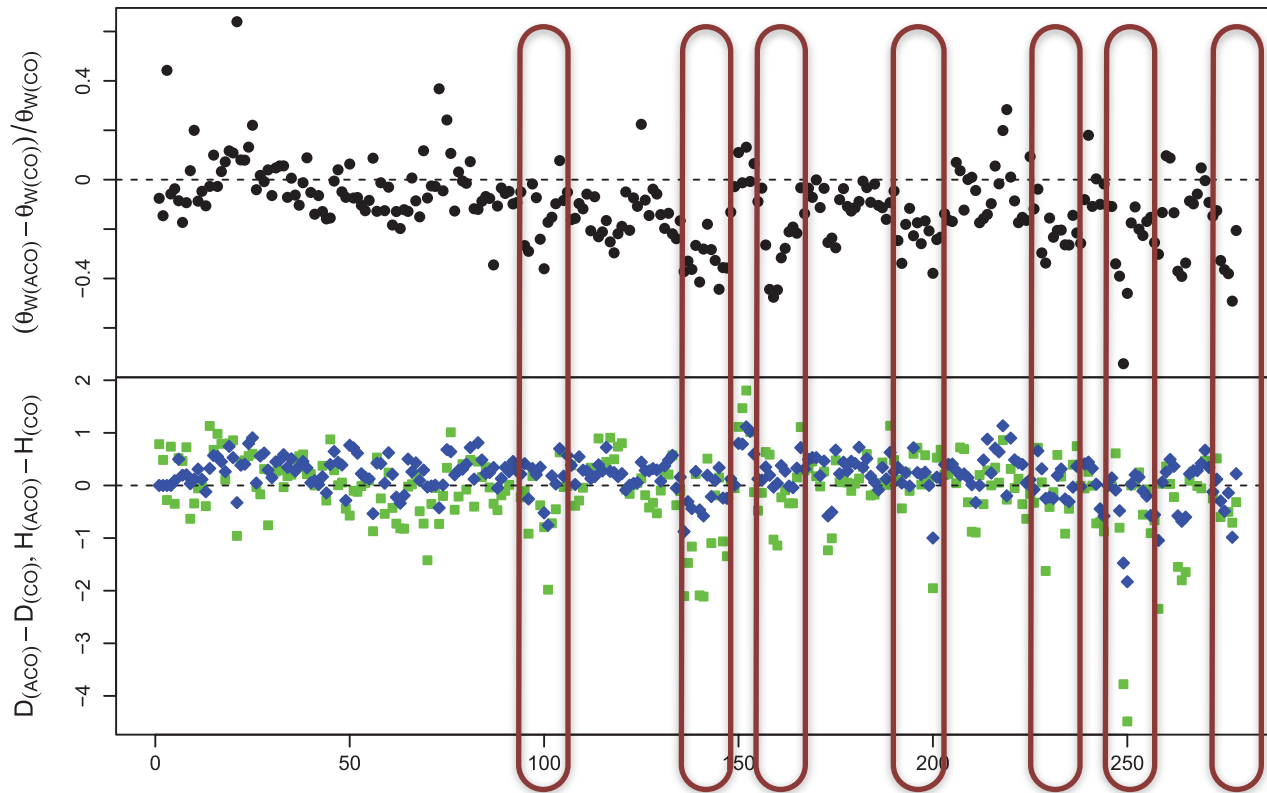
Example: experimental evolution for accelerated life cycle in *Drosophila*



Burke et al, Nature 2010 (analysis from Ferretti et al, Mol Ecol 2013)


# Signals of recent selection from sequences

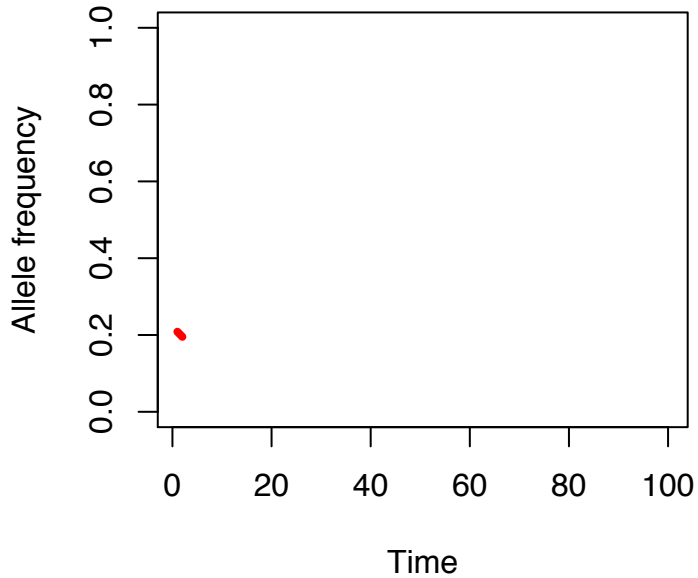
Example: experimental evolution for accelerated life cycle in *Drosophila*



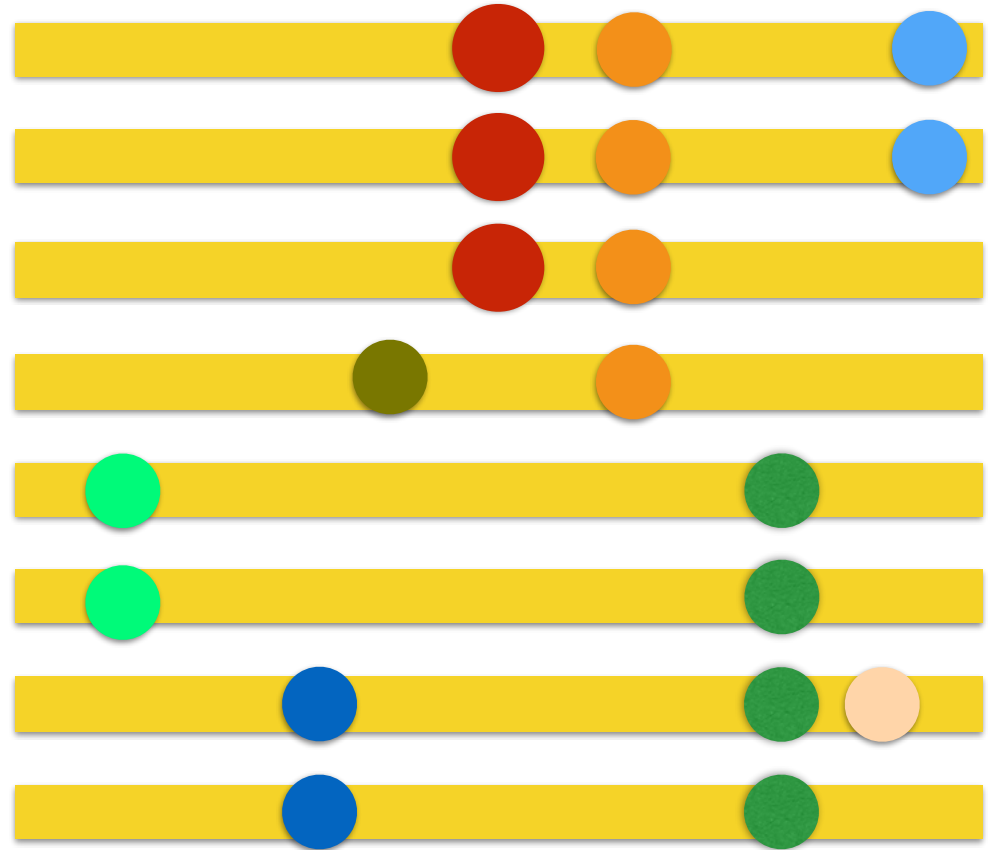
Partial selective sweeps?

# Evolution of a neutral sequence


Frequency of the  mutation in the population

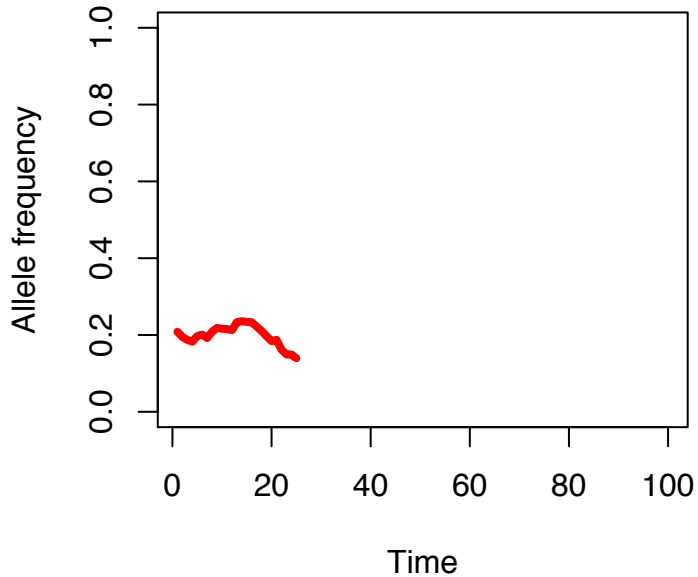


Mutations in a sample:

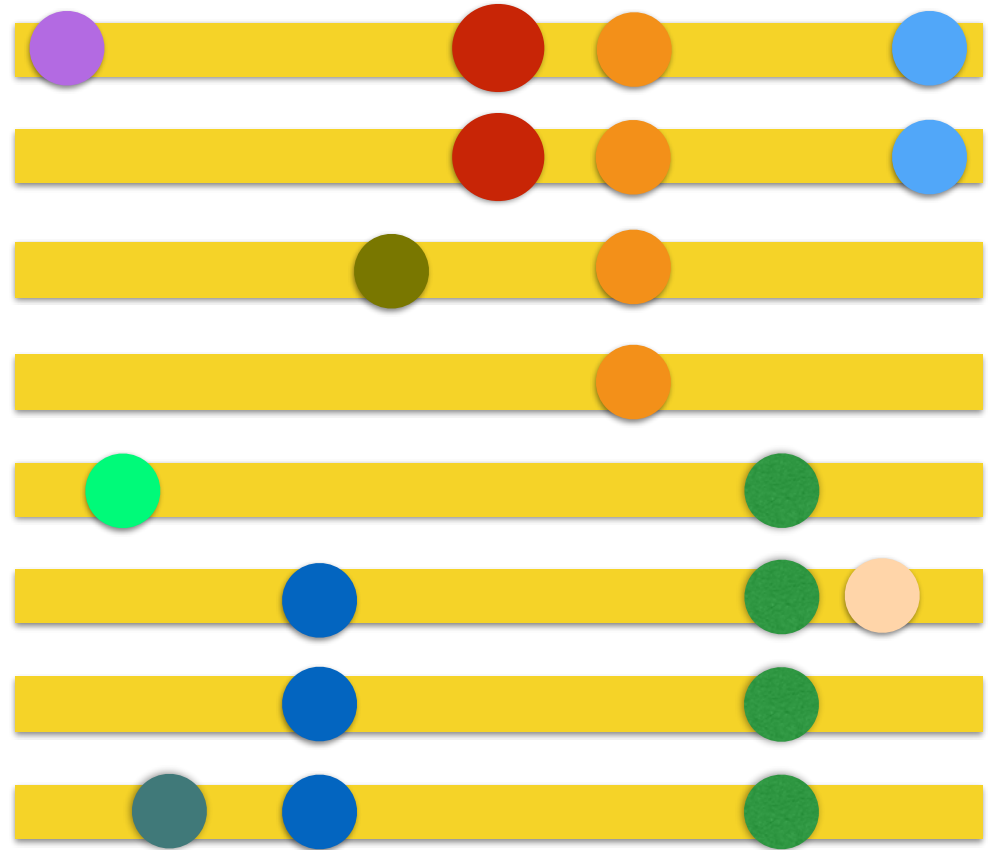


# Evolution of a neutral sequence

Frequency of the  mutation in the population



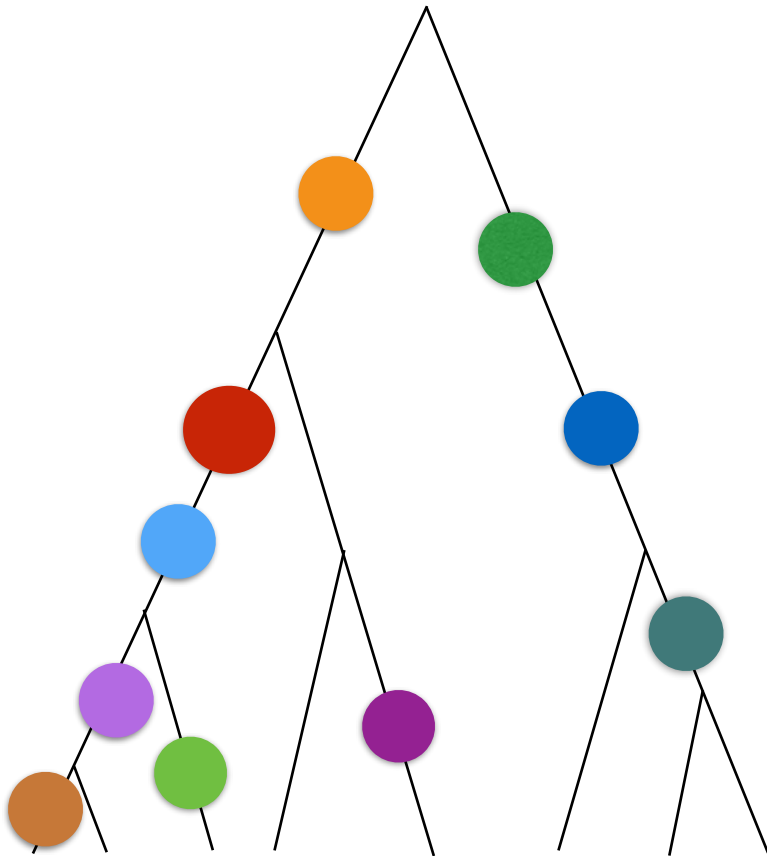
Mutations in a sample:



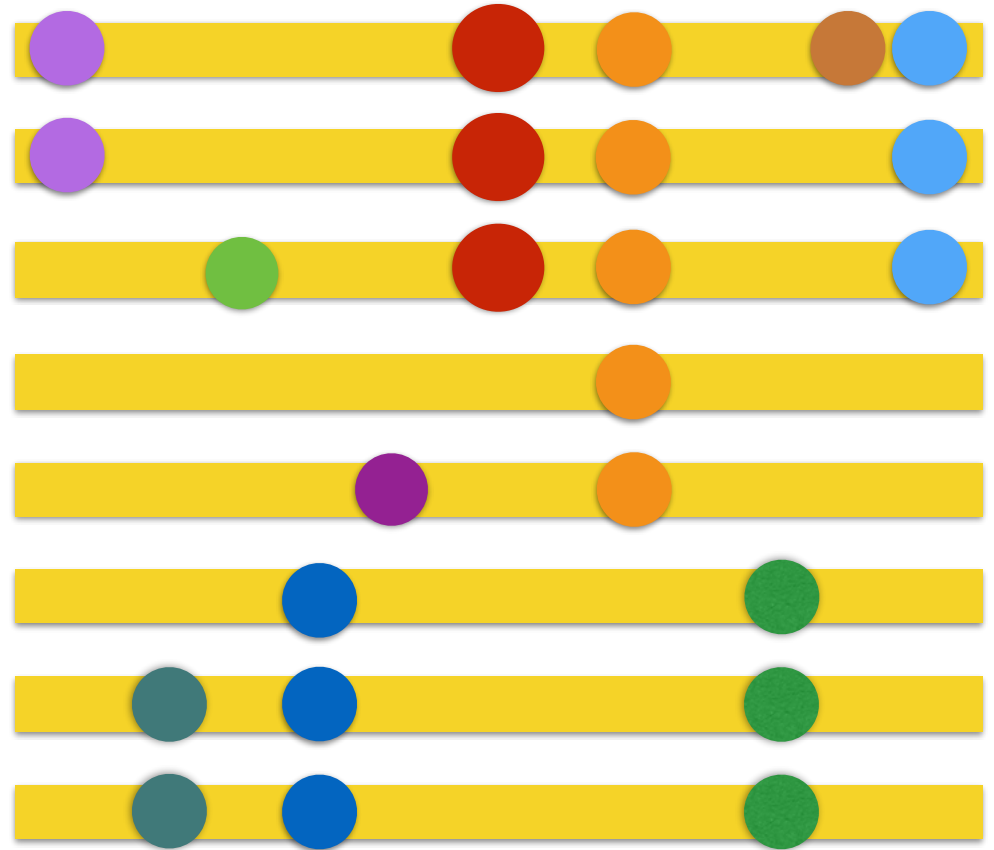
# Evolution of a neutral sequence



Genealogy of the sample

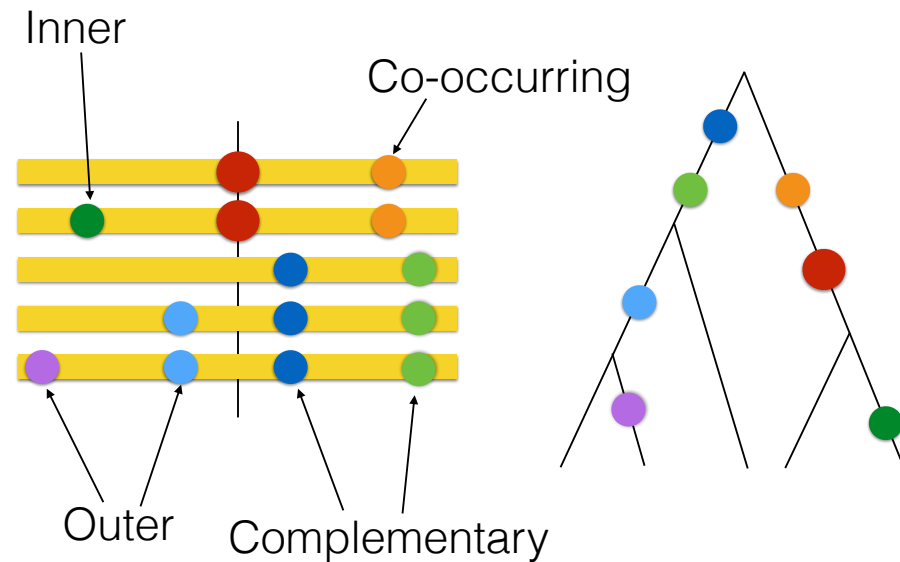
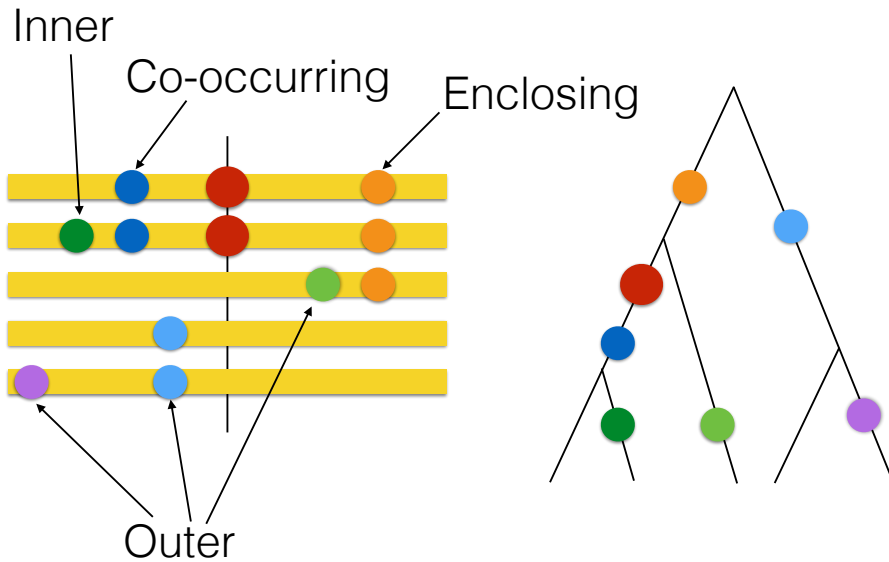


Mutations in a sample:



# How? Coalescent theory of pairs of mutations

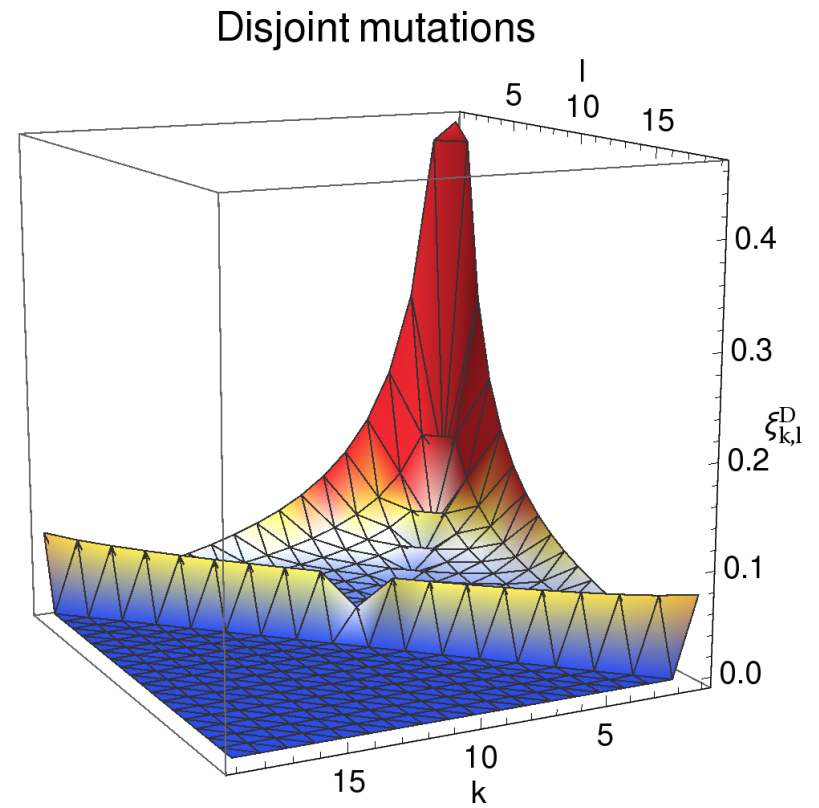
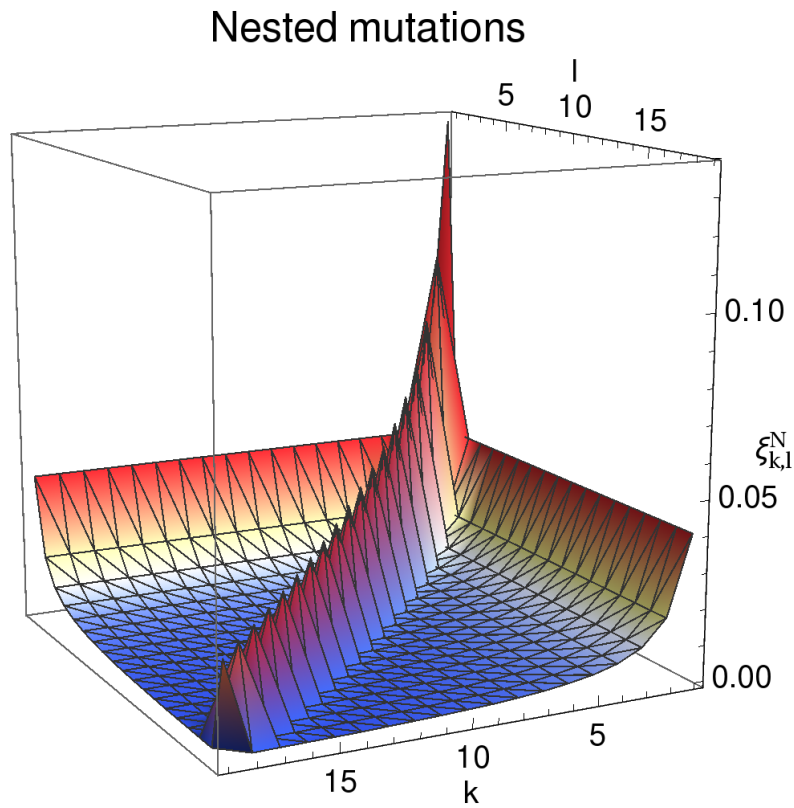
no recombination: 2 types of pairs, *nested* or *disjoint*  
and 5 types of mutations relative to a focal mutation...



nested = inner + cooccurring + enclosing  
disjoint = outer + complementary



# 2-SFS



for neutral model (from Kingman's coalescent)

# 2-SFS and spectrum of linked mutations



From *2-SFS of pairs of mutations*  $f, f_0$   
to *SFS of mutations  $f$  linked to a focal one  $f_0$*

“joint” 2-SFS : “conditional” SFS of linked sites

=

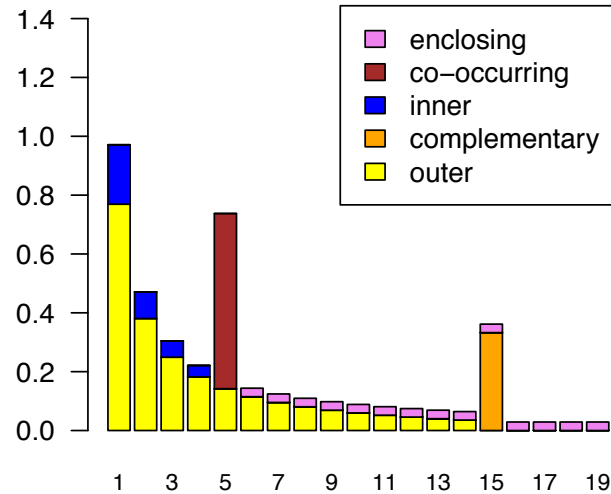
joint probability  $p(f, f_0)$  : conditional probability  $p(f|f_0)$

# Frequency of linked mutations

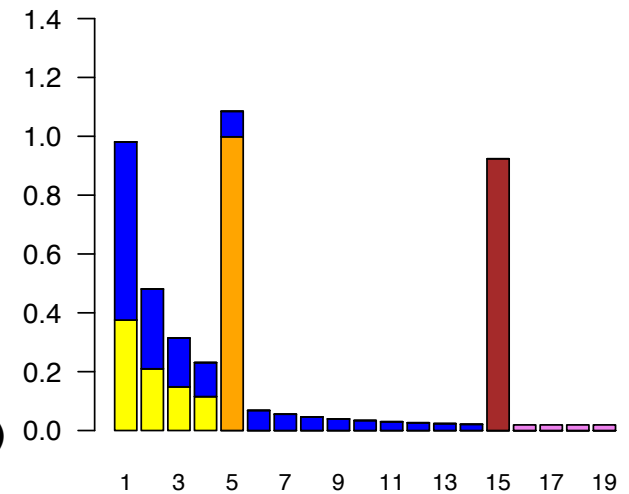
$$\begin{aligned} \mathbb{E}[\xi^{(i)}(f|f_0)] &= \theta L \cdot \frac{f_0}{(1-f)^2} \left( 1 + \frac{1}{f} + \frac{2 \ln(f)}{1-f} \right), \quad f < f_0 \\ \mathbb{E}[\xi^{(co)}(f|f_0)] &= \theta L \cdot \delta(f - f_0) \frac{2f_0}{1-f_0} \left( -\frac{\ln(f_0)}{1-f_0} - 1 \right) \\ \mathbb{E}[\xi^{(e)}(f|f_0)] &= \theta L \cdot \frac{f_0}{(1-f_0)^2} \left( 1 + \frac{1}{f_0} + \frac{2 \ln(f_0)}{1-f_0} \right), \quad f > f_0 \quad (14) \\ \mathbb{E}[\xi^{(cm)}(f|f_0)] &= \theta L \cdot \delta(f - 1 + f_0) \left[ \frac{1-f_0}{f_0} \log(1-f_0) + \left( \frac{f_0}{1-f_0} \right)^2 \log(f_0) + \frac{1}{1-f_0} \right] \\ \mathbb{E}[\xi^{(o)}(f|f_0)] &= \theta L \cdot \left[ \frac{1}{f} - \frac{f_0}{(1-f)^2} \left( 1 + \frac{1}{f} + \frac{2 \ln(f)}{1-f} \right) \right. \\ &\quad \left. - \frac{f_0}{(1-f_0)^2} \left( 1 + \frac{1}{f_0} + \frac{2 \ln(f_0)}{1-f_0} \right) \right], \quad f < 1 - f_0 \end{aligned}$$

# Frequency of linked mutations

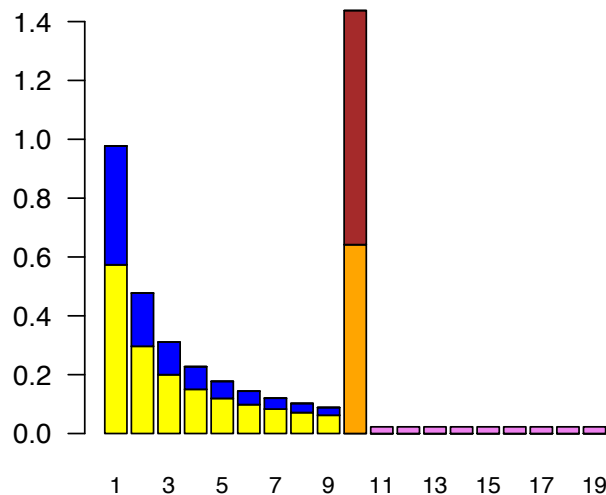
Linked mutation frequency (n=20,k=5)




Linked mutation frequency (n=20,k=15)

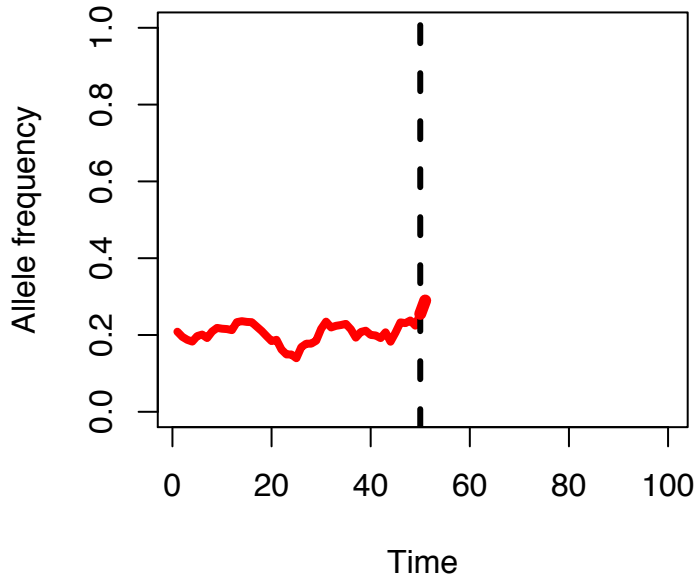


Linked mutation frequency (n=20,k=10)

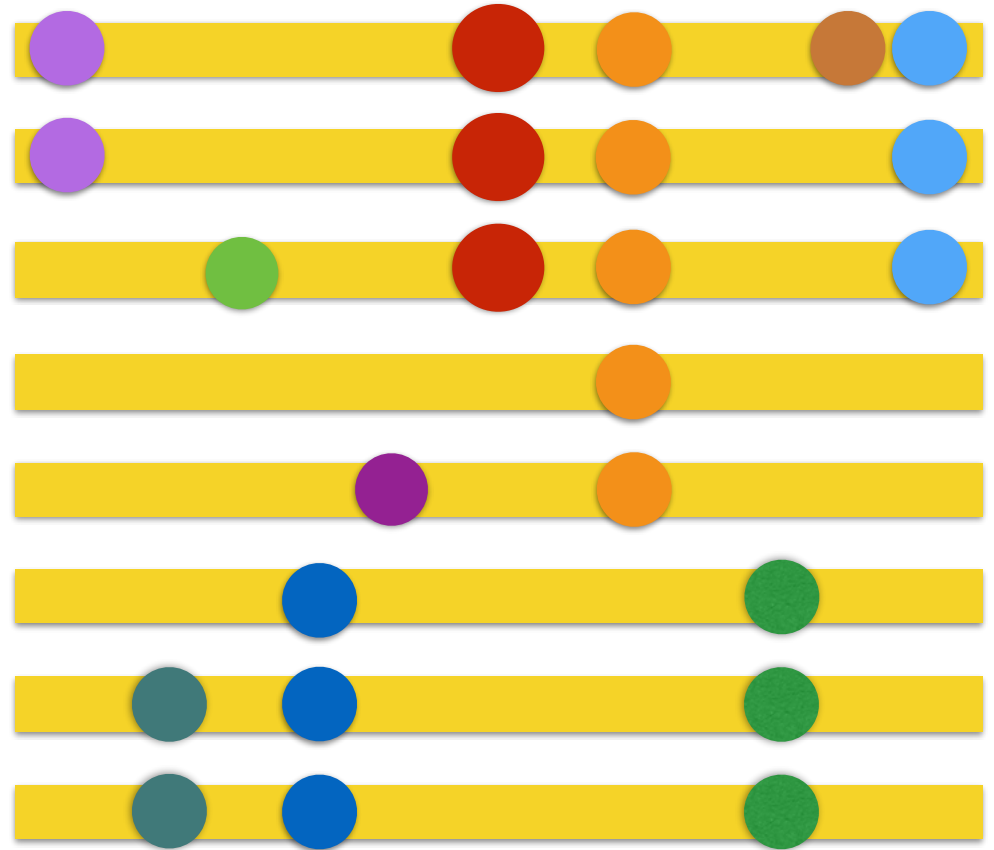


# Sudden environmental change! e.g. new viral strain

Frequency of the  mutation in the population

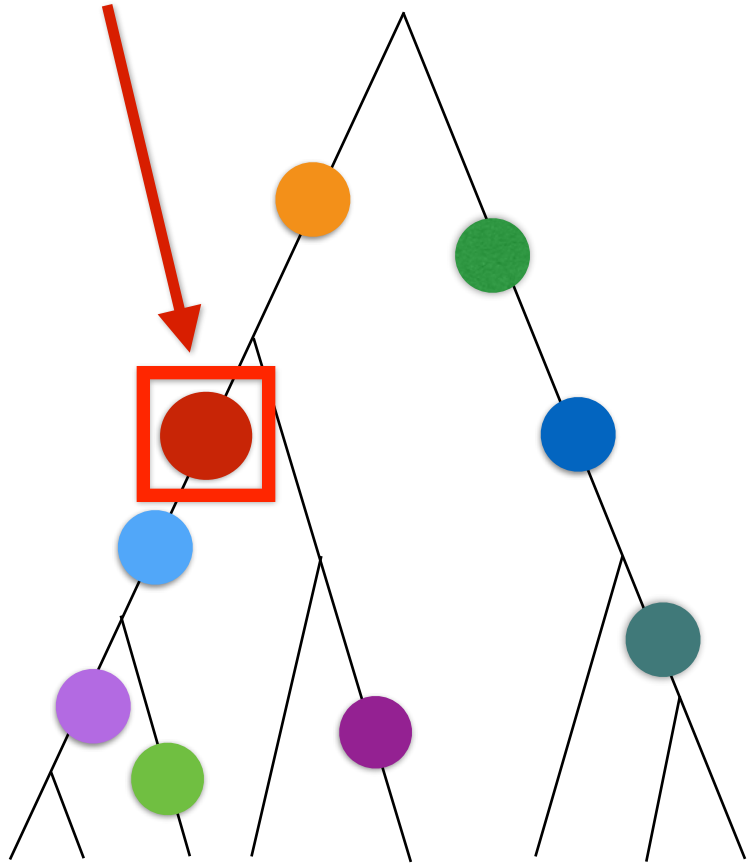


Mutations in a sample:

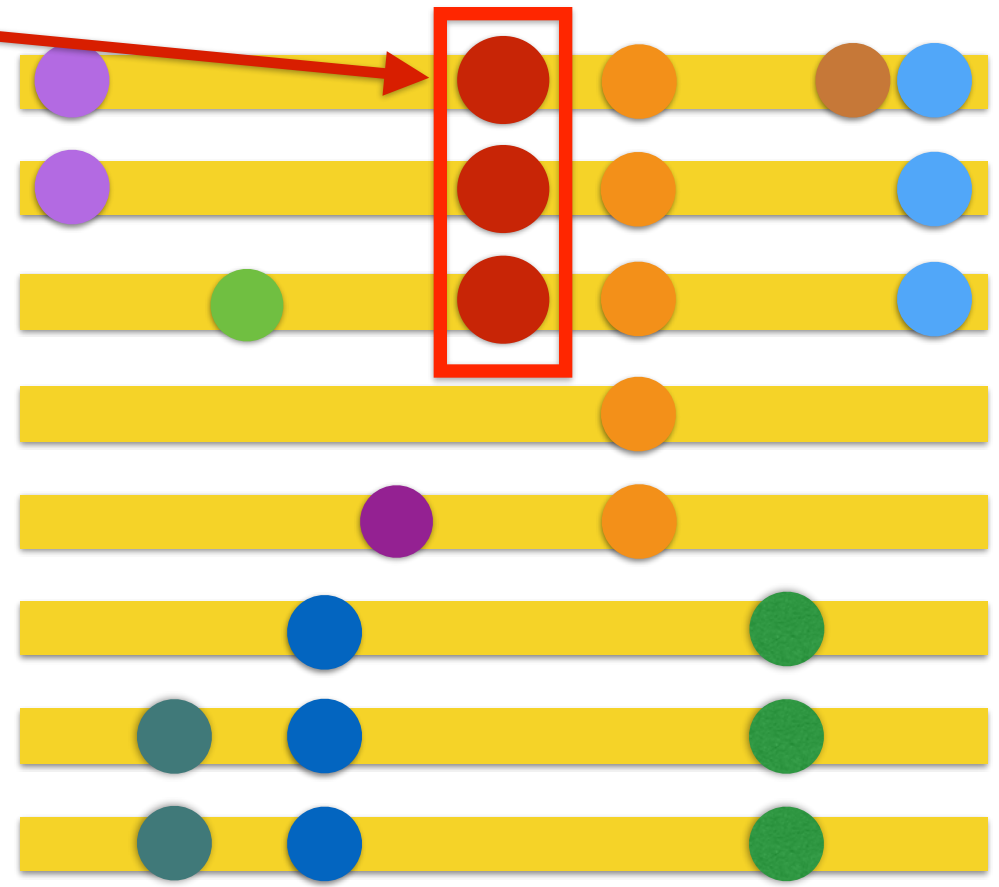


# Sudden environmental change! e.g. new viral strain

Resistant mutation




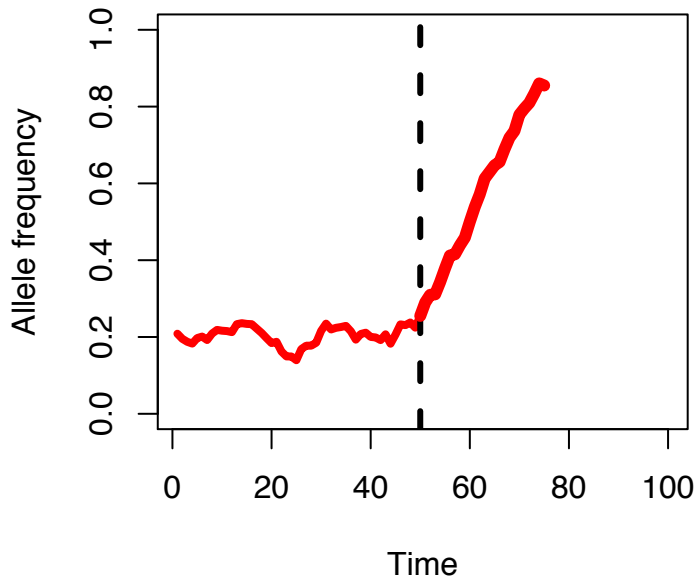
Mutations in a sample:



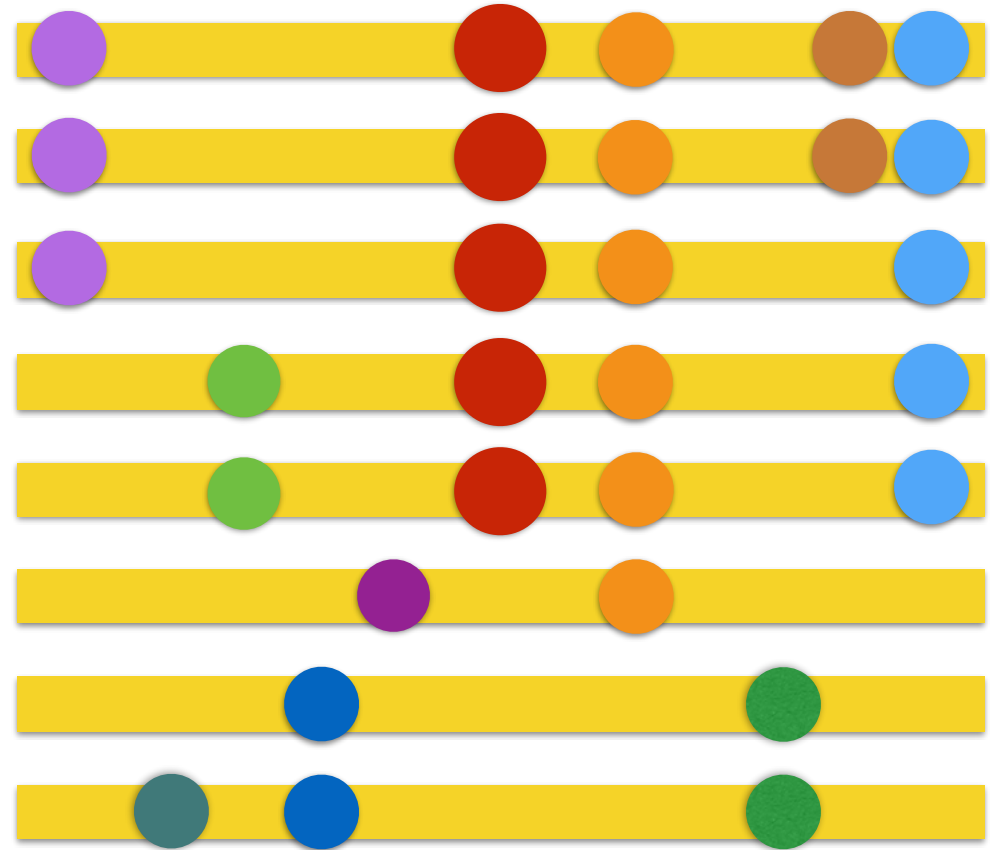
Selection on **standing variation**!

# Selection for resistance

Frequency of the  mutation in the population




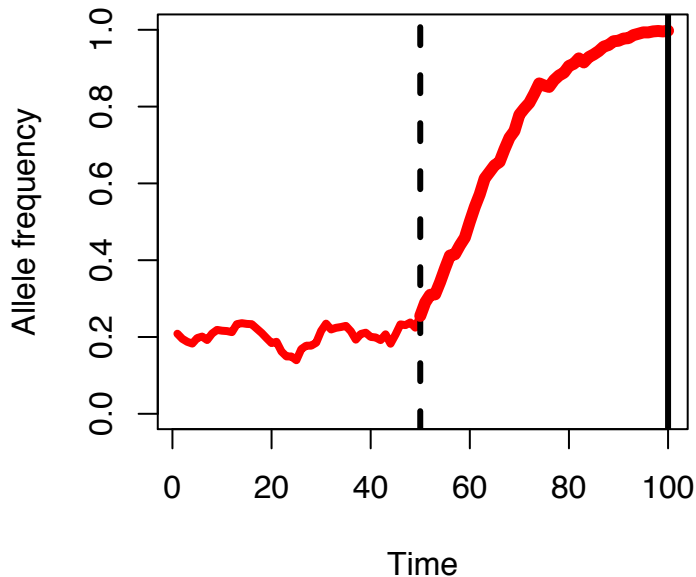
Mutations in a sample:



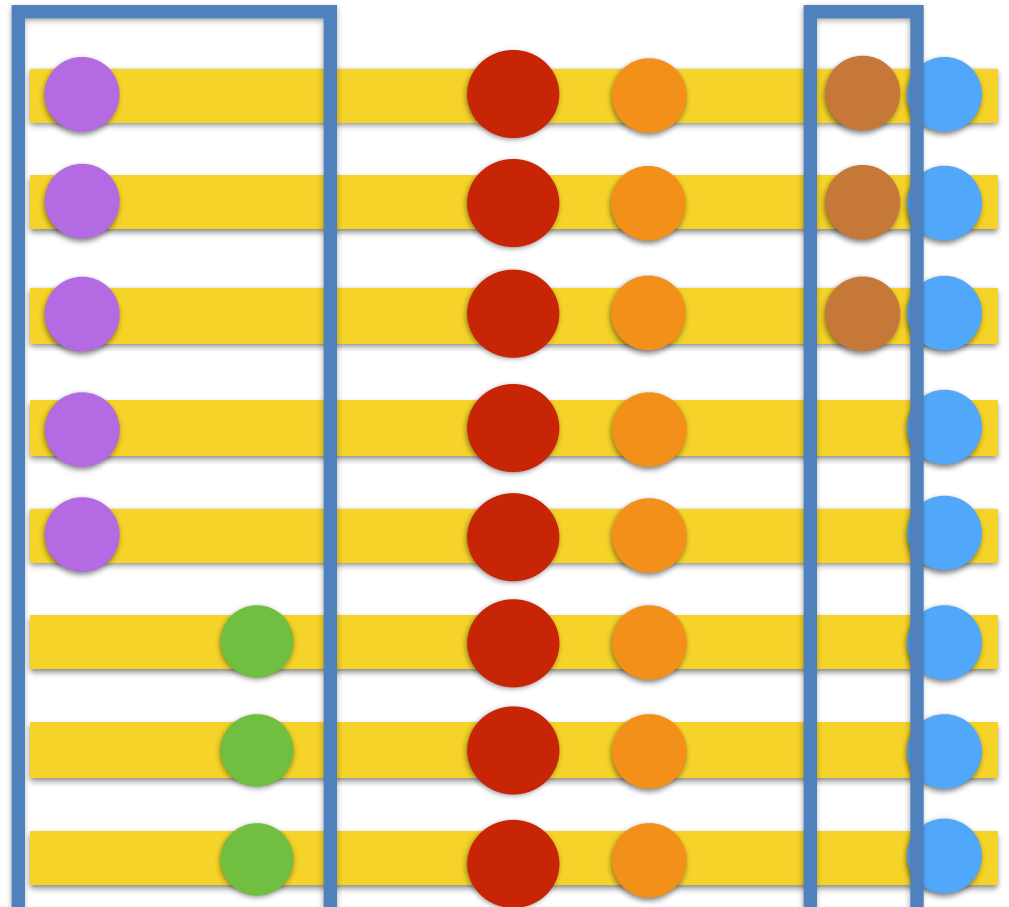
Selection on **standing variation!**

# Selection for **resistance**: *soft sweep*

Frequency of the  mutation in the population



Mutations in a sample:



Detected by pattern of sequence diversity



# From neutral spectrum to fast sweep

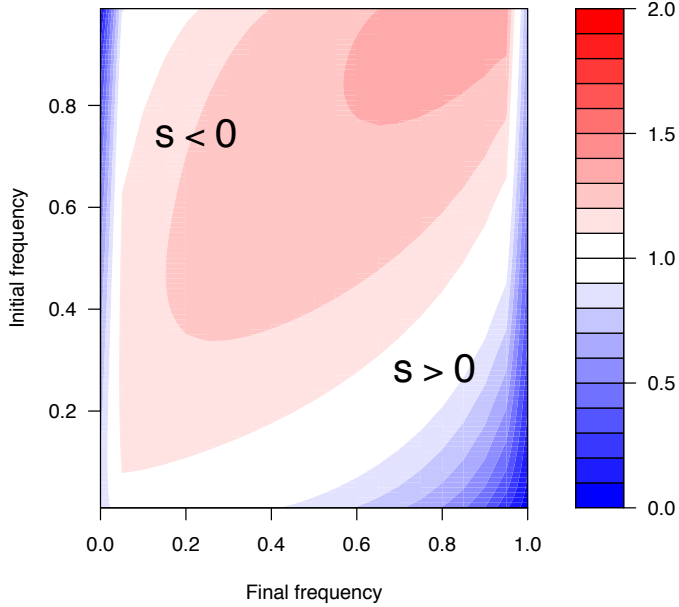
Selected allele changes frequency from  $f_0$  to  $f_s$

Rescale frequencies according to the component of the spectrum and the change in frequency of the selected allele:

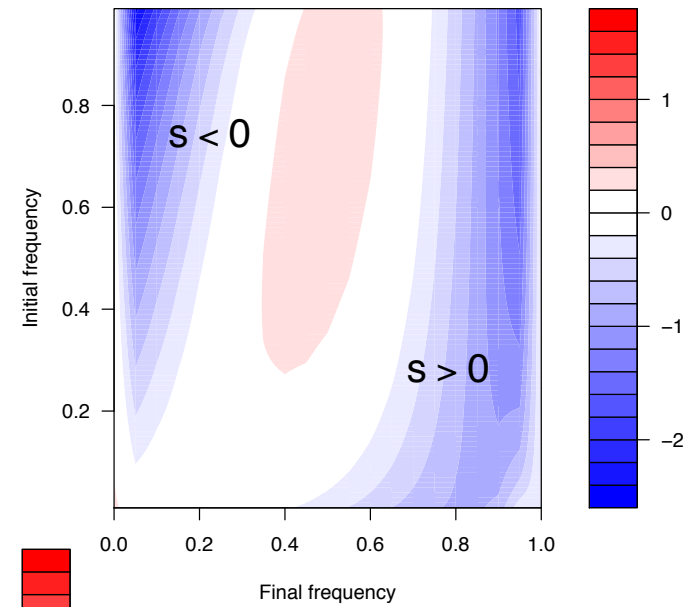
| Component     | Freq. 1st subpop. | Freq. 2nd subpop.     | Final frequency                      |
|---------------|-------------------|-----------------------|--------------------------------------|
| nested        | $f/f_0$           | 0                     | $f_s f/f_0$                          |
| co-occurring  | 1                 | 0                     | $f_s$                                |
| containing    | 1                 | $(f - f_0)/(1 - f_0)$ | $f_s + (1 - f_s)(f - f_0)/(1 - f_0)$ |
| complementary | 0                 | 1                     | $1 - f_s$                            |
| exclusive     | 0                 | $f/(1 - f_0)$         | $(1 - f_s)f/(1 - f_0)$               |

# Signatures of ongoing selection

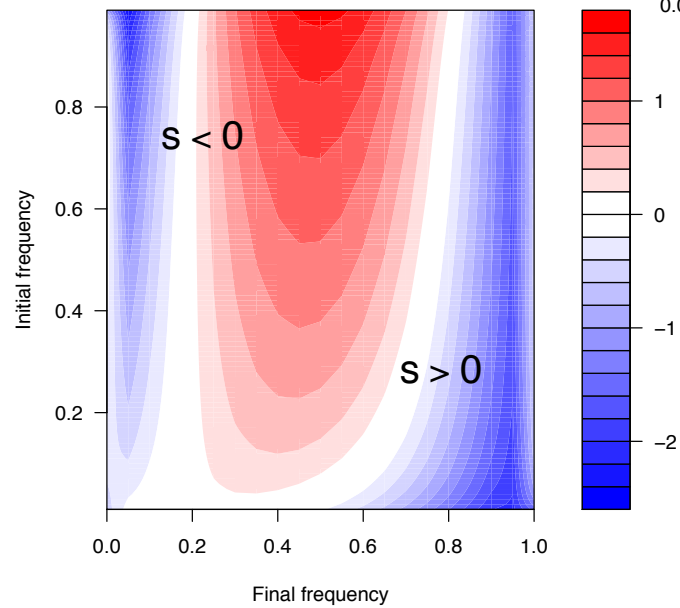
Watterson  $\theta_w$



Fay&Wu's H



Tajima's D



# Perspectives

- Composite Likelihood-Ratio Test for partial sweeps
- Maximum Composite Likelihood inference of the initial and final frequency of the sweep
- Similar methods applied to balancing selection
- Include recombination (approximate) and joint sweep finder with haplotype-based methods

# Acknowledgments

- Emanuele Raineri
- Thomas Wiehe
- Paolo Ribeca
- Adrià Madico Ferrer



**Thanks for your attention!**



# Frequency spectrum linked to a soft selective sweep

$$\xi^{soft}(f|f_0) = \theta L \cdot \frac{f_0^2}{(1 - ff_0)^2} \left( 1 + \frac{1}{ff_0} + \frac{2 \ln(ff_0)}{1 - ff_0} \right)$$

Applicable to selection on standing variation

