

Mosaïque @ Arcachon

## Which formal languages for natural languages?

(revision of a talk for Huet 60th birthday)

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## Survey with something new

- Formal syntax of natural language
- Natural language syntax with strings
- State of the art and discussion
- Tree languages for natural language
- The place of Ed Stabler's minimalist grammars in the hierarchy (very recent joint work with Gregory Kobele and Sylvain Salvati)

## Back to the origins of computational linguistics

Which formal languages  
for natural language syntax?  
(first strings, then trees)

## Two traditions

1. Logic and grammar
  - o Denis from Thrax (Alexandria, Byzance)
  - o Scholastics
  - o Frege, Montague, Lambek
2. Grammar and computation
  - o Panini
  - o Chomsky, Schutzenberger
3. Mixed (new in Computational Linguistics)  
Model theoretic syntax
  - o 60's TCS: Buchi, Doner, Thatcher,...
  - o 90's CL: Mönnich, Rogers, Morawietz, Pullum, ...

## Two traditions

1. Logic and grammar
  - ++ connexion to semantics
  - + learning
  - efficiency, complexity
2. Grammar and computation
  - ++ Complexity, (abstract) machines
  - Learning
  - Connexion to semantics

Me: 1 visiting 2

## Some ideas from generative grammar

- Language ≠ corpus  
He believes that (longest sentence)
- Language: set of unconscious rules  
evidence: learning overgeneralisation.  
Against learning by imitation.  
Why the child holded the baby rabbit
- Competence (rules) ≠ performance  
The wheat {that the rat [that the cat (that the dog chased) killed] ate} was poisonous.

## Some ideas from generative grammar

- Universal grammar / parameters explaining the acquisition paradox
- Movement / comparison between sentences  
Which book that Chomsky wrote did he like?  
He likes three books that Chomsky wrote.
- Syntax/semantics quantifiers  
possible impossible coreferences  
(affirmative: he and Chomsky non coreferent)

## Two principles from generative grammar

1. Fast (polynomial?) analysis  
Grammaticality is decided quickly by speakers
2. Learnable under some conditions
  - Knowing argument structure and root meaning
  - With interaction
  - With prosody
  - With positive examples only
  - Not that much positive examples
  - By iterated restrictions of the language

## Two mixable kinds of finite descriptions of a class of well-formed expressions.

- Formal Grammar
  - CFGs, TAGs, HPSGs, CGs,
- Logic, finite model theory  
Model Theoretic Syntax
  - CFGs, TAGs, CGs, CxGs, GP,...

## Two mixable kinds of finite descriptions of a class of well-formed expressions.

- Formal Grammar
  - Rules generating the potential infinity of sentences, structures,....
  - Computationally, Efficient,
  - Difficult to write and understand (especially if lexicalised)
- Logic, finite model theory  
Model Theoretic Syntax
  - The set of strings or terms satisfying a set of constraints -> degrees of grammaticality.
  - No natural underlying computational process.
  - Natural for linguistic descriptions, easy to write.

## String Grammars

Usual Hypotheses  
and current State of the Art

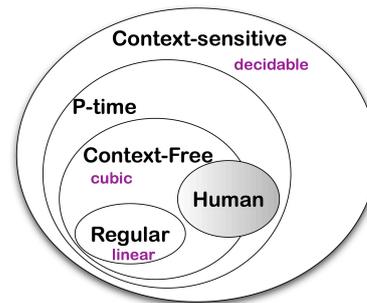
## Formal grammars

- T terminals, N non terminals
  - Rules  $W \rightarrow W'$  (W: at least one N)
- = {
- $W=W_1 Z W_2$  and  $W'=W_1 W'' W_2$   
context sensitive
  - $|W'| \geq |W|$  length increasing
  - $|W|=1$  context-free
  - $|W|=1$  and  $W'=mZ$  regular

## Which string languages?

- Center-embedded relatives  
 Pierre (que Pierre)<sup>n</sup> connaît<sup>n</sup> dort.  
 at least context-free.
- Dutch (Swiss-German) completives  
 ...dat ik<sub>1</sub> Henk<sub>2</sub> haar<sub>3</sub> de nijlpaarden<sub>3</sub>  
 zag<sub>1</sub> helpen<sub>2</sub> voeren<sub>3</sub>  
 ... that I<sub>1</sub> see<sub>1</sub> Henk<sub>2</sub> help<sub>2</sub> her<sub>3</sub> to feed<sub>3</sub>  
 the hippopotamuses

## The current hypothesis on human string languages



Challenged from time to time:

Michaelis & Kracht 96 old Georgian is not semi-linear

Kobele 06 Yoruba involves unbounded copying

## Mildly context sensitive languages

- First notion:
  - Tree Adjoining Grammars 1975 come back 1991
  - Combinatorial Categorical Grammars
- A larger one:
  - Multi-Component-TAG Weir
  - Minimalist grammars Stabler 1996
  - LCFRS Vijay-Shankar, Weir, Joshi, Seki, Matsumura, Fujii, Kasimi
- Large classe = P-time  
 Range Concatenation Grammars Boullier

## Discussion: complexity

- Recursion limited to two (or say five)
  - Computer = finite state automaton??
  - Speakers (with extra processing time) accept nested sentences
  - Rules are stated like this by speakers, books, ...
  - Economy of the description

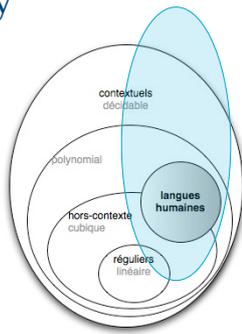
## Discussion: word order

- Models of strict word orders, what about more free word order (e.g. with rich morphology, Latin, Russian, Sanskrit)
  - Standard answer: there is a canonical order from which other are derived and it induces semantic nuances
  - A hidden answer: it is much simpler to work with total orders than with partial orders!!

## Discussion: acquisition

- Acquisition condition left out... but very important
  - for understanding human language faculty
  - for building large grammars from corpora.
- Exception: categorial grammars can be learnt:
  - lexicalized
  - structured types -> unification

## Learnable languages in the Hierarchy



## Discussion: local state of the art

- Richard Moot MMCG: extraction, parsing
  - NWO Dutch Spoken Corpus (spontaneous conversation, annotated transcript)
    - 1.002.098 word occurrences
    - 114.801 phrases (7,6 words per sentence)
    - 44.306 different word forms
  - Multi-Modal Categorical Grammar, acquired from the corpus (average 100 trees per word!)
  - Supertagging (n-most likely sequences of trees corresponding to the words in the sentence)
  - Results on test corpus 19.237 sentences 146.497 words (supertagging >> parsing):
    - 1 supertag 2'53" 40% correct (9 ms/sent., 1.18 ms/wd)
    - 10 best supertags 48'34" 70% correct (151ms/sent., 20ms/wd)

## Discussion: local state of the art

- Benoît Sagot, Eric de la Clergerie LFG parsing
  - Corpus EASy (Evaluation des Analyseurs Syntaxiques) Newspapers, web, mail, political speeches, literature....
    - 87177 word occurrences
    - 4322 sentences (20,2 words per sentence)
  - Handwritten LFG grammar
  - Selects one parse per sentence
  - Parsing time: total 152s, 35ms/sentence 1,7ms/word
    - Correct chunks: 86%
    - Correct relations: 49%

## Discussion:how to compare two different practical states of the art

- |   |   |
|---|---|
| 1. Mainly written                         | 1. Spoken                                       |
| 2. Rather long sentences ~ 20 words       | 2. Very short but tricky sentences <10 words    |
| 3. Flat annotations                       | 3. Deeply annotated                             |
| 4. Hand written grammar                   | 4. Automatically acquired grammar               |
| 5. Lexical Functional Grammar             | 5. MultiModal Categorical Grammar               |
| 6. Correctness measure: results on chunks | 6. Correctness results on whole parse structure |

## Tree grammars

- Strings are not enough:
  - For learning
  - For interpreting sentences
- Graphs (proof-nets of categorial grammars, dependency graphs) would be much welcome .....but let's start with trees.

## Tree grammars

(that I am just discovering, be indulgent)

## Context-free tree grammars (Engelfriet after Fisher)

- A ranked signature of terminals
- A ranked signature of non-terminals
- Productions rules of the form
 
$$A(x_1, \dots, x_n) \rightarrow t(x_1, \dots, x_n)$$
  - where  $A$  non terminal of arity  $n$
  - where  $t$  tree over terminals and non terminals with variables  $x_1, \dots, x_n$

## Regular Tree Grammars Thatcher, Doner, 1967

- Rules only for non-terminals of rank 0 rewrite (ONLY LEAVES rewrite)
- These tree languages exactly are the ones definable in monadic second order logic
- Their yields are context free strings languages

## Context Free Tree Grammars Fisher 1968, Engelfriet 1977

- **OI** (~ unrestricted) only the highest non terminal undergo rewriting.  
Strings: indexed languages
- **IO** only the lowest non terminals undergo rewriting.  
Strings: LCFRS (incomparable)
- Monadic (always a single NT)  
**CFTG (IO=OI) ~ TAG derived trees**  
Mönnich 1996

## Context free Hyper Edge Replacement Grammars Courcelle 1987, Engelfriet

- Non terminal: hyper edges (ordered with possible repetitions)
- External vertices
- Replace an hyper edge with one with the same external vertices, possibly with new hyperedges linking them

## Where are the tree languages that I like?

Categorial grammars  
Minimalist grammars

## Categorial grammars

- Old notion: parse tree: any proof tree any bracketting is possible...
- Normal natural deduction only (Tiede)
- Non associative Lambek grammars
  - RTG Tiede (?), Kandulski
  - ACG encoding Salvati Retoré
- Associative Lambek grammars
  - RTG are not enough (despite CFL only)
  - CFTG Salvati september 2007

## Stabler's minimalist grammars

- Close to categorial grammars or linear logic but much richer
- Implements Chomsky's minimalist program
- Lexicalised
- Two operations
  - Merge (binary)
  - Move (unary)

## Minimalist grammars

- Trees with a head "<" or ">" on internal nodes, indicating where the head is.
- Complete trees: a single  $\epsilon$  on the head, only words on other leaves
- Sequences of features on the leaves
  - Selection  
d n v .....  
=d =n =v .....
  - Movement  
+wh +k ....  
-wh -k ...

Lexical items sequence of features associated with a word, possibly empty

## Minimalist grammars

- Merge
  - a tree  $t$  with head  $=x w$
  - Another tree  $t'$  with head  $xw'$
- Result  
suppress the  $x$  and  $=x$  yielding  $\bar{t}$  and  $\bar{t}'$   
the selector  $s$  is the head  
the selected is not  
 $<(\bar{t}; \bar{t}')$  if  $t$  is lexical (a leaf)  
 $>(\bar{t}'; \bar{t})$  if  $t$  is a real tree

## Minimalist grammars

- Move
  - a tree  $t[t']$  with head  $+f w$  and a subtree  $t'$  with head  $-f w$
- Result  
suppress the  $+f$  and  $-f$  yielding  $t$  and  $t'$   
the context is the head  
 $>(\bar{t}'; \bar{t}[\epsilon])$

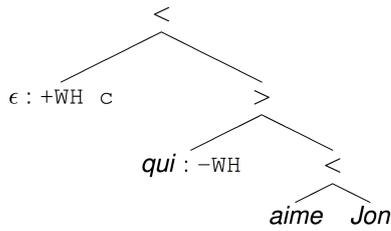
## Minimalist grammars: lexicon

Jon : d  
 aime : =d =d v  
 qui : d -WH  
 $\epsilon$  : =v +WH c

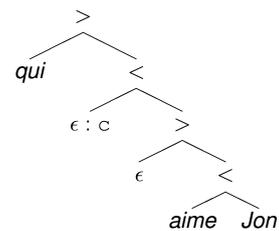
## Minimalist grammars: merge

$aime : =d =d v + Jon : d$   
 $\downarrow$   
 $<$   
 $aime : =d v \quad Jon$

## Minimalist grammars: merge



## Minimalist grammars: move



## Shortest move condition SMC

- Chomsky: whenever two subtrees (-f) are competing for a movement triggered by (+f), the one closest to the attractor (+f) moves.
- Stabler: whenever two subtrees (-f) are competing for a movement triggered by (+f), the derivation crashes. Strong SMC !

## Minimalist tree languages in the hierarchy

As the image by a transducer of a regular language

## Two step description

de Mönnich, Morawietz, Michaelis

- If minimalist tree languages are complicated, can we describe them as the image by a simple mechanism of a simple set of tree languages.
- MG->MCFG
- Lift -> RTG (derivation trees)
- Walking Tree Automaton computing dominance, precedence of the MG derived trees

## A simpler and lower description

Kobele, Retoré, Salvati

- Derivation trees (regular set):  
lexical, move( $\_$ ) merge ( $\_$ , $\_$ )  
Tree tuples  
[main tree, ( $-f_1$  subtree), ..., ( $-f_n$  subtree)]  
Strong SMC at most one subtree per  $f_i$
- Eliminate the derivations that fail (still regular)
- Defined move and merge on tuples of trees
- Can be done with a Linear Deterministic Mult. Bottom-Up Tree Transducer

## Merge with tuples of trees

$(t_0 [= xw], t_1, \dots, t_n) \quad (t'_0 [xm], t'_1, \dots, t'_n)$

- Compute  $< (t_0, t'_0) \text{ or } > (t'_0, t_0)$
- Put the trees in the tuple, and if there are two trees whose head starts with the same -f, the derivation crashes. (Strong Shortest Move Condition)

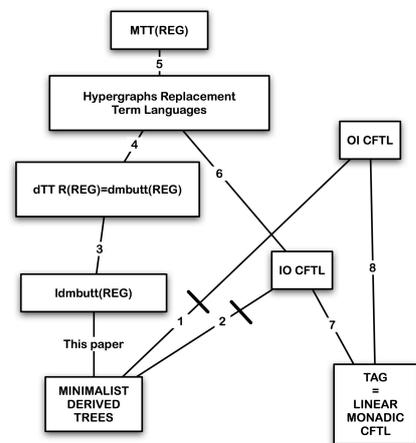
## Move with tuples of trees

$(t_0 [+fiw], t_1, \dots, t_i [-fm], \dots, t_n)$

- Compute  $> (t_i, t_0)$
- Put the trees in the tuple, and if there are two trees whose head starts with the same -f, the derivation crashes. (Strong Shortest Move Condition)

## Interpreting this result

- Filtering the wrong derivation tree is linear (bottom up automaton)
- The computing of the derived tree ensures to be included into HR CFG (technical horrible reason: a top-down tree transducer with regular look-ahead and finite copying can do what a linear deterministic multi bottom up tree transducer does)



## Conclusion

- Admittedly, little is known, but we're learning and starting to clear the picture.
- At least we know where stand a formalisation of a/the main linguistic theory
- Improving the connexion between logical formalisms and rewrite formalisms
  - Syntax / Semantics correspondence
  - Parsing efficiency (kind of compilation)
- The need for two kinds of descriptions:
  - Model Theoretic Syntax: linguistic description
  - Derivational syntax: processing

## Some references

- Edward Stabler A derivational approach to minimalism. LACL Springer 1996
- James Rogers A descriptive approach to language complexity CSLI 1998
- Frank Morawietz Two step approaches to natural language formalism Mouton de Gruyter 2003
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