

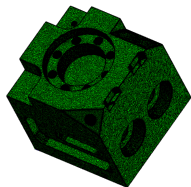
# Digitized 3D mesh segmentation based on curvature analysis

S. Gauthier<sup>1,2</sup>

R. Bènière<sup>2</sup>

W. Puech<sup>1</sup>

G. Subsol<sup>1</sup>

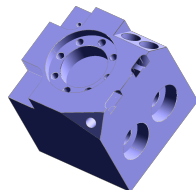


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<sup>2</sup>C4W, Montpellier, France

silvere.gauthier@lirmm.fr

February 02, 2017

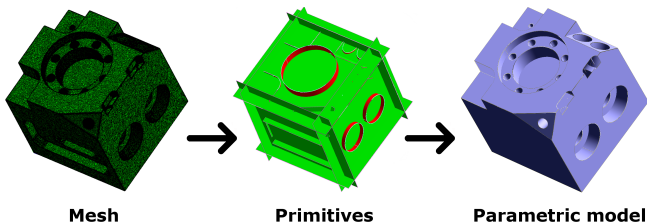



# Context

## Reverse Engineering

Study of an object to determine its functioning or manufacturing method.

⇒ Reconstruction of a 3D parametric model (combination of geometric primitives) from a discrete one (3D mesh).



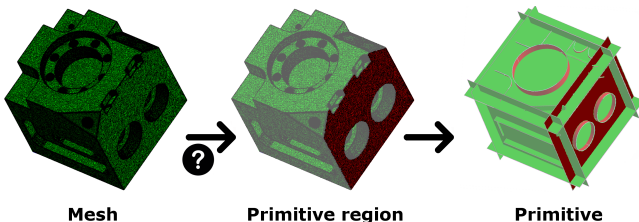
 R. Bénére, G. Subsol, G. Gesquière, F. Le Breton, and W. Puech. A comprehensive process of reverse engineering from 3D meshes to CAD models. *Computer-Aided Design*, 45(11), 2013.

# Context

## Reverse Engineering

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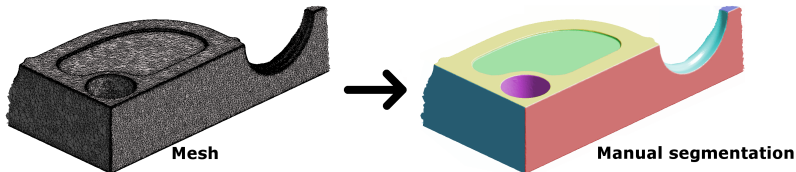
- **Problem:** how to define precisely primitive regions?

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📄 R. Bénéière, G. Subsol, G. Gesquière, F. Le Breton, and W. Puech. A comprehensive process of reverse engineering from 3D meshes to CAD models. *Computer-Aided Design*, 45(11), 2013.

# Segmentation

- **Solution:** segment the 3D mesh in homogeneous regions corresponding to the primitives.



## Segmentation

Many methods exist but not efficient enough for our application.

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📄 A. Shamir. A survey on mesh segmentation techniques. *Computer Graphics Forum*, 27(6):1539-1556, 2008.

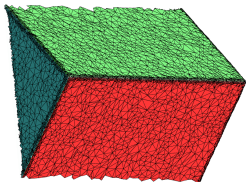


# Segmentation

Primitives are separated by “edges”.

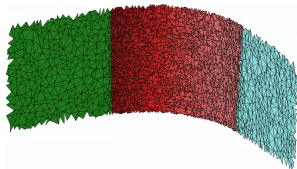
- **Idea:** Extract object edges to delimit homogeneous regions by a method based on surface curvature ( $k_1, k_2, k_g, k_m$ ).

“Sharp” edges



Curvature discontinuity

“Smooth” edges

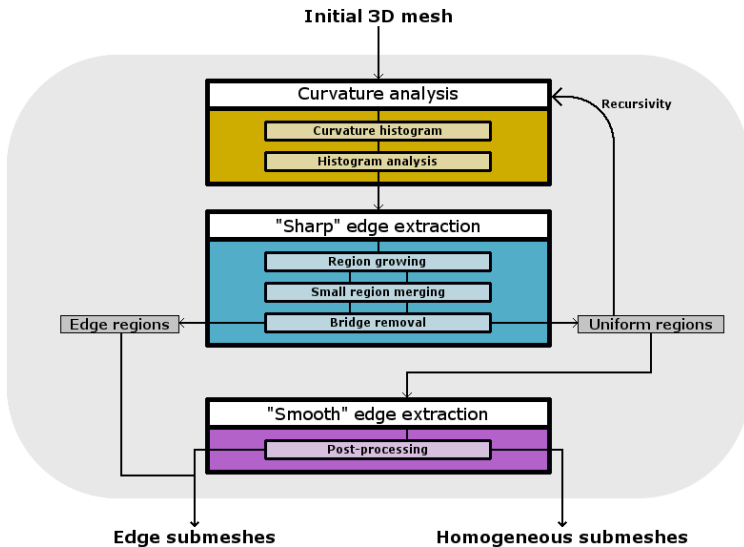


Curvature continuity

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  - “Sharp” edge extraction
  - Recursivity
  - “Smooth” edge extraction
- 3 Experimental results
- 4 Conclusion and perspectives

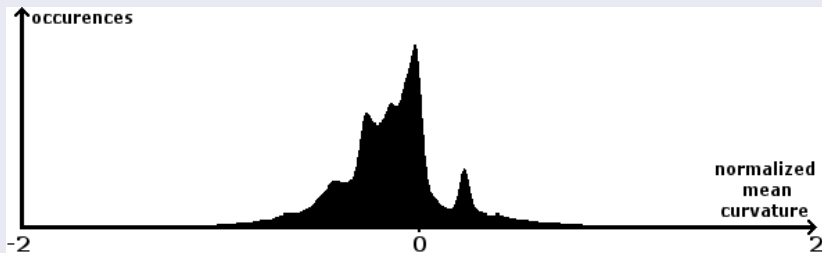
# Method overview



# Curvature analysis

## Curvature histogram

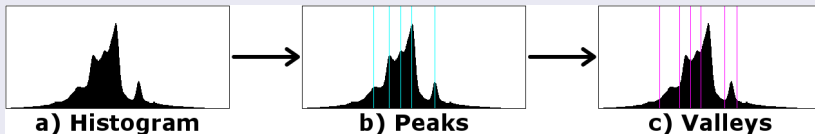
- Compute mean curvature at each vertex of the 3D mesh
- Normalize curvature values using the average edge length
- Construct a histogram using a Gaussian kernel estimation



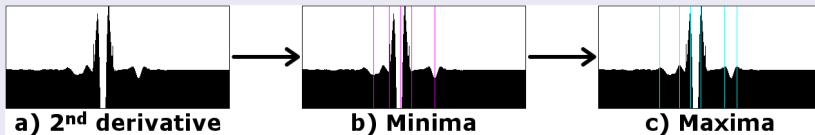
# Curvature analysis

## Histogram analysis

- Detect positions of “peaks” and “valleys”



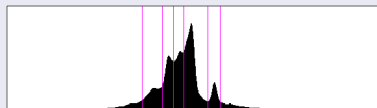
- Local minima in second derivative correspond to peaks in histogram
- Local maxima in second derivative correspond to valleys in histogram



# Curvature analysis

## Curvature thresholding

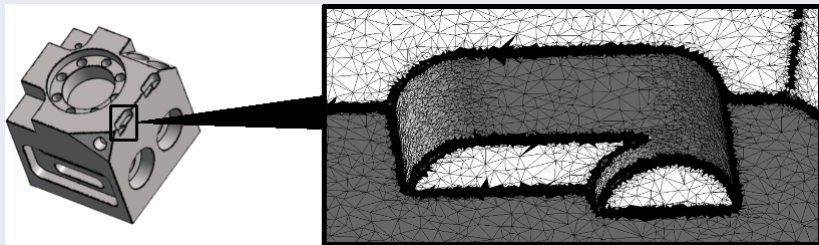
- Use extremal valleys as curvature thresholds



a) Valleys



b) Segmentation thresholds



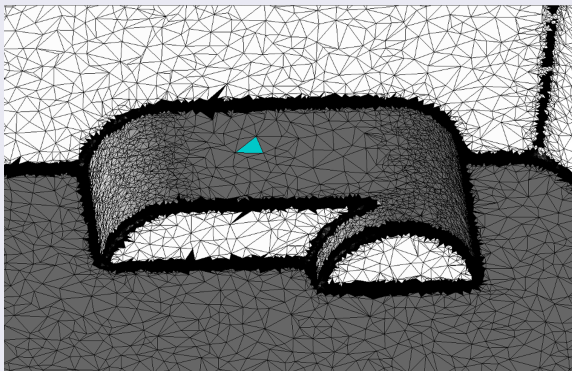
$]T_1, T_2[ \rightarrow$  homogeneous triangles (white)

$] -\infty, T_1[ \cup ]T_2, +\infty[ \rightarrow$  edge triangles (black)

# “Sharp” edge extraction

## Region growing

- Retrieve homogeneous and “edge” regions by propagation

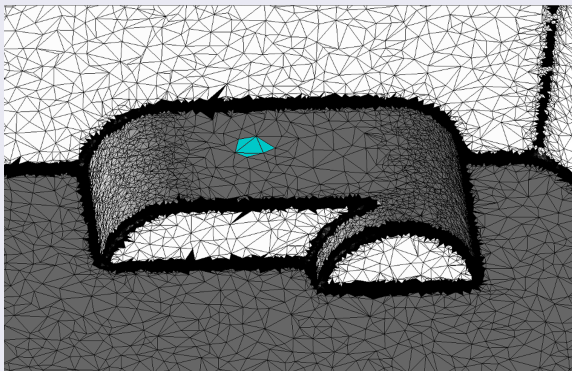


Take a triangle and assign a unique ID

# “Sharp” edge extraction

## Region growing

- Retrieve homogeneous and “edge” regions by propagation



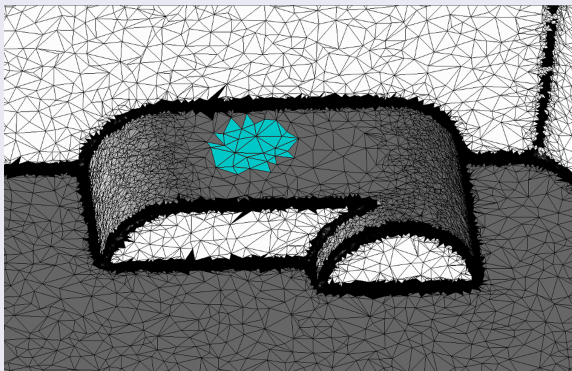
Propagate ID on its neighbors



# “Sharp” edge extraction

## Region growing

- Retrieve homogeneous and “edge” regions by propagation

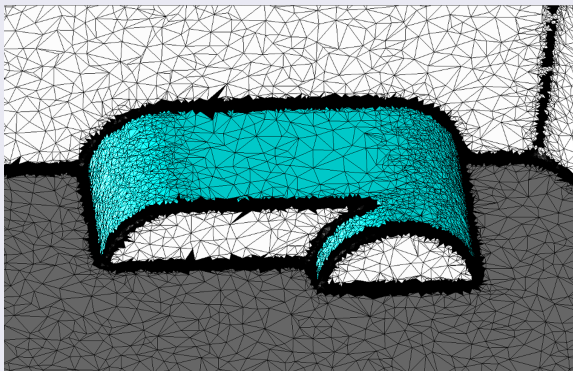


Propagate ID on its neighbors

# “Sharp” edge extraction

## Region growing

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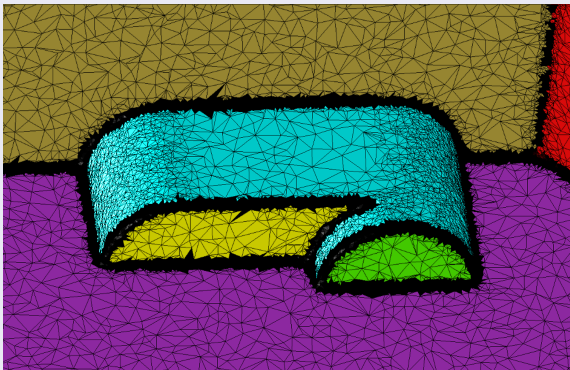


Until it reaches “edge” triangles

# “Sharp” edge extraction

## Region growing

- Retrieve homogeneous and “edge” regions by propagation

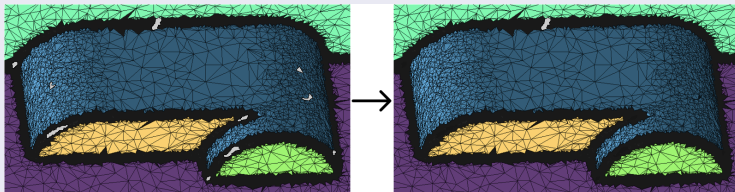


Start again with a new triangle until all triangles are processed

# “Sharp” edge extraction

## Over-segmentation: small region merging

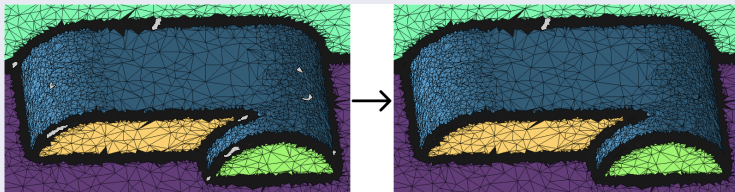
- Merge small regions included in larger ones



# “Sharp” edge extraction

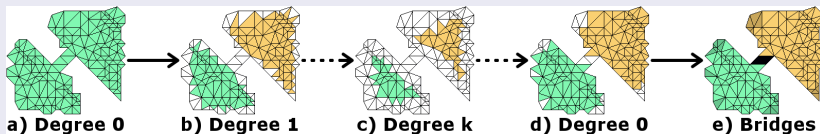
## Over-segmentation: small region merging

- Merge small regions included in larger ones



## Under-segmentation: bridge removal

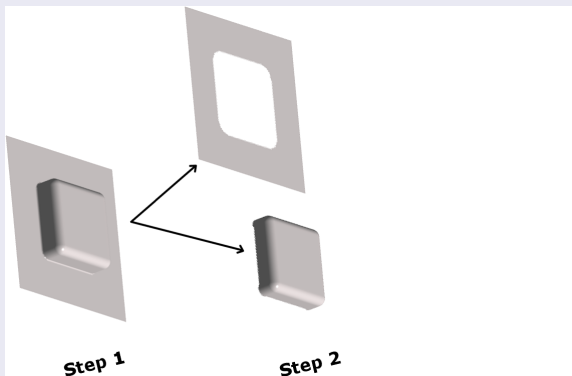
- Separate regions connected by thin strips of triangles



# Recursivity

## Recursive segmentation

- Start the process again on each region, with an updated histogram
- Stop when only one homogeneous region is found

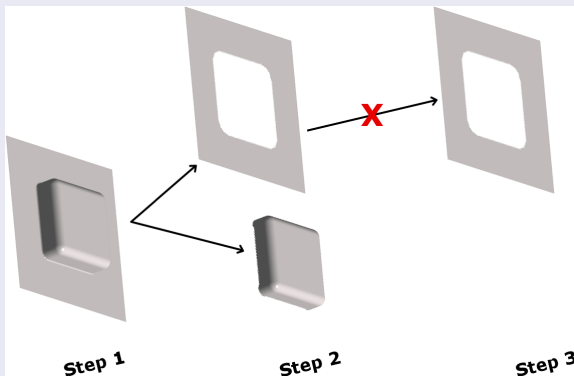


Adaptive parameters at each step

# Recursivity

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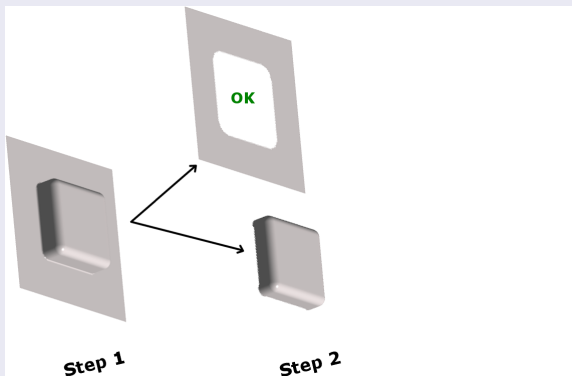


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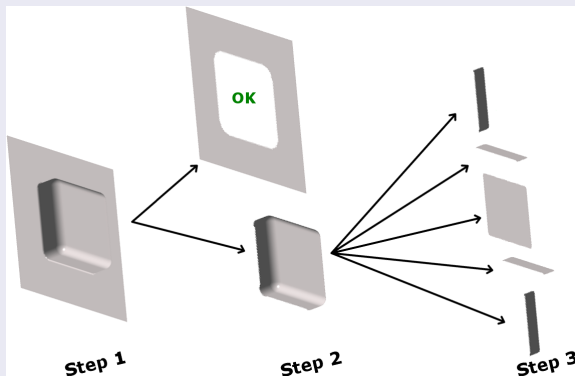
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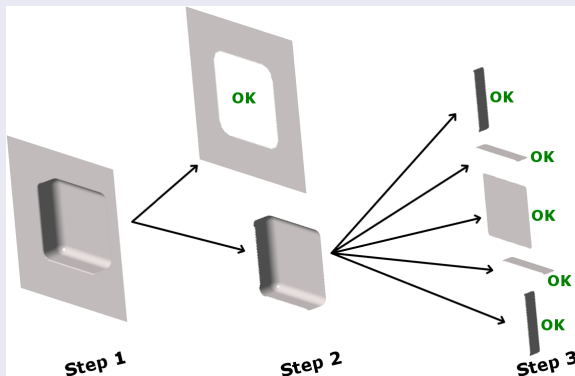


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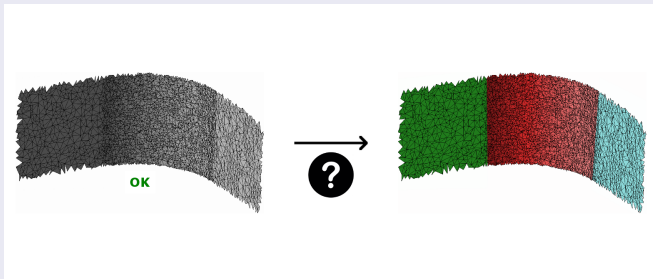


Adaptive parameters at each step

# “Smooth” edge extraction

## Multiple curvature thresholding

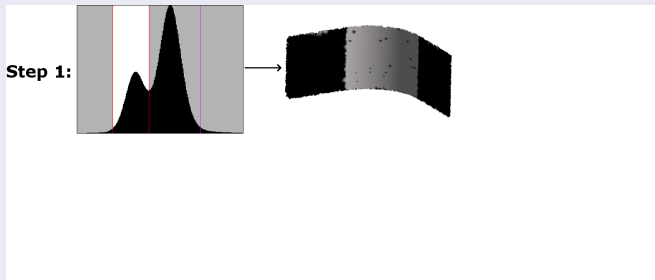
- Compute an updated curvature histogram for each region
- Separate homogeneous regions by a multiple thresholding
- Apply our segmentation process at each step (without recursion)



# “Smooth” edge extraction

## Multiple curvature thresholding

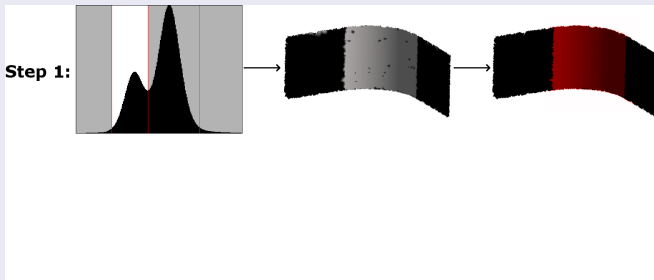
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# “Smooth” edge extraction

## Multiple curvature thresholding

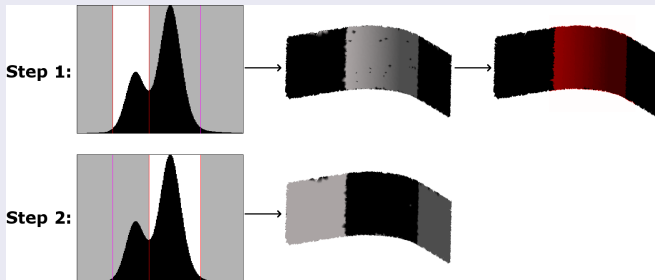
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# “Smooth” edge extraction

## Multiple curvature thresholding

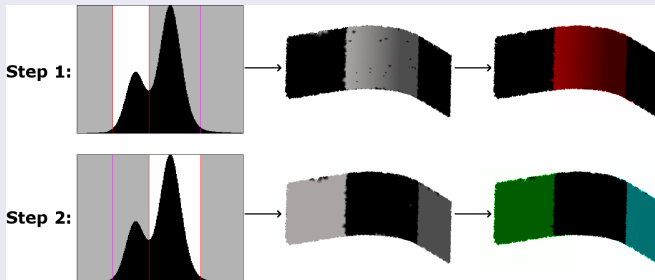
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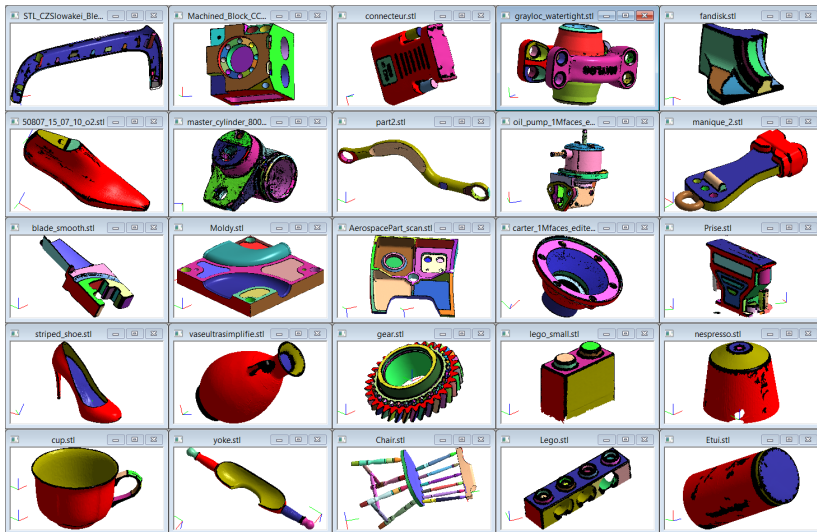


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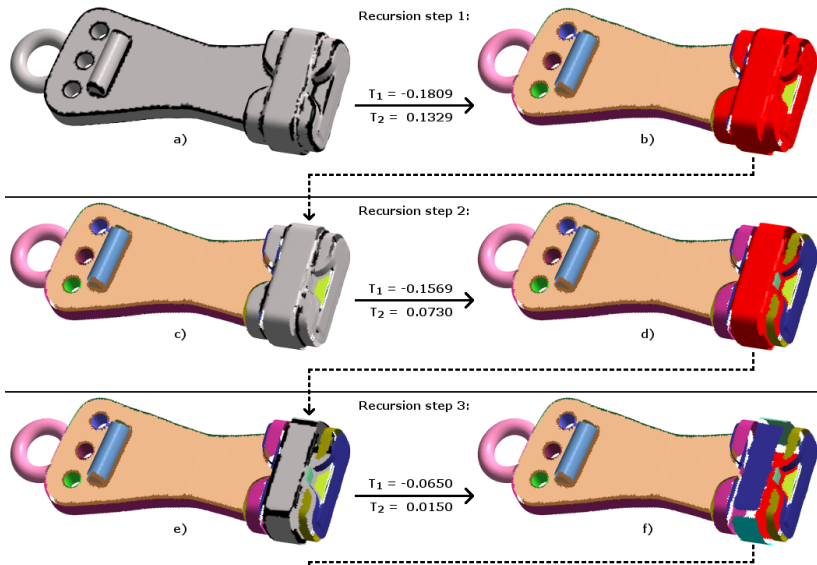


# Experimental results

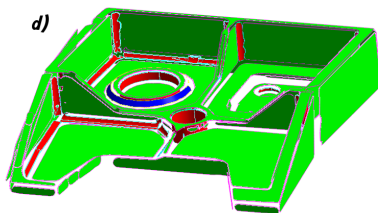
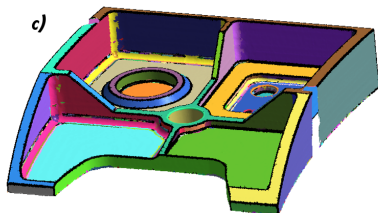
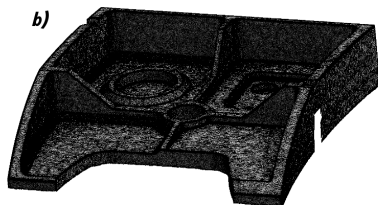
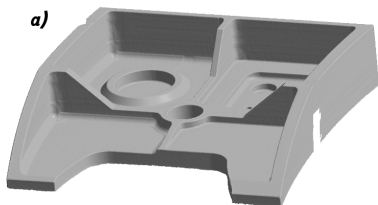


From 20,000 to 2,500,000 triangles — Different surface scanning devices — Heterogeneous noise

# Recursivity example

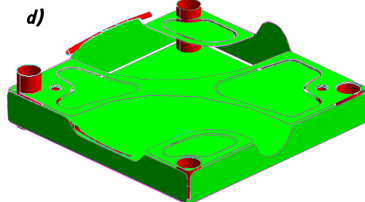
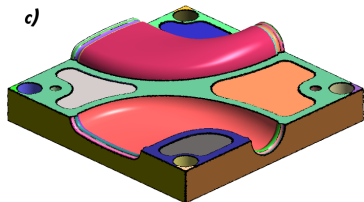
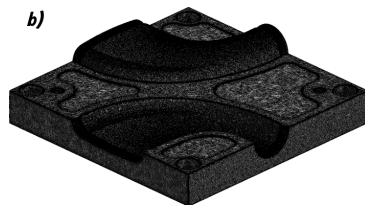
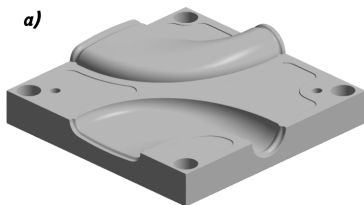


# Back to context



**Segmentation:** 799 296 triangles — 16 seconds — 70 regions — 94.3% with only one primitive

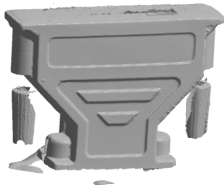
# Back to context



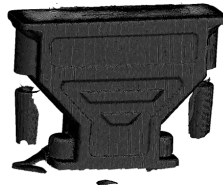
**Segmentation:** 851 194 triangles — 13 seconds — 48 regions — 100% with only one primitive

# Back to context

a)



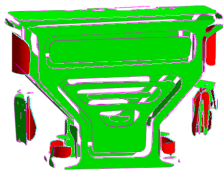
b)



c)



d)



**Segmentation:** 195 853 triangles — 5 seconds — 72 regions — 100% with only one primitive

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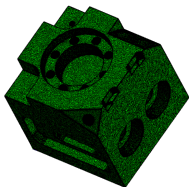
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# Conclusion

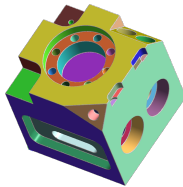
## Results

### Segmentation:

- Fast: 10-30 seconds for 1 million triangles
- Adaptive: compute parameters from input data at each step
- Automatic: no user action



Mesh



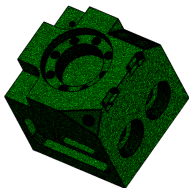
Submeshes

# Conclusion

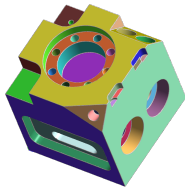
## Results

### Reverse engineering:

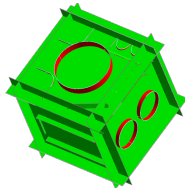
- Around 96% of obtained submeshes contain only one primitive
- Reduce computational cost (40 to 80%)
- Improve reconstruction accuracy (+50%)



Mesh



Submeshes



Primitives



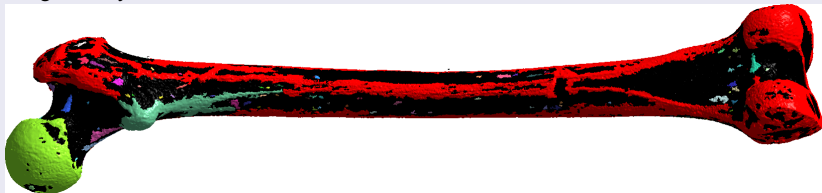
# Perspectives

## Accuracy

Optimize some parameters, like bin number for histogram construction.

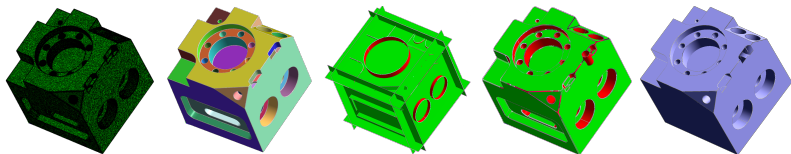
## Extensibility

Adapt our approach for natural objects, for example to use it for medical image analysis.



# Thank you

## Some questions?



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**Silvère Gauthier**, R. Bénéière, W. Puech, G. Pouessel, G. Subsol,  
*Digitized 3D mesh segmentation based on curvature analysis*, 2017

