# Active Tremor Compensation in Handheld Instrument for Microsurgery





School of Mechanical & Aerospace Engineering Nanyang Technological University Singapore wtang@ntu.edu.sg



## Contributors

Cameron N. Riviere
 Associate Research Professor





Si Yi Khoo

Research Engineer

Medical Robotics Technology Center The Robotics Institute Carnegie Mellon University Pittsburgh, PA, USA  Wei Tech Ang Assistant Professor



Mounir Krichane
 Exchange Student (EPFL)



Robotics Research Centre & Sch. of Mechanical & Aerospace Eng. Nanyang Technological University Singapore



## Microsurgery with Active Handheld Instrument





### Vitreoretinal Microsurgery

 Removal of membranes ≤ 20 µm thick from front or back of retina







Vitreoretinal Microsurgery

 Injection of anticoagulant using intraocular cannulation to treat retinal vein (~Ø100 µm) occlusion





## Vitreoretinal Microsurgery

#### Tremor: under microscope





# Involuntary Hand Movement and Microsurgery





# Involuntary Hand Movement and Microsurgery

- Complicate microsurgical procedures and makes certain delicate interventions impossible
- Impact on microsurgeons
  - □ 2 of 10 surgeons become microsurgeons
- Factors affecting tremor
  - □ Fatigue strenuous exercise etc.
  - Caffeine/alcohol consumption
  - □ Lack of practice long vacation etc.
  - □ Age experience vs hand stability
- Microsurgeons' consensus:
  - 10 μm positioning accuracy



## Involuntary Hand Movement of Healthy Human

- Physiological Tremor
  - Roughly sinusoidal motion, 8-12 Hz
  - □  $\leq$  50 µm rms in each principal axis
- Non-tremulous Errors
  - Myoclonic jerk, drift etc.
  - Aperiodic, may be in the same frequency band as voluntary motion
  - Larger amplitude: > 100 µm





## Microsurgery with Active Handheld Instrument





### Robotic Error Compensation Approaches

- Telerobotic systems: Zeus (Computer Motion) & Da Vinci (Intuitive Surgical)
  - Master-Slave manipulators
- Erroneous motion filtered by motion scaling



Computer Motion, Inc.





### Robotic Error Compensation Approaches

- 'Steady-hand' robot: Russell Taylor et al., Johns Hopkins University
  - Surgeon and compliant robot hold tool simultaneously
  - Force feedback
  - 'Third hand' operation
- Erroneous motion damped by rigidity of robot





### Robotic Error Compensation Approaches

 Active Handheld Instrument:
 Paolo Dario,
 Scuola Superiore
 Sant'Anna, Pisa,
 Italy

Same concept





### Comparison of Robotic Solutions

#### Telerobotics

- Steady Hand' robot
- Active Handheld Instrument
  - ✓ Cheap
  - ✓ Unobtrusive
  - ✓ Safer
  - Limited workspace
  - No motion scaling
  - No 'third hand'

> US
$$1M$$
  
> US $150K$   
 $\leq$  US $15K$   
Unobtrusive

Obtrusive



## Micron Current Prototype

- Length: 180 mm long
- Diameter: Ø20(16) mm
- Weight <100 g</p>
- 9 DOF inertial and magnetic sensing system at the back end
- 3 DOF piezoelectric driven parallel manipulator at front end with disposable surgical needle





# System Overview





## Microsurgery with Active Handheld Instrument





# Sensing System Design

- Magnetometer-aided allaccelerometer inertial measurement unit (IMU):
  - 3 dual-axis miniature MEMS accelerometers
     Analog Devices ADXL-203: 5mm x 5mm x 2mm, < 1g</li>
  - Three-axis magnetometer Honeywell HMC-2003: 26mm x 19mm x 12mm, <10g</li>
- Housed in 2 locations





# Sensing Modality

#### Internally referenced sensors because:

- Less obtrusive
  - Externally referenced sensors require a line of sight
- Resolution:
  - Inertial sensor < 1  $\mu$ m
  - Externally referenced (e.g. Optotrak): ~ 0.1 mm
- All accelerometers because:
  - Low cost, miniature gyros too noisy
    - $\rightarrow$  Poor sensing resolution
  - Navigation/tactical grade gyros too expensive and bulky



### Differential Sensing Kinematics





## Differential Sensing Kinematics

3 unknowns:

 $\Omega = [\omega_x \ \omega_y \ \omega_z]^T$ 3 differential acceleration measurements:

 $A_D = [a_{13x} \ a_{23y} \ a_{12z}]^T$ 

- Solve system of nonlinear equations by Gauss-Newton or Levenberg-Marquart method
- Numerical instability
  - □ Assume  $\Omega^2 \approx 0$ , solve for  $\dot{\Omega}$  analytically





## Sensing Kinematics

Updating quaternions:

$$\dot{q}(t) = \widetilde{\Omega}(t)q(t), \ \widetilde{\Omega} = \frac{1}{2} \left[ \frac{\left[\Omega \times \right]_{3\times 3}}{-\Omega_{1\times 3}^{T}} \left| \frac{\Omega_{3\times 1}}{0} \right]$$

Directional Cosines matrix

$${}^{W}C_{B} = \begin{bmatrix} q_{0}^{2} + q_{1}^{2} - q_{2}^{2} - q_{3}^{2} & 2(q_{1}q_{2} - q_{0}q_{3}) & 2(q_{1}q_{3} + q_{0}q_{2}) \\ 2(q_{1}q_{2} + q_{0}q_{3}) & q_{0}^{2} - q_{1}^{2} + q_{2}^{2} - q_{3}^{2} & 2(q_{2}q_{3} - q_{0}q_{1}) \\ 2(q_{1}q_{3} - q_{0}q_{2}) & 2(q_{2}q_{3} + q_{0}q_{1}) & q_{0}^{2} - q_{1}^{2} - q_{2}^{2} + q_{3}^{2} \end{bmatrix}$$

- Gravity Removal:  ${}^{W}A_{E} = {}^{W}C_{B}{}^{B}A {}^{W}g$
- Tip Displacement:

$${}^{W}P_{tip}(t) = {}^{W}P_{tip}(t-T) + \int_{t-T} \int_{t-T}^{t} {}^{W}A_{E}(\tau)d\tau d\tau + {}^{W}C_{B}(t)[{}^{B}\Omega \times ]^{B}P_{tip}$$



## Sensing Resolution (Error Variance) Analysis

- Sensing resolution dependent on sensor noise floor
- Angular Sensing
  - Sensing equation:

$$A_{ij} = f(\Omega) = ([\Omega \times] [\Omega \times] + [\dot{\Omega} \times])P_{ij}$$

Covariance:

$$C(A_{ij}) = C(\Omega) P_{ij}$$
$$P_{ij} \uparrow, C(\Omega) \downarrow$$





Proposed All-Accelerometer vs Conventional Inertial Measurement Unit

- All-accelerometer IMU
  - Maximized  $P_{ij}$ , with physical constraint of a slender handheld instrument
- Conventional IMU (3A-3G)
  - □ Tokin CG-L43D rate gyros x 3

	3G-3A Error std. dev. (deg/s)	6A Error std. dev. (deg/s)	Noise reduction / resolution improvement
$\omega_x \& \omega_y$	1.41	1.08 × 10 <sup>-2</sup>	99.3% / 130x
$\omega_{z}$	1.41	4.42 × 10 <sup>-2</sup>	96.9% / 32x



Angular Sensing Resolution Comparison





## Sensing Resolution (Error Variance) Analysis

- Translational Sensing
  - □ 2 accelerometers in each sensing direction:

$$\frac{1}{\sigma_A^2} = \frac{1}{\sigma_{Ai}^2} + \frac{1}{\sigma_{Aj}^2} \rightarrow \sigma_A = \frac{\sigma_{Ai}}{\sqrt{2}}$$

- $\hfill\square$  Sensing resolution improves by a factor of  $2^{\frac{1}{2}}$
- Better orientation estimation → more complete removal of gravity → better translation estimation



## Microsurgery with Active Handheld Instrument





### Integration Drift of Inertial Sensors

- - Error accumulates and grows unbounded over time
- Poor sensing accuracy





### Measurement Model

- Measurement model allows error analysis and compensation
- Measurement Model = Physical (Deterministic) Model + Stochastic Model





## Accelerometer Model

#### Calibration

- Record accelerometer outputs at orientation inline ( $V_{+g}$ ) and opposite ( $V_{-g}$ ) to gravity
- Linear model
  - □ Acceleration,

$$A = (V_o - B)/SF \qquad g$$

□ Scale factor,

$$SF = \frac{1}{2}(V_{+g} - V_{-g}) V/g$$

Bias

$$B = \frac{1}{2} (V_{+g} + V_{-g}) \quad V$$





### Experimental Observations





### Phenomenological Modeling

• Bias, 
$$B_x(V_y, V_z) = B_x + g_x(V_y) + h_x(V_z)$$

Scale Factor,  $SF_x(V_z) = r_{x2}V_z^2 + r_{x1}V_z + r_{x0}$ 

Model

$$A_x = (V_x - B_x(V_y, V_z)) / SF_x(V_z)$$







### Sensing Experiment - Translation

- Motion generator
  - $\square$  10 Hz, 50  $\mu$ m p-p sinusoid
- Displacement Sensor
  - Infrared interferometer
    (Philtec, Inc., Model D63)
  - Sub-micrometer accuracy





## Sensing Results - Translation

	Rmse (mm/s <sup>2</sup> )	Bias (mm/s <sup>2</sup> )	Scale Factor (mm/s <sup>2</sup> )
Linear Model	300	272	6
Proposed Physical Model	31*	<5	<1
Error Reduction (%)	89.7	-	-

\* ADXL-203 rated rms noise =  $22.1 \text{ mm/s}^2$ 



## Stochastic Model

- Random noise analysis by Allan Variance method
- Dominant accelerometer noise types:
  - Velocity random walk
    - White noise in acceleration
  - Acceleration random walk
    - White noise in jerk
  - Trend / Bias Instability
    - Temperature drift





Temperature Drift

- Time varying zero bias
  - Heating up of internal circuitry
  - □ Steady state: 2-12 hours
- Solutions:
  - Modeling
  - Wait for steady state
  - Ovenization
    - Heat up sensor using power resistor
    - Changes sensor behavior




## Sensor Fusion via Cascaded Two-Stage Kalman Filtering





#### Augmented State Kalman Filtering

- Time domain sensor fusion
- Augmented state dynamic equation:



### Orientation Fusion

- Source 1: Differential sensing kinematics
  - $\square \quad \Omega_A[k] \text{ from differential acceleration}$
  - State transition matrix:

$$F[k] = \cos \frac{\left|\theta[k]\right|}{2} I_{(4\times4)} + \frac{1}{\left|\Omega[k]\right|} \sin \frac{\left|\theta[k]\right|}{2} \widetilde{\Theta}[k]_{(4\times4)}$$
$$\theta[k] = \Omega_A[k]T; \widetilde{\Theta}[k] = \frac{1}{2} \left[ \frac{\left[\Omega_A \times \left]_{3\times3}\right]}{-\Omega_{A1\times3}} + \frac{\Omega_{A3\times1}}{0} \right] T$$

- Dynamic state equation:  $q_A[k+1] = F[k]q_A[k] + \gamma[k]$
- Orientation defined by quaternion
- + : high resolution
  - : drift



#### Orientation Fusion

- Source 2: TRIAD
  - Gravity vector & Magnetic North vector are noncollinear
  - **TRIAD** algorithm:
    - $z_B = -g_B / ||g||;$
    - $y_B = z_B \times N_B / || z_B \times N_B ||;$
    - $x_B = y_B \times z_B$
  - $\square \qquad {}^{W}C_{B} = [x_{B} \ y_{B} \ z_{B}]$
- + : non-drifting
  - : poor resolution





#### Quaternion-based Kalman Filtering

 $\Omega_A$ 

600

Time(ms)

800

400

- Gravity Tracking
- Source 1: Ω<sub>A</sub>
  □ High resolution, drifting

0.4

0.35

0.3

0.25

0.2

0.15

0.1

0.05

0

0

200

Normalized Gravity

- Source 2:  $N_B + g_B$ Noisy, non-drifting
- Quaternion-based KF: Q-KF
  - Reduced noise, non-drifting





#### Sensing Experiment - Orientation





#### Translational Sensing Accuracy

- No non-drifting reference
  - Poor translational sensing accuracy
- Not important if tremor is separable from drift and intended motion





### Microsurgery with Active Handheld Instrument



### Frequency Selective Filters Phase Characteristics

- Physiological tremor has a distinct frequency bands:8 – 12 Hz
  - □ Voluntary motion:  $\leq$  1 Hz; Electrical noise: >> 12 Hz
- Classical frequency selective bandpass / band-stop (notch) filters
  - $\Box \quad Phase \ Iag \equiv Group \ (time) \ delay$
  - Filtered signal is a time delayed version of the actual sensed motion
  - Unacceptable condition for real-time error canceling application: compensating action might worsen the error



## Zero Phase Filtering

- Separation of tremor from the intended motion without introducing phase lag
  - Prediction/projection capability
  - Adaptive
    - Non-linear phase response of IIR filter, i.e. phase characteristic changes with frequency
- Two proposed algorithms
  - Weighted-frequency Fourier Linear Combiner (WFLC)
  - Adaptive Phase Compensating Band-pass Filter



#### Fourier Linear Combiner (FLC)

• Truncated Fourier series to adaptively estimate amplitude and phase of periodic signal with *known frequency* ( $\omega_0$ )





Weighted-frequency Fourier Linear Combiner (WFLC)

- Extends FLC to also adaptively estimate the frequency using another LMS algorithm
- Band-pass filter to select the band of interest
  - Assumption: rate of change of the dominant input signal frequency is slow
- Zero-phase notch (band-stop) filter effect





### Weighted-frequency Fourier Linear Combiner (WFLC)





Weighted-frequency Fourier Linear Combiner (WFLC) Experiment

- 1 DOF motion canceling experiment
- Ave. rms tremor amplitude reduced 69%
- Stability problem
  - Double adaptive algorithm





Filter Phase Characteristics

- Low-pass filters create phase lag
- High-pass filters create phase lead





## Adaptive Phase Compensating Band-pass Filter

- The idea:
  - To design a cascaded low-pass and high-pass filters such that phase lag of low-pass is compensated by phase lead of high-pass for a certain known input frequency
  - WFLC to estimate
    the instantaneous
    frequency
- Motivation
  - Most sensors come with built-in low pass filters





# Implementation

- Design LP-HP filter pairs with equal and opposite phase characteristics
- Filter design frequency band: 3 – 7 Hz
- Filter type: Elliptical 2<sup>nd</sup> order
- Roots of transfer function can be modeled by a linear function





 $\times$  - Poles

o - Zeros



## Adaptive Phase Compensating Band-pass Filter





## Motion Canceling Experiment

- Motion generator oscillating at 2.0 Hz
- Camcorder recording a rectangular target
  - 25 frames per second
- Image post processing to simulate real-time compensation





### Adaptive Phase Compensating Band-pass Filter

 Rmse: Raw footage

 = 2.61 pixels
 Compensated
 = 0.66 pixels

 Error reduction: 75%





### Microsurgery with Active Handheld Instrument





#### Piezoelectric Actuator Hysteresis

**+**:

- High bandwidth
- Fast response
- High output force
- :
  - Hysteresis
- ~15% of max. displacement





## Commercial Piezo-System with Feedback

#### Controller

- Piezo-driven 3 axis micro-positioner
  - □ Polytec-PI, Germany, NanoCube<sup>TM</sup> P-611
  - □ >\$ 10,000
  - Feedback sensors: strain gages
  - $\square$  Tracking a 10 Hz, 100  $\mu m$  p-p sinusiod
    - Hysteresis still present
    - Low-pass filtered behavior









### Open-loop Feedforward Controller with Inverse Hysteresis Model

- Develop a mathematical model that closely describes the hysteretic behavior of a piezoelectric actuator
- Existence of an inverse hysteresis model



#### Prandtl-Ishlinskii (PI) Operator

Rate independent backlash operator:

$$H_r = \max\{x(t) - r, \min\{x(t) + r, y_0\}\}$$

Linearly weighted superposition of backlash operators:





# Modified PI Operator

Backlash operators are symmetric but real hysteresis is not



Modeling saturation by linearly weighted superposition of dead-zone operators:





#### Modified PI Operator

#### $z(t) = \Gamma[x](t) = \vec{w}_s^T \cdot \vec{S}_d[\vec{w}_h^T \cdot \vec{H}_r[x, \vec{y}_0]](t)$



#### Inverse Modified PI Hysteresis Model





#### Inverse Modified PI Operator



#### Piezoelectric Hysteresis is Rate Dependent

- Basic assumption of Prandtl-Ishlinskii operator:
  - Hysteresis is rate independent
- Our observation:
  - Hysteresis is rate dependent
- Tremor frequency is time varying and person specific
  - □ 8-12 Hz





## Rate-dependent PI Operator

- Assume saturation is rate independent
- Sum of the backlash weights up to r<sub>i</sub> (slope of the hysteresis curve at interval i) is linearly dependent on actuation rate

$$W_{hi} = \Sigma w_{hi};$$



$$W_{hi}(\dot{x}(t)) = W_{hi}(\dot{x}_0) + c_i \dot{x}(t), \ i = 0...n$$



#### Rate Dependent PI Hysteresis Model

#### Rate dependent model:

 $z(t) = \Gamma[x, \dot{x}](t) = \vec{w}_s^T \cdot \vec{S}_d[\vec{w}_h(\dot{x}(t))^T \cdot \vec{H}_r[x, \vec{y}_0]](t)$ 

- Also a PI type  $\rightarrow$  Inverse exists
- Rate dependent inverse model

$$\Gamma^{-1}[\hat{z}](t) = \vec{w}_{h}(\dot{x}(t))^{T} \cdot \vec{H}_{r'(\dot{x}(t))}[\vec{w}_{s}^{T} \cdot \vec{S}_{d'}[\hat{z}], \vec{y}_{0}](t)$$



#### Open-Loop Feedforward Controller with Inverse Rate-Dependent PI Hysteresis Model



Open-Loop Feedforward Controller with Inverse Rate-Dependent PI Hysteresis Model

Tracking multiple frequency non-stationary sinusoids







2

0

-2 0 Error

0.05

0.1

0.15

0.2

#### Dynamic Motion Tracking Results

	Without model	Rate- independent	Rate- dependent
rmse $\pm \sigma(\mu m)$	$1.02 \pm 0.07$	$0.31 \pm 0.03$	$0.15 \pm 0.003$
$\frac{\text{rmse}}{\text{p-p amplitude}}(\%)$	9.2	2.8	1.4
max error $\pm \sigma$ (µm)	$1.91 \pm 0.08$	$0.89\pm0.04$	$0.59\pm0.06$
$\frac{\text{max error}}{\text{p - p amplitude}}(\%)$	17.3	8.0	5.3

rms noise of interferometer = 0.01  $\mu$ m



#### Tremor Tracking Results

Tracking recordings of real tremor using 1 piezoelectric stack
 Rmse = 0.64% of max ampl.; Max error = 2.4% of max ampl.




## Microsurgery with Active Handheld Instrument





### Design of Parallel Mechanism





Manipulator Design

- 3 DOF piezoelectric-driven parallel manipulator
  - $\square$  1 actuator per axis, max effective stroke = 12.5  $\mu$ m
  - Motion amplification = 9.4x, total stroke > 100  $\mu$ m
- Tool tip approximated as a point, hence only 3 DOF manipulation
- Parallel manipulator design because
  - Rigidity, compactness, and design simplicity
- Located at the front end to balance the weight of the instrument



## Design of Parallel Mechanism - New

- IEEE EMBS 2005 (Shanghai) Best Student Design Competition winner
  - David Choi et al.
- Monolith design using Stereolithography
- Ø22 x 58 mm







Manipulator Kinematics

- Inverse kinematics
  - Modeled as Lee & Shah RS-type
  - Closed-form solution
- No internal singularity





## Workspace Analysis

- $X_{max}$ ,  $Y_{max} = 650 \ \mu m$
- $Z_{max} = 100 \ \mu m$
- Tremor Space =  $\emptyset$  50  $\mu$ m





## Manipulator 3D Tracking Result

- Tracking planar circle of Ø200 μm
- Mean tracking rmse ~ 12.1 μm





## Microsurgery with Active Handheld Instrument





#### Motion Canceling Experiment

- Translation only
  - Generated motion: 9 Hz, 91 μm p-p
- Ave compensated tip motion over 10 runs = 60 μm p-p
- 34.3% reduction
- 3D optical sensing system
  - $\Box$  < 1.0 µm rms accuracy





## Motion Canceling Experiment





## Micron Canceling Hand Tremor



Total range: **52%** reduction

RMS amplitude: **47%** reduction



Other Applications

Surgery and Diagnostics

Active compensation of periodic human physiological and pathological motion

- Beating heart, breathing, etc.
- Pathological tremor due to Parkinson's diseases, multiple sclerosis, etc.
- Military optical tracking devices
  Handheld, vehicle & ship mounted
- Consumer camera/camcorder



# Other Applications: Cell Manipulation / Dissection





Questions & Comments

#### Wei Tech Ang School of Mechanical & Aerospace Engineering Nanyang Technological University Singapore wtang@ntu.edu.sg

